Pilot Superone Mathematics

Class 9th

Exercise 1.1

1. Find the order of the following matrices.

$$A = \begin{bmatrix} 2 & 3 \\ -5 & 6 \end{bmatrix}, \qquad B = \begin{bmatrix} 2 & 0 \\ 3 & 5 \end{bmatrix}, \quad C = \begin{bmatrix} 2 & 4 \end{bmatrix}$$

$$D = \begin{bmatrix} 4 \\ 0 \\ 6 \end{bmatrix}, \qquad E = \begin{bmatrix} a & d \\ b & e \\ c & f \end{bmatrix}, \quad F = \begin{bmatrix} 2 \end{bmatrix}$$

$$G = \begin{bmatrix} 2 & 3 & 0 \\ 1 & 2 & 3 \\ 2 & 4 & 5 \end{bmatrix}, \quad H = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 0 & 6 \end{bmatrix}$$

Solution: $A = \begin{bmatrix} 2 & 3 \\ -5 & 6 \end{bmatrix}$

Number of Rows (R) \$2

Number of Columns = 2

Order of the matrix = R by C

Order of the matrix = 2 by 2

$$B = \begin{bmatrix} 2 & 0 \\ 3 & 5 \end{bmatrix}$$

Order = 2 by 2

$$C = \begin{bmatrix} 2 & 4 \end{bmatrix}$$

Order = 1 by 2

$$D = \begin{bmatrix} 4 \\ 0 \\ 6 \end{bmatrix}$$

Order = 3 by 1

$$E = \begin{bmatrix} a & d \\ b & e \\ c & f \end{bmatrix}$$

Order = 3 by 2

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$$F = [2]$$
Order = 1 by 1
$$G = \begin{bmatrix} 2 & 3 & 0 \\ 1 & 2 & 3 \\ 2 & 4 & 5 \end{bmatrix}$$
Order = 3 by 3
$$H = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 0 & 6 \end{bmatrix}$$
Order = 2 by 3

2. Which of the following matrices are equal?

$$A = \begin{bmatrix} 3 \end{bmatrix}, \quad B = \begin{bmatrix} 3 & 5 \end{bmatrix}, \quad C = \begin{bmatrix} 5 - 2 \end{bmatrix}$$

$$D = \begin{bmatrix} 5 & 3 \end{bmatrix}, \quad E = \begin{bmatrix} 4 & 0 \\ 6 & 2 \end{bmatrix}, \quad F = \begin{bmatrix} 2 \\ 6 \end{bmatrix}$$

$$G = \begin{bmatrix} 3 - 1 \\ 3 + 3 \end{bmatrix}, \quad H = \begin{bmatrix} 4 & 0 \\ 6 & 2 \end{bmatrix}, \quad I = \begin{bmatrix} 3 & 3 + 2 \end{bmatrix}$$

$$J = \begin{bmatrix} 2+2 & 2-2 \\ 2+4 & 2+0 \end{bmatrix}$$

Solution:

(i)
$$A = C$$
 (ii) $B = I$ (iii) $E = H = J$

(iv)
$$F = G$$

Order of one is equal to the order of the other and their corresponding elements are equal.

Q.3. Find the values of a, b, c and d which satisfy the matrix equation.

$$\begin{bmatrix} a+c & a+2b \\ c-1 & 4d-6 \end{bmatrix} = \begin{bmatrix} 0 & -7 \\ 3 & 2d \end{bmatrix}$$

Solution:



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Pilot Superone Mathematics c-1=3(iii) a + 2b = -7(iii) 4d - 6 = 2d (iv) c-1 = 3 From (ii) c = 3 + 1 = 4a+c=0 (i)a+4 = 0 From (il) a = -44d-6=2d From (iv) 4d - 2d = 62d = 6d = 3a+2b = -7 From (iii)

Putting value of 'a'.

$$-4 + 2b = -7$$

 $2b = -7 + 4$
 $2b = -3$
 $b = -\frac{3}{2}$

Thus a=-4, $b=-\frac{3}{2}$, c=4, d=3

Types of Matrices:

Row Matrix: A row matrix has only ONE row, e.g.

 $A = [3-2 \ 0]$ is a row matrix.

Column Matrix: A column matrix has only ONE column e.g.

$$B = \begin{bmatrix} 1 \\ 2 \\ -2 \end{bmatrix}$$
 is a column matrix.

Rectangular Matrix: If the number of rows is not equal to the number of columns in a matrix then it is a rectangular matrix.



Written/Composed by: - SHANZAD IFTIKHAR Contact # 0313-5665666 Website: www.download.casanutes.com . E-mail: raoshahzadi.rdkhar@gmail.com

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Square Matrix: A matrix is called a square matrix if its number of rows is equal to its number of columns.

Null or Zero Matrix: A matrix is called a null or zero matrix if each of its entries is zero.

Transpose of a Matrix: A matrix obtained by interchanging rows into columns or columns into rows is called a transpose of the given matrix.

Negative of a Matrix: A matrix obtained by changing the signs of all the entries of a matrix is called negative of the given matrix.

Symmetric Matrix: A square matrix is symmetric if it is equal to its transpose. If A is a square matrix then its symmetrix matric is written as A^1 and $A^1 = A$.

Skew-Symmetric Matrix: A square matrix A is said to be skew-symmetric if $A^{\dagger} = -A$

Diagonal Matrix: A square matrix is called a diagonal matrix if atleast any one of the entries of its diagonal is not zero and non-diagonal entries must all be zero. e.g.

Scalar Matix. A diagonal matrix is called a scalar matrix, if all the diagonal entries are same and non-zero.

for example $\begin{bmatrix} k & 0 & 0 \\ 0 & k & 0 \\ 0 & 0 & k \end{bmatrix}$ where k is a constant.

$$A = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 3 & 0 \\ 0 & 0 & 0 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 4 & 0 \\ 0 & 0 & 5 \end{bmatrix}$$

Identity Matrix: A diagonal matrix is called identity (unit) matrix if all diagonal entries are 'I'. It is denoted by I.

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Exercise 1.2

ı. Find the following matrices, identify unit matrices, row matrices, column matrices and null matrices.

$$A = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}, B = \begin{bmatrix} 2 & 3 & 4 \end{bmatrix}, C = \begin{bmatrix} 4 \\ 0 \\ 6 \end{bmatrix}$$
$$D = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, E = \begin{bmatrix} 0 \end{bmatrix}, F = \begin{bmatrix} 5 \\ 6 \\ 7 \end{bmatrix}$$

Solution:

$$A = \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

A is a zero matrix.

$$B = \begin{bmatrix} 2 & 3 & 4 \end{bmatrix}$$

B is a row matrix.

$$C = \begin{bmatrix} A \\ 0 \\ 6 \end{bmatrix}$$

C is a column matrix.

$$D = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

D is an identity (unit) matrix.

$$E = [0]$$

E is a zero matrix.

$$F = \begin{bmatrix} 5 \\ 6 \\ 7 \end{bmatrix}$$

F is a column matrix.

- Q.2. From the following matrices, identify.

 - (a) Square matrices (b) kectangular matrices
 - (c) Row matrices
- (d) Column matrices

Pilot Superone Mathematics (e) Identity matrices (f) Null matrices (i) $\begin{bmatrix} -8 & 2 & 7 \\ 12 & 0 & 4 \end{bmatrix}$ (ii) $\begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix}$ (iii) $\begin{bmatrix} 6 & -4 \\ 3 & -2 \end{bmatrix}$ (iv) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ (v) $\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$ (vi) $\begin{bmatrix} 3 & 10 & -1 \end{bmatrix}$ Solution: $\begin{bmatrix} 6 & -4 \\ 3 & -2 \end{bmatrix}, \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, \begin{bmatrix} 1 & 2 & 3 \\ -1 & 2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \dots Square matrices$ $\begin{bmatrix} -8 & 2 & 7 \\ 12 & 0 & 4 \end{bmatrix}$, $\begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix}$, $\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$... Rectangular matrices $\begin{bmatrix} 3 & 10 & -1 \end{bmatrix}, \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$ $\begin{bmatrix} 3 \\ 0 \\ 1 \end{bmatrix}, \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix} \dots Column matrix$ $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots Identity matrix$ $\begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ 0 0 0 ... Zero matrix or mill

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From the following matrices, identify diagonal, scalar and unit (identity).

$$A = \begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix}, B = \begin{bmatrix} 2 & 0 \\ 0 & -1 \end{bmatrix}, C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$D = \begin{bmatrix} 3 & 0 \\ 0 & 0 \end{bmatrix}, and E = \begin{bmatrix} 5-3 & 0 \\ 0 & 1+1 \end{bmatrix}$$

Solution:

$$A = \begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix}, B = \begin{bmatrix} 2 & 0 \\ 0 & -1 \end{bmatrix} \dots Diagonal matrices$$

$$C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, D = \begin{bmatrix} 3 & 0 \\ 0 & 0 \end{bmatrix}, E = \begin{bmatrix} 5-3 & 0 \\ 0 & 1+1 \end{bmatrix}$$

$$A = \begin{bmatrix} 4 & 0 \\ 0 & 4 \end{bmatrix}, E = \begin{bmatrix} 5-3 & 0 \\ 0 & 1+1 \end{bmatrix} \dots Scalar matrices$$

$$C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \dots Identity matrix$$

Q.4. Find negative of matrices A,B,C,D and F when:

$$C = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$
 Identity matrix
$$Q.4. \quad \text{Find negative of matrices A,B,C,D and } A = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}, B = \begin{bmatrix} 3 & -1 \\ 2 & 1 \end{bmatrix}, C = \begin{bmatrix} 2 & 6 \\ 3 & 2 \end{bmatrix}$$

$$D \approx \begin{bmatrix} -3 & 2 \\ -4 & 5 \end{bmatrix}, E = \begin{bmatrix} 1 & -5 \\ 2 & 3 \end{bmatrix}$$
Solution:

 $A = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$ sign of every element is changed.

Class 9* Pilot Superone Mathematics $-A = -\begin{bmatrix} 1 \\ 0 \end{bmatrix} = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$ $B = \begin{bmatrix} 3 & -1 \\ 2 & 1 \end{bmatrix}$ $-B = -\begin{bmatrix} 3 & -1 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} -3 & 1 \\ -2 & -1 \end{bmatrix}$ $C = \begin{bmatrix} 2 & 6 \\ 3 & -2 \end{bmatrix}$ $-C = -\begin{bmatrix} 2 & 6 \\ 3 & -2 \end{bmatrix} = \begin{bmatrix} -2 & -6 \\ -3 & 2 \end{bmatrix}$ $D = \begin{bmatrix} -3 & 2 \\ -4 & 5 \end{bmatrix}$ $E = \begin{bmatrix} 1 & -5 \\ 2 & 3 \end{bmatrix}$ $-E = -\begin{bmatrix} 1 \\ 2 \end{bmatrix}$ $-D = -\begin{bmatrix} -3 & 2 \\ -4 & 5 \end{bmatrix} = \begin{bmatrix} 3 & -2 \\ 4 & -5 \end{bmatrix}$ $-E = -\begin{bmatrix} 1 & -5 \\ 2 & 3 \end{bmatrix} = \begin{bmatrix} -1 & 5 \\ -2 & -3 \end{bmatrix}$ Find the transpose of each of the following matrices. $A = \begin{bmatrix} 0 \\ 1 \\ 2 \end{bmatrix}, B = \begin{bmatrix} 5 & 1-6 \end{bmatrix}, C = \begin{bmatrix} 1 & 2 \\ 2 & -1 \\ 3 & 0 \end{bmatrix}$ $D = \begin{bmatrix} 2 & 3 \\ 0 & 5 \end{bmatrix}, E = \begin{bmatrix} 2 & 3 \\ -4 & 5 \end{bmatrix}, F = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

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$$A = \begin{bmatrix} 0 \\ 1 \\ -2 \end{bmatrix}$$
 columns are changed into rows

$$A^{f} = \begin{bmatrix} 0 & 1-2 \end{bmatrix}$$

$$B = \begin{bmatrix} 5 & 1-6 \end{bmatrix} ; B^{I} = \begin{bmatrix} 5 \\ 1 \\ -6 \end{bmatrix}$$

$$C = \begin{bmatrix} 1 & 2 \\ 2 & -1 \\ 3 & 0 \end{bmatrix} \; ; \; D^f = \begin{bmatrix} 1 & 2 & 3 \\ 2 & -1 & 0 \end{bmatrix}$$

$$D = \begin{bmatrix} 2 & 3 \\ 0 & 5 \end{bmatrix} \; ; \; D^I = \begin{bmatrix} 2 & 0 \\ 3 & 5 \end{bmatrix}$$

$$E = \begin{bmatrix} 2 & 3 \\ -4 & 5 \end{bmatrix} ; E^l = \begin{bmatrix} 2 & -4 \\ 3 & 5 \end{bmatrix}$$

$$F = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} ; F^t = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}$$

Q.6. Verify that if
$$A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$ then

(i)
$$(A^{l})^{l} = A$$
 (ii) $(B^{l})^{l} = B$

Solution

$$6(i) \quad A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$
$$A^{I} = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$$



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$$(A^t)^t = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} = A$$

$$6(ii) \quad B = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$$

$$B^f = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$(B^t)^t = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix} = B$$

Addition and subtration of Matrices

Remember:

- Two matrices are conformable for addition if they have the same order.
- (ii) In case of addition, corresponding elements are added.
- (iii) In case of subtraction, corresponding elements are subtracted in an order.

Commutative and Associative Laws of Addition of Matrices:

(a) Commutative law under Addition.

$$A + B = B + A$$

(b) Associative law under addition.

$$(A + B) + C = A + (B + C)$$

Additive identity of a matrix

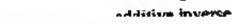
For any matrix A and zero matrix O of the same order. O is called additive identity of A as

$$A + O = O + A$$

Additive Inverse of a matrix

If A and B are two matrices of the same order such that

then A and B are called additive inverse of each other.
We change the sign of all the elements of a matrix to get its



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Exercise 1.3

1. Which of the following matrices are conformable for addition?

$$A = \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}, B = \begin{bmatrix} 3 \\ 1 \end{bmatrix}, C = \begin{bmatrix} 1 & 0 \\ 2 & -1 \\ 1 & 2 \end{bmatrix}$$
$$D = \begin{bmatrix} 2+1 \\ 3 \end{bmatrix}, E = \begin{bmatrix} 1 & 0 \\ 1 & 2 \end{bmatrix}, F = \begin{bmatrix} 3 & 2 \\ 1+1 & 4 \\ 3+2 & 2+1 \end{bmatrix}$$

Solution

order of A = 2 by 2 order of B = 2 by 1 order of C = 3 by 2 order of B = 2 by 1 order of E = 2 by 2 order of F = 3 by 2

Matrices of the same order are conformable for addition A and E, B and D, C and F are conformable for addition

Find the additive inverse of the following matrices.

$$A \begin{bmatrix} 2 & 4 \\ -2 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & 3 \\ 3 & -2 & 1 \end{bmatrix}, C = \begin{bmatrix} 4 \\ -2 \end{bmatrix}$$

$$D = \begin{bmatrix} 1 & 0 \\ 3 & -2 \\ 2 & 1 \end{bmatrix}, E = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}, F = \begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{2} \end{bmatrix}$$

Solution:

$$A = \begin{bmatrix} 2 & 4 \\ -2 & 1 \end{bmatrix}$$

$$-A = \begin{bmatrix} 2 & 4 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} -2 & 4 \\ 2 & -1 \end{bmatrix}$$
 (Additive inverse of A)
$$B = \begin{bmatrix} 1 & 0 & -1 \\ 2 & -1 & 3 \\ 3 & 2 & 1 \end{bmatrix}$$

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$B = \begin{bmatrix} 1 & 0 & -1 \\ 2 & -1 & 3 \\ 3 & -2 & 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 & 1 \\ -2 & 1 & -3 \\ 3 & 2 & 1 \end{bmatrix} $ (Additive inverse of B)	\sim
$c \begin{bmatrix} 4 \\ -2 \end{bmatrix}$	\cup
$C = \begin{bmatrix} 4 \\ -2 \end{bmatrix} = \begin{bmatrix} -4 \\ 2 \end{bmatrix} \text{ (additive inverse of C)}$	
$D = \begin{bmatrix} 1 & 0 \\ -3 & -2 \\ 2 & 1 \end{bmatrix}$	
$-D - \begin{bmatrix} 1 & 0 \\ -3 & 2 \\ 2 & 1 \end{bmatrix} = \begin{bmatrix} -1 & 0 \\ 3 & 2 \\ -2 & -1 \end{bmatrix} $ (additive inverse of D)	
$E = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	
$-E = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} $ (additive inverse of E)	
$-E = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$ (additive inverse of E) $F = \begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{2} \end{bmatrix}$ $-F = -\begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{2} \end{bmatrix} = \begin{bmatrix} -\sqrt{3} & -1 \\ 1 & -\sqrt{2} \end{bmatrix}$ (additive inverse of F)	
$-F = -\begin{bmatrix} \sqrt{3} & 1 \\ -1 & \sqrt{2} \end{bmatrix} = \begin{bmatrix} -\sqrt{3} & -1 \\ 1 & -\sqrt{2} \end{bmatrix}$ (additive inverse of F)	

Pilot Superone Mathematics $A \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}, B = \begin{bmatrix} 1 \\ -1 \end{bmatrix}, C = \begin{bmatrix} 1 & 1 & 2 \end{bmatrix}.$ $D = \begin{bmatrix} 1 & 2 & 3 \\ -1 & 0 & 2 \end{bmatrix}$ then find (i) $A + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ (ii) $B + \begin{bmatrix} 2 \\ 3 \end{bmatrix}$ (iii) $C + \begin{bmatrix} -2 & 1 & 3 \end{bmatrix}$ (iv) $D + \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix}$ $(v) \cdot 2 A$ (vi) (-1) B (vii) (-2) C (viii) 3D (ix) 3CSolution: $A + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ **(i)** $= \begin{bmatrix} -1 & 2 \\ 2 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} Putting A = \begin{bmatrix} 1 & 2 \\ 2 & 1 \end{bmatrix}$ $\begin{bmatrix} 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \end{bmatrix} Pu$ $= \begin{bmatrix} 1+1 & 2+1 \\ 2+1 & 1+1 \end{bmatrix} = \begin{bmatrix} 0 & 3 \\ 3 & 2 \end{bmatrix}$ (II) $B + \begin{bmatrix} -2 \\ 3 \end{bmatrix}$ $= \begin{vmatrix} 1 \\ -1 \end{vmatrix} + \begin{vmatrix} -2 \\ 3 \end{vmatrix} Putting B = \begin{bmatrix} 1 \\ -1 \end{vmatrix}$

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$$= \begin{bmatrix} 1 & -2 \\ -1 & +3 \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$$
(iii) $C + [2 \ 1 \ 3]$

$$= \{1 -1 \ 2] + [-2 \ 1 \ 3] Putting $C = [1 - 1 \ 2]$

$$-[1 -2 \ -1 + 1 \ 2 + 3] = [1 \ 0 \ 5]$$
(iv) $D + \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix}$

$$- \begin{bmatrix} 1 & 2 & 3 \\ 1 & 0 & 2 \end{bmatrix} + \begin{bmatrix} 0 & 1 & 0 \\ 2 & 0 & 1 \end{bmatrix} Putting $D = \begin{bmatrix} 1 & 2 & 3 \\ -1 & 0 & 2 \end{bmatrix}$

$$= \begin{bmatrix} 1 + 0 & 2 + 1 & 3 + 0 \\ 1 + 2 & 0 + 0 & 2 + 1 \end{bmatrix} = \begin{bmatrix} 1 & 3 & 3 \\ 1 & 0 & 3 \end{bmatrix}$$
(v) $2A$

$$= 2 \begin{bmatrix} -1 & 2 \\ 2 & 1 \end{bmatrix} Putting $A = \begin{bmatrix} -1 & 2 \\ 2 & 1 \end{bmatrix}$

$$= \begin{bmatrix} 2(-1) & 2(2) \\ 2(2) & 2(1) \end{bmatrix} = \begin{bmatrix} -2 & 4 \\ 4 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} (-1)(1) \\ (-)(-1) \end{bmatrix} = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} (-1)(1) \\ (-)(-1) \end{bmatrix} = \begin{bmatrix} -1 \\ 1 \end{bmatrix}$$$$$$$$

 $=(-2)[1 \ 1 \ 2]$ Putting $C = [1-1 \ 2]$

(vii) (−2) C

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$$= [(-2)(1) \ (-2)(-1) \ (-2)(2)] = [2 \ 2 - 4]$$
(viii) 3 D
$$= 3\begin{bmatrix} 1 & 2 & 3 \\ -1 & 0 & 2 \end{bmatrix} \quad Putting \quad D = \begin{bmatrix} 1 & 2 & 3 \\ 1 & 0 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 3(1) & 3(2) & 3(3) \\ 3(-1) & 3(0) & 3(2) \end{bmatrix} = \begin{bmatrix} 3 & 6 & 9 \\ 3 & 0 & 6 \end{bmatrix}$$
(ix) 3 C
$$= 3[1 - 1 & 2] \quad Putting \quad C = [1 - 1 & 2]$$

$$= [3(1) \ 3(-1) \ 3(2)] = [3 - 3 \ 6]$$

 Perform the indicated operations and sumplify the followers.

(i)
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$$

(ii)
$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$$

(iii)
$$\begin{bmatrix} 2 & 3 \end{bmatrix} + (\begin{bmatrix} 1 & 0 & 2 \end{bmatrix}) - \begin{bmatrix} 2 & 2 & 2 \end{bmatrix}$$

(iv)
$$\begin{bmatrix} 1 & 2 & 3 \\ -1 & -1 & -1 \\ 0 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix}$$

(v)
$$\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 2 \\ -2 & 1 & 0 \\ 0 & 2 & -1 \end{bmatrix}$$

Class 9th Pilot Superone Mathematics $\begin{bmatrix} 1 & 2 \\ \mathbf{0} & \mathbf{1} \end{bmatrix} + \begin{bmatrix} 2 & 1 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ (vi) Solution: 4 (i) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $= \left(\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix} \right) + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $= \begin{bmatrix} 1+0 & 0+2 \\ 0+3 & 1+0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $= \begin{bmatrix} 1 & 2 \\ 3 & 1 \end{bmatrix} + \begin{bmatrix} 1 & \mathbf{i} \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 1+\mathbf{i} & 2+\mathbf{j} \\ 3+\mathbf{i} & 1+0 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 4 & \mathbf{i} \end{bmatrix}$ **4** (ii) $\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $\begin{bmatrix} 0 & 1 \end{bmatrix}^{+} \begin{bmatrix} 3 & 0 \end{bmatrix}$ $= \begin{bmatrix} 1+0 & 0+2 \\ 0+3 & 1+0 \end{bmatrix} - \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix}$ $= \begin{bmatrix} 1 & 2 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \end{bmatrix}$ $= \left(\begin{bmatrix} 1 & \mathbf{6} \\ \mathbf{0} & \mathbf{1} \end{bmatrix} + \begin{bmatrix} 0 & 2 \\ 3 & \mathbf{0} \end{bmatrix} \right) \begin{bmatrix} 1 & 1 \\ 1 & \mathbf{0} \end{bmatrix}$ $= \begin{bmatrix} 1 & 2 \\ 3 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 2-1 \\ 3-1 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 2 & 1 \end{bmatrix}$

4 (iii) [2 3 1]+([1 0 2] [2 2 2])

 $[2 \ 3 \ 1]+[-1 \ -2 \ 0]$

 $=[2 \ 3 \ 1]+([1-2 \ 0 \ 2 \ 2 \ 2])$

 $[2 \ 1 \ 3 \ 2 \ 1+0]=[1 \ 1 \ 1]$

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$$\begin{bmatrix} 1 & 2 & 3 \\ -1 & -1 & -1 \\ 0 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 3 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1+1 & 2+1 & 3+1 \\ -1+2 & -+2 & -1+2 \\ 0+3 & 1+3 & 2+3 \end{bmatrix} = \begin{bmatrix} 2 & 3 & 4 \\ 1 & 1 & 1 \\ 3 & 4 & 5 \end{bmatrix}$$

$$4 (v) \begin{bmatrix} 2 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 0 & -2 \\ 2 & -1 & 0 \\ 0 & 2 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} 1+1 & 2+0 & 3-2 \\ 2 & 2 & 3 & 1 & 1+0 \\ 3+0 & 1+2 & 2-1 \end{bmatrix} = \begin{bmatrix} 2 & 2 & 1 \\ 0 & 2 & 1 \\ 3 & 3 & 1 \end{bmatrix}$$

$$4 (vi) \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 2 & 1 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1+2 & 2+1 \\ 0+1 & 1+0 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 3 & 3 \\ 1+1 & 1+1 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 3 & 3 \\ 1+1 & 1+1 \end{bmatrix} + \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 3+1 & 3+1 \\ 1+1 & 1+1 \end{bmatrix} = \begin{bmatrix} 4 & 4 \\ 2 & 2 \end{bmatrix}$$
For the matrices
$$A = \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix}, B = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} \text{ and } C = \begin{bmatrix} -1 & 0 & 0 \\ 0 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

verify the following rules:

$$(5) \qquad A + C = C + A$$

(ii)
$$A + B = R + A$$

 $\frac{24}{\text{(iv) } A + (B + A) = 2A + B}$ Pilot Superone Mathematics 24 B + C = C + B(iii) (v) (C - B) + A = C + (A - B)(vi) 2A + B = A + (A + B)(vii) $(C - B) \cdot A = (C - A) - B$ (viii) (A + B) + C = A + (B + C)(ix) A + (B - C) = (A - C) + B(x) 2A + 2B = 2(A + B)Solution: 5 (i) A+C=C+A LHS = A + C $= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$ $\begin{bmatrix} 1-1 & 2+0 & 3+0 \\ 2+0 & 3-2 & 1+3 \\ 1+1 & -1+1 & 0+2 \end{bmatrix} = \begin{bmatrix} 0 & 2 & 3 \\ 2 & 1 & 4 \\ 2 & 0 & 2 \end{bmatrix}$ (i) RHS = C + A $= \begin{bmatrix} 1 & \mathbf{0} & \mathbf{0} \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$ $\begin{bmatrix}
-1+1 & 0+2 & 0+3 \\
0+2 & -2+3 & 3+1 \\
1+1 & 1-1 & 2+0
\end{bmatrix} = \begin{bmatrix} 0 & 2 & 3 \\
2 & 1 & 4 \\
2 & 0 & 2 \end{bmatrix} (ii)$ $A + C = C + A \qquad From (i) and (ii)$ $S (ii) \quad A + B = B + A$ L.H.S = A + B $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$ $= \begin{bmatrix} 1+1 & 2-1 & 3+1 \\ 2+2 & 3-2 & 1+2 \\ 1+3 & -1+1 & 0+3 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} (i)$

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RHS =
$$\begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1+1 & 1+2 & 1+3 \\ 2+2 & -2+3 & 2+1 \\ 3+1 & 1-1 & 3+0 \end{bmatrix} = \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} (ii)$$

$$A+B=B+A \qquad From (l) and (ii),$$
S(iii) B+C=C+B

L.H.S = B+C
$$= \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 1-1 & -1+0 & 1+0 \\ 2+0 & 2 & 2 & 2+3 \\ 3+1 & 1+1 & 3+2 \end{bmatrix} = \begin{bmatrix} 0 & -1 & 1 \\ 2 & 4 & 5 \\ 4 & 2 & 5 \end{bmatrix} (ii)$$
RHS = C+B
$$= \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 1+3 & 1+2+3 \end{bmatrix} = \begin{bmatrix} 0 & -1 & 1 \\ 2 & -4 & 5 \\ 4 & 2 & 5 \end{bmatrix} (iii)$$

$$B+C=C+B \qquad From (i) and (ii)$$
S(Iv) A+(B+A) = 2A+B
L.H.S = A+(B+A)
$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

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$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix}$		_
$= \begin{bmatrix} 1+2 & 2+1 & 3+4 \\ 2+4 & 3+1 & 1+3 \\ 1+4 & -1+0 & 0+3 \end{bmatrix}$		0
$= \begin{bmatrix} 3 & 3 & 7 \\ 6 & 4 & 4 \\ 5 & -1 & 3 \end{bmatrix} (i)$	Q	
RHS = 2A + B		
$=2\begin{bmatrix}1 & 2 & 3\\2 & 3 & 1\\1 & -1 & 0\end{bmatrix}+\begin{bmatrix}1 & 1 & 1\\2 & -2 & 2\\3 & 1 & 3\end{bmatrix}$		
$=\begin{bmatrix} 2(1) & 2(2) & 2(3) \\ 2(2) & 2(3) & 2(1) \\ 2(1) & 2(-1) & 2(0) \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$		
$= \begin{bmatrix} 2 & 4 & 6 \\ 4 & 6 & 2 \\ 2 & -2 & 0 \end{bmatrix} + \begin{bmatrix} I & -1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$		
$= \begin{bmatrix} 2+1 & 4 & 1 & 6+1 \\ 4+2 & 6-2 & 2+2 \\ 2+3 & -2+1 & 0+3 \end{bmatrix}$		
$= \begin{bmatrix} 3 & 3 & 7 \\ 6 & 4 & 4 \\ 5 & -1 & 3 \end{bmatrix} $ (ii)		
A + (B + A) = 2A + B		
$\begin{bmatrix} 5 & -1 & 3 \end{bmatrix}$ $A + (B + A) = 2A + B$ $5(v) (C - B) + A = C + (A - B)$ $L + S (C - B) + A$ $= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \end{bmatrix} \cdot \begin{bmatrix} 1 & 2 \\ 2 & 3 \end{bmatrix}$		
ило (C-р)+A	_	
$-\left\{ \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix}, -\begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} \right\} + \begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 1 & 1 \end{bmatrix}$	37	
$(\begin{bmatrix} 1 & \hat{1} & \hat{2} \end{bmatrix} \begin{bmatrix} \hat{3} & \hat{1} & \hat{3} \end{bmatrix}) \begin{bmatrix} \hat{1} & \hat{1} \\ \hat{1} & 1 \end{bmatrix}$	ōJ	

Pilot Superone Mathematics Class 9" $= \begin{bmatrix} -1-1 & 0+1 & 0-1 \\ 0-2 & -2+2 & 3-2 \\ 1 & 3 & 1-1 & 2 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$ $= \begin{bmatrix} 2 & 1 & 1 \\ -2 & 0 & 1 \\ -2 & 0 & -1 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$ $= \begin{bmatrix} -2+1 & 1+2 & -1+3 \\ -2+2 & 0+3 & 1+1 \\ -2+1 & 0+1 & -1+0 \end{bmatrix} = \begin{bmatrix} 1 & 3 & 2 \\ 0 & 3 & 2 \\ 1 & -1 & -1 \end{bmatrix} (1)$ $R.H S = \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$ $= \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 2+1 & 3-1 \\ 2 & 2 & 3+2 & 1-2 \\ 1 & 3 & -1-1 & 0-3 \end{bmatrix}$ $= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix} + \begin{bmatrix} 0 & 3 & 2 \\ 0 & 5 & -1 \\ 2 & -2 & -3 \end{bmatrix}$ $= \begin{bmatrix} -1+0 & 0+3 & 0+2 \\ 0+0 & -2+5 & 3-1 \\ 1-2 & 1 & 2 & 2-3 \end{bmatrix}$

 $\begin{bmatrix} -1 & 3 & 2 \\ 0 & 3 & 2 \\ -1 & 1 & -1 \end{bmatrix}$ (ii) $\begin{bmatrix}
-1 & 1 & -1 \\
(C & B) + A = C + (A & B)$ From (i) and (ii) $5 \text{ (vi)} \quad 2A + B = A + (A + B)$ L H S = 2A + B $\int_{-1}^{2} -1$

$$(C B) + A = C + (A B)$$

$$5 (vi) 2A + B = A + (A + B)$$

$$-2\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

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$$= \begin{bmatrix} 2(1) & 2(2) & 2(3) & 2(1) \\ 2(2) & 2(3) & 2(1) & 1 \\ 2(1) & 2(-1) & 2(0) \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 4 & 6 \\ 4 & 6 & 2 \\ 2 & 2 & 2 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 2 + 1 & 4 - 1 & 6 + 1 \\ 4 + 2 & 6 - 2 & 2 + 2 \\ 2 + 3 & -2 + 1 & 0 + 3 \end{bmatrix} = \begin{bmatrix} 3 & 3 & 7 \\ 6 & 4 & 4 \\ 5 & -1 & 3 \end{bmatrix} \quad (i)$$

$$R. H. S. = A + (A + B)$$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 2 & 1 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 + 1 & 2 - 1 & 3 + 1 \\ 2 + 2 & 3 - 2 & 1 + 2 \\ 1 + 3 & -1 + 1 & 0 + 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1 + 2 & 2 + 1 & 3 + 4 \\ 2 + 4 & 3 + 1 & 1 + 3 \\ 1 + 4 & -1 + 0 & 0 + 3 \end{bmatrix} = \begin{bmatrix} 3 & 3 & 7 \\ 6 & 4 & 4 \\ 5 & 1 & 3 \end{bmatrix} \quad (fi)$$

$$2A + B = A + (A + B) \quad From \quad (i) \quad and \quad (in)$$

$$5 \text{ (vis) } \quad (C - B) - A = (C - A) - B$$

$$L. H. S = (C - B) \quad A$$

$$= \begin{bmatrix} 1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} - \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} -1 - 1 & 0 + 1 & 0 - 1 \\ 0 - 2 & -2 + 2 & 3 - 2 \\ 1 - 3 & 1 - 1 & 2 & 3 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$$

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Piket Superone Mathematics 29 Class 9th
$$= \begin{bmatrix} 2 & 1 & -1 \\ -2 & 0 & 1 \\ -2 & 0 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}$$

$$- \begin{bmatrix} -2-1 & 1-2 & 1-3 \\ -2-2 & 0-3 & 1-1 \\ -2 & 1 & 0+1 & -1-0 \end{bmatrix} = \begin{bmatrix} -3 & -1 & -4 \\ -4 & -3 & 0 \\ -3 & 1 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} -1-1 & 0-2 & 0 & 3 \\ 0-2 & -2-3 & 3 & 1 \\ 1-1 & 1+1 & 2 & 0 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -2 & -3 \\ 2 & -5 & 2 \\ 0 & 2 & 2 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -2 & -3 \\ 2 & -5 & 2 \\ 0 & 2 & 2 \end{bmatrix} - \begin{bmatrix} 1 & -1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$$

$$- \begin{bmatrix} -2+1 & -2+1 & 3+1 \\ -2-2 & -5+2 & 2-2 \\ 0 & 3 & 2-1 & 2-3 \end{bmatrix} = \begin{bmatrix} -3 & -1 & -4 \\ 4 & -3 & 0 \\ -3 & 1 & -1 \end{bmatrix}$$

$$= \begin{bmatrix} (C-B) - A = (C-A) - B & From (i) \text{ and (iii)}$$

$$5 \text{ (viii) } (A+B) + C = A + (B+C)$$

$$L.H. S. = (A+B, +C)$$

$$= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 1+1 & 2-1 & 3+1 \\ 2+2 & 3-2 & 1+2 \\ 1+3 & -1+1 & 0+3 \end{bmatrix} + \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix} + \begin{bmatrix} 1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$$

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MATHEMATICS FOR 9TH CLASS (UNIT # 1)

Pilot Superone Mathematics 30 Class 9th $\begin{bmatrix} 2 & 1 & 1+0 & 4+0 \\ 4+0 & 2 & 3+3 \\ 4+1 & 0+1 & 3+2 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 4 \\ 4 & -1 & 6 \\ 5 & 1 & 5 \end{bmatrix}$ (i) R.H.S. = A + (B + C) $= \left(\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} \right) + \begin{bmatrix} -1 & 0 & 0 \\ 0 & 2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$ $\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 - 1 & -1 + 0 & 1 + 0 \\ 2 + 0 & 2 - 2 & 2 + 3 \\ 3 + 1 & 1 + 1 & 3 + 2 \end{bmatrix}$ $= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 0 & -1 & 1 \\ 2 & 4 & 5 \\ 4 & 2 & 5 \end{bmatrix}$ $= \begin{bmatrix} 1+0 & 2-1 & 3+1 \\ 2+2 & 3-4 & 1+5 \\ .+4 & -1+2 & 0+5 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 4 \\ 4 & 1 & 6 \\ 5 & 1 & 5 \end{bmatrix}$ (ii) (A + B) + C - A + (B + C) From (i) and (ii) 5 (ix) A + (B - C) = (A - C) + BL.H.S. = A + (B - C) $= \begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix} - \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix}$ $-\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 1+1 & -1 & 0 & 1 & 0 \\ 2-0 & -2+2 & 2-3 \\ 3-1 & 1-1 & 3 & 2 \end{bmatrix}$ $-\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix} + \begin{bmatrix} 2 & -1 & 1 \\ 2 & 0 & -1 \\ 2 & 0 & 1 \end{bmatrix}$ $\begin{bmatrix} 1+2 & 2-1 & 3+1 \\ 2+2 & 3+0 & 1 & 1 \\ 1+2 & -1+0 & 0+1 \end{bmatrix} = \begin{bmatrix} 3 & 1 & 4 \\ 4 & 3 & 0 \\ 3 & -1 & 1 \end{bmatrix}$ (i)

 $R.H.S. = (A \cdot C) + B$

Pilot Superone Mathematics Class 9" $= \left(\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & -1 & 0 \end{bmatrix}, \begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 3 \\ 1 & 1 & 2 \end{bmatrix} \right) + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$ $\begin{bmatrix} 1+1 & 2 & 0 & 3-0 \\ 2-0 & 3+2 & 1-3 \\ 1-1 & -1 & 1 & 0-2 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$ $= \begin{bmatrix} 2 & 2 & 3 \\ 2 & 5 & -2 \\ 0 & -7 & -2 \end{bmatrix} + \begin{bmatrix} 1 & 1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}$ $= \begin{bmatrix} 2+1 & 2-1 & 3+1 \\ 2+2 & 5 & 2 & -2+2 \\ 0+3 & 2+1 & 2+3 \end{bmatrix} - \begin{bmatrix} 3 & 1 & 4 \\ 4 & 3 & 0 \\ 3 & 1 & 1 \end{bmatrix} (u)$ A + (B - C) = (A - C) + B From (i) and (ii) 5(x) = 2A + 2B = 2(A + B)LHS = 2A + 2B $-\begin{bmatrix} 2(1) & 2(2) & 2(3) \\ 2(2) & 2(3) & 2(1) \\ 2(1) & 2(-1) & 2(0) \end{bmatrix} + \begin{bmatrix} 2(1) & 2(-1) & 2(1) \\ 2(2) & 2(-2) & 2(2) \\ 2(3) & 2(1) & 2(3) \end{bmatrix}$ $\begin{bmatrix} 2 & 4 & 6 \\ 4 & 6 & 2 \\ 2 & 2 & 0 \end{bmatrix} + \begin{bmatrix} 2 & -2 & 2 \\ 4 & -4 & 4 \\ 6 & 2 & 6 \end{bmatrix}$ $= \begin{bmatrix} 2 + 2 & 4 - 2 & 6 + 2 \\ 4 + 4 & 6 - 4 \end{bmatrix}$ $= \begin{bmatrix} 2 + 2 & 4 - 2 & 6 + 2 \\ 4 + 4 & 6 - 4 \end{bmatrix}$ $= \begin{bmatrix} R.H.c.$ $= \begin{bmatrix} 2+2 & 4-2 & 6+2 \\ 4+4 & 6-4 & 2+4 \\ 2+6 & -2+2 & 0+6 \end{bmatrix} = \begin{bmatrix} 4 & 2 & 8 \\ 8 & 2 & 6 \\ 8 & 0 & 6 \end{bmatrix}$ (i) $\approx 2\left[\begin{bmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 1 & 1 & 0 \end{bmatrix} + \begin{bmatrix} 1 & -1 & 1 \\ 2 & -2 & 2 \\ 3 & 1 & 3 \end{bmatrix}\right]$

Class 9th Pilot Superone Mathematics $= 2 \begin{bmatrix} 1+1 & 2-1 & 3+1 \\ 2+2 & 3-2 & 1+2 \\ 1+3 & -1+1 & 0+3 \end{bmatrix}$ $= 2 \begin{bmatrix} 2 & 1 & 4 \\ 4 & 1 & 3 \\ 4 & 0 & 3 \end{bmatrix}$ $= \begin{bmatrix} 2(2) & 2(1) & 2(4) \\ 2(4) & 2(1) & 2(3) \\ 2(4) & 2(0) & 2(3) \end{bmatrix} = \begin{bmatrix} 4 & 2 & 8 \\ 8 & 2 & 6 \\ 8 & 0 & 6 \end{bmatrix} \quad (ii)$ 2A + 2B = 2(A + B) From (i) and (ii) If $A = \begin{bmatrix} 1 & -2 \\ 3 & 4 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 7 \\ -3 & 8 \end{bmatrix}$ then find: (i) 3A - 2B (ii) $2A^1 - 3B^1$ 3A - 2B6 (i) $= 3\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} - 2\begin{bmatrix} 0 & 7 \\ -3 & 8 \end{bmatrix}$ Putting values of A and B $-\begin{bmatrix} 3(1) & 3(-2) \\ 3(3) & 3(4) \end{bmatrix} - \begin{bmatrix} 2(0) & 2(7) \\ 2(-3) & 2(8) \end{bmatrix}$ $\begin{bmatrix}
3 & -6 \\
9 & 12
\end{bmatrix} = \begin{bmatrix}
0 & 14 \\
-6 & 16
\end{bmatrix}$ $\begin{bmatrix}
3-0 & -6-14 \\
9+6 & 12 & 16
\end{bmatrix} = \begin{bmatrix}
3 & 20 \\
15 & 4
\end{bmatrix}$ 6 (ii) $2A^{t}$ $3B^{t}$ $A = \begin{bmatrix} 1 & -2 \\ 2 & A \end{bmatrix}$ We find A^l and B^l

First Superone Mathematics 33 Class
$$9^a$$

$$A^i = \begin{bmatrix} 1 & 3 \\ -2 & 4 \end{bmatrix}$$

$$B = \begin{bmatrix} 0 & 7 \\ -3 & 8 \end{bmatrix}$$

$$2A^1 & 3B^1$$

$$= 2\begin{bmatrix} 1 & 3 \\ -2 & 4 \end{bmatrix} & 3\begin{bmatrix} 0 & -3 \\ 7 & 8 \end{bmatrix} & (Putting values A^i \text{ and } B^i)$$

$$= \begin{bmatrix} 2(1) & 2(3) \\ 2(2) & 2(4) \end{bmatrix} & \begin{bmatrix} 3(0) & 3(-3) \\ 3(7) & 3(8) \end{bmatrix}$$

$$= \begin{bmatrix} 2 & 6 \\ 4 & 8 \end{bmatrix} - \begin{bmatrix} 0 & -9 \\ 21 & 24 \end{bmatrix}$$

$$= \begin{bmatrix} 2 & -0 & 6+9 \\ -4-21 & 8-24 \end{bmatrix} = \begin{bmatrix} 2 & 15 \\ 25 & -16 \end{bmatrix}$$
7. If $2\begin{bmatrix} 2 & 4 \\ -3 & a \end{bmatrix} + 3\begin{bmatrix} 1 & b \\ 8 & -4 \end{bmatrix} = \begin{bmatrix} 7 & 10 \\ 18 & 1 \end{bmatrix}$, then
find a and b.
$$\begin{bmatrix} 7 & 10 \\ 18 & 1 \end{bmatrix} = 2\begin{bmatrix} 2 & 4 \\ 3 & a \end{bmatrix} + 3\begin{bmatrix} 1 & b \\ 8 & -4 \end{bmatrix}$$

$$= \begin{bmatrix} 2(2) & 2(4) \\ 2(-3) & 2a \end{bmatrix} + \begin{bmatrix} 3(1) & 3b \\ 8 & -4 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 10 \\ 18 & 1 \end{bmatrix} = 2 \begin{bmatrix} 2 & 4 \\ 3 & a \end{bmatrix} + 3 \begin{bmatrix} 1 & b \\ 8 & -4 \end{bmatrix}$$
$$= \begin{bmatrix} 2(2) & 2(4) \\ 2(-3) & 2a \end{bmatrix} + \begin{bmatrix} 3(1) & 3b \\ 3(8) & 3(-4) \end{bmatrix}$$

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$$= \begin{bmatrix} 4 & 8 \\ -6 & 2a \end{bmatrix} + \begin{bmatrix} 3 & 3b \\ 24 & -12 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 10 \\ 18 & 1 \end{bmatrix} = \begin{bmatrix} 4+3 & 8+3b \\ -6+24 & 2a-12 \end{bmatrix}$$

$$\begin{bmatrix} 7 & 10 \\ 18 & 1 \end{bmatrix} = \begin{bmatrix} 7 & 8+3b \\ 18 & 2a-12 \end{bmatrix}$$

Therefore 8 + 3b = 10 (Corresponding elements are same)

$$3b = 2$$

$$b = \frac{2}{3}$$
and
$$1 = 2a \quad 12$$

$$13 = 2a$$

$$a = \frac{13}{2}$$

8. If
$$A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$
, $B = \begin{bmatrix} I & 1 \\ 2 & 0 \end{bmatrix}$ then verify that

(1)
$$(A + B)^{t} = A^{t} + B^{t}$$

(ii)
$$(A - B)^{t} = A^{t} - B^{t}$$

(i)
$$(A + B)^{t} = A^{t} + B^{t}$$
 (ii) $(A - B)^{t} = A^{t} - B^{t}$
(iii) $(A - B)^{t} = A^{t} - B^{t}$
(iv) $(A - B)^{t} = A^{t} - B^{t}$

(v)
$$B + B^{t}$$
 is symmetric



8 (i)
$$A \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$
, $B \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$

Solution.

$$(A + B)^{t} = A^{t} + B^{t}$$

 $(A + B)^{t} = ?$ (Taking L.H.S)
 $A + B = ?$ (Taking L.H.S)

Prior Superone Mathematics $A+B=\begin{bmatrix}1&2\\0&1\end{bmatrix}+\begin{bmatrix}1&1\\2&0\end{bmatrix}$ $= \begin{bmatrix} 1+1 & 2+1 \\ 0+2 & 1+0 \end{bmatrix}$ $A+B=\begin{bmatrix}2&3\\2&1\end{bmatrix}$ $(A+B)^{t} = \begin{bmatrix} 2 & 2 \\ 3 & 1 \end{bmatrix}$ (i) $A^{t} + B^{t} = 9$ (Taking R H S) $A^{t} = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix} \text{ and }$ $\mathbf{B}^{\mathsf{t}} = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$ $A^{1} + B^{1} = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$ $\begin{bmatrix} 1+1 & 0+2 \\ 2+1 & 1+0 \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 3 & 1 \end{bmatrix}$ (ii) printip.de $(A + B)^{t} = A^{t} + B^{t}$ From (i) and (ii) 8 (ii) If $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$ Prove that $(A - B)^{\dagger} = A^{\dagger} - B^{\dagger}$ LHS = $A - B = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$

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$$\begin{bmatrix}
1-1 & 2-1 \\ 0-2 & 1-0
\end{bmatrix} = \begin{bmatrix}
0 & 1 \\ -2 & 1
\end{bmatrix}$$
(A B)^f = $\begin{bmatrix} 0 & -2 \\ 1 & 1 \end{bmatrix}$

R.H.S A = $\begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$

A¹ = $\begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$, B = $\begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$, B^f = $\begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$

A^f - B^f = $\begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$ - $\begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$

$$= \begin{bmatrix} 1-1 & 0-2 \\ 2-1 & 1-0 \end{bmatrix} = \begin{bmatrix} 0 & -2 \\ 1 & 1 \end{bmatrix} \text{ (ii)}$$
(A - B)^{1/2} A¹ - B¹ From (i) and (ii)

8 (iii) If $A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$

Show A + A' is a symmetric matrix.
$$A' = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$$

$$A + A' = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} + \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$$

Pilot Superone Mathematics 37 Class 9th $= \begin{bmatrix} 1+i & 2+0 \\ 0+2 & 1+i \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$ $(A+A^{i})^{t} = \begin{bmatrix} 2 & 2 \\ 2 & 2 \end{bmatrix}$

So A + A is a symmetric matrix.

Note: If M = M then M is a symmetric matrix.

8 (iv) If
$$A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

Show that $A - A^{t}$ is symmetric matrix.

$$A^{I} = \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$$

$$A - A^{I} = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 2 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1-1 & 2-0 \\ 0-2 & 1-1 \end{bmatrix} = \begin{bmatrix} 0 & 2 \\ -2 & 0 \end{bmatrix}$$
Now
$$(A - A^{I})^{I} = \begin{bmatrix} 0 & -2 \\ 2 & 0 \end{bmatrix} = A - A^{I}$$

· A - A1 is Not a symmetric matrix

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8 (v) If
$$B = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$$

Show B + Bt is a symmetric matrix.

$$B^t = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$B + B^{f} = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix} + \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$
$$= \begin{bmatrix} 1+1 & 1+2 \\ 2+1 & 0+0 \end{bmatrix} = \begin{bmatrix} 2 & 3 \\ 3 & 0 \end{bmatrix}$$

$$(1, -B^l)^l = \begin{bmatrix} 2 & 3 \\ 3 & 0 \end{bmatrix}$$

Now
$$B + B^t = (B + B^t)^t$$

B + B' is a symmetric matrix.

8 (vi)
$$B = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix}$$

$$E^{I} = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$E^{I} = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$E^{I} = \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$E^{I} = \begin{bmatrix} 1 & 1 \\ 2 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 2 \\ 1 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 1 - 1 & 1 & 2 \\ 2 - 1 & 0 - 0 \end{bmatrix}$$

Pilot Superone Mathematics 39 Class 9^a $= \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix}$

$$= \begin{bmatrix} 1 & 0 \end{bmatrix}$$

$$(B - B^f)^f = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \neq B - B^f$$

B - B^t is Not a symmetric matrix Multiplication of Matrices

- (i) Two matrices are conformable for multiplication if to number of columns of the first matrix is equal to the number of rows of the second matrix.
- (ii) Association Law of multiplication
 If A, B and C are three matrices conformable I multiplication then associative law of multiplication is
 (AB) C = A (BC)
- (iii) Distribution Laws of Multiplication over Addition and Subtraction.

i.
$$A(B+C) = AB + AC$$

ii.
$$(A + B) C = AC + BC$$

iii.
$$A(B C) = AB AC$$

EV.
$$(A - B) C = AC - BC$$

(iv) Multiplication Identity of a matrix. If A is a matrix and B another matrix. B is called the identity matrix of A under multiplication if:

$$AB = A = BA$$

(v) Singular and Non - singular Matrix

A square matrix A called singular

if |A| = 0 and if $|A| \neq 0$ then

A is called non consular and

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(vi) Adjoint of a Matrix

Adjoint of a square matrix is obtained by interchanging the diagonal entries and changing the sign of other entries. Adjoint of matrix A is denoted as Adj A

(vii) Multiplication inverse of a non - singular square matrix if A and B will multiplication of each other if:

Multiplication inverse of A is written as A-1

(viii) Inverse of matrix using Adjoint.

Let M be a square matrix

Then
$$M = \frac{Adj M}{|M|}$$



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Exercise 1.4

1. Which of the following product of matrices is conformable for multiplication?

(i)
$$\begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} -2 \\ 3 \end{bmatrix}$$
 (ii)
$$\begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$$

(iii)
$$\begin{bmatrix} 1 \\ -1 \end{bmatrix} \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix}$$
 (iv)
$$\begin{bmatrix} 1 & 2 \\ 0 & -1 \\ -1 & -2 \end{bmatrix} \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 2 \end{bmatrix}$$

(v)
$$\begin{bmatrix} 3 & 2 & 1 \\ 0 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ 2 & 3 \end{bmatrix}$$

1 (i) Let
$$A = \begin{bmatrix} 1 & -1 \\ 0 & 2 \end{bmatrix}$$
, $B = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$

Number of columns of A = 2Number of rows of B = 2Multiplication is possible.

1 (ii) Let
$$A = \begin{bmatrix} 1 & -1 \\ 1 & 0 \end{bmatrix}$$
, $B = \begin{bmatrix} 2 & -1 \\ 1 & 3 \end{bmatrix}$

Number of columns in A = 2Number of rows in B = 2Multiplication is possible.

1 (iii) Let
$$A = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$
, $B = \begin{bmatrix} 0 & 1 \\ -1 & 2 \end{bmatrix}$

Number of columns in A = 1

Number of rows in B = 2

Multiplication is NOT possible.

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1 (iv) Let
$$A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \\ -1 & 2 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 2 \end{bmatrix}$

Number of columns in A = 2

Number of rows in B = 2

Multiplication is possible.

1 (v) Let
$$A = \begin{bmatrix} 3 & 2 & 1 \\ & & \\ 0 & 1 & -1 \end{bmatrix}$$
, $B = \begin{bmatrix} 1 & -1 \\ 0 & 2 \\ -2 & 3 \end{bmatrix}$

Number of columns in A = 3

Number of rows in B = 3

Multiplication AB is possible.

2. If
$$A = \begin{bmatrix} 3 & 0 \\ 1 & 2 \end{bmatrix}$$
, $B = \begin{bmatrix} 6 \\ 5 \end{bmatrix}$ find (i)AB (ii) BA (if possible)

2(i)
$$AB = \begin{bmatrix} 3 & 0 \\ -1 & 2 \end{bmatrix} \begin{bmatrix} 6 \\ 5 \end{bmatrix}$$

= $\begin{bmatrix} 1(6) & +0(5) \\ -1(6) & +2(5) \end{bmatrix} \begin{bmatrix} 18+0 \\ -6+10 \end{bmatrix} \begin{bmatrix} 18 \\ 4 \end{bmatrix}$

- 2(BA is NOT possible
- 3. Find the following products.

(i)
$$\begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$
 (ii) $\begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 5 \\ 4 \end{bmatrix}$

(iii)
$$\begin{bmatrix} 3 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$
 (iv) $\begin{bmatrix} 6 & -0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$

(v)
$$\begin{bmatrix} 1 & 2 \\ -3 & 0 \\ 6 & 1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 0 & -4 \end{bmatrix}$$

Class 9th Pilot Superone Mathematics 43 Solution:

3 (i)
$$\begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

= $\begin{bmatrix} 1(4) + 2(0) \end{bmatrix} = \begin{bmatrix} 4 + 0 \end{bmatrix} = \begin{bmatrix} 4 \end{bmatrix}$

3 (ii)
$$\begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 5 \\ -4 \end{bmatrix}$$

= $\begin{bmatrix} 1(5) + 2(-4) \end{bmatrix} = \begin{bmatrix} 5 - 8 \end{bmatrix} = \begin{bmatrix} 3 \end{bmatrix}$

3 (iii)
$$\begin{bmatrix} -3 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

 $\begin{bmatrix} -3(4) + 0(0) \end{bmatrix} = \begin{bmatrix} -12 + 0 \end{bmatrix} = \begin{bmatrix} -12 \end{bmatrix}$

3 (iv)
$$\begin{bmatrix} 6 & 0 \end{bmatrix} \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

$$AB = [6(4) + 0(0)] = [24 + 0] = [24]$$

3 (v)
$$\begin{bmatrix} 1 & 2 \\ -3 & 0 \\ 6 & -1 \end{bmatrix} \begin{bmatrix} 4 & 5 \\ 0 & 4 \end{bmatrix}$$

$$= \begin{bmatrix} 1(4)+\lambda(0) & 1(5)+2(-4) \\ -3(4)+0(0) & -3(5)+0(-4) \\ 6(4)+(-1)(0) & 6(5)+(-1)(-4) \end{bmatrix}$$

$$= \begin{bmatrix} 4+0 & 5-8 \\ 12+0 & -15+0 \\ 24+0 & 30+8 \end{bmatrix} = \begin{bmatrix} 4 & -3 \\ 12 & -15 \\ 24 & 38 \end{bmatrix}$$

Multiply the following matrices.

$$= \begin{bmatrix} 1(4)+\lambda(0) & 1(5)+2(-4) \\ -3(4)+0(0) & -3(5)+0(-4) \\ 6(4)+(-1)(0) & 6(5)+(-1)(-4) \end{bmatrix}$$

$$= \begin{bmatrix} 4+0 & 5-8 \\ 12+0 & -15+0 \\ 24+0 & 30+8 \end{bmatrix} = \begin{bmatrix} 4 & -3 \\ 12 & -15 \\ 24 & 38 \end{bmatrix}$$
4. Multiply the following matrices.
$$\begin{bmatrix} 2 & 3 \\ 1 & 1 \\ 0 & -2 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 3 & 0 \end{bmatrix} \quad (b) \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ -1 & 1 \end{bmatrix}$$

Pilot Superone Mathematics (c) $\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$ (d) $\begin{bmatrix} 8 & 5 \\ 6 & 4 \end{bmatrix} \begin{bmatrix} 2 & -\frac{5}{2} \\ -4 & 4 \end{bmatrix}$

(e)
$$\begin{bmatrix} -1 & 2 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$$

4 (a) Solution:

$$\begin{bmatrix} 2 & 3 \\ 1 & 1 \\ 0 & 2 \end{bmatrix} \begin{bmatrix} 2 & -1 \\ 3 & 0 \end{bmatrix}$$

$$= \begin{bmatrix} 2(2)+3(3) & 2(-1)+3(0) \\ 1(2)+1(3) & 1(-1)+1(0) \\ 0(2)+(-2)(3) & 0(-1)+(-2)(0) \end{bmatrix}$$

$$\begin{bmatrix} 4+9 & -2+0 \\ 2+3 & -1+0 \\ 0 & 6 & 0+0 \end{bmatrix} = \begin{bmatrix} 13 & -2 \\ 5 & -1 \\ -6 & 0 \end{bmatrix}$$

4 (b)
$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ -1 & 1 \end{bmatrix}$$

4 (b)
$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & 4 \\ -1 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1(1) + 2(3) + 3(-1) & 1(2) + 2(4) + 3(1) \\ 4(1) + 5(3) + 6(-1) & 4(2) + 5(4) + 6(1) \end{bmatrix}$$

$$= \begin{bmatrix} 1 + 6 - 3 & 2 + 8 + 3 \\ 4 + 15 - 6 & 8 + 20 + 6 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 13 \\ 13 & 34 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} 1+6-3 & 2+8+3 \\ 4+15-6 & 8+20+6 \end{bmatrix}$$

$$-\begin{bmatrix} 4 & 13 \\ 13 & 34 \end{bmatrix}$$

4(t)
$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ -1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$

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Pilot Superone Mathematics 45 $= \begin{bmatrix} 1(1)+2(4) & 1(2)+2(5) & 1(3)+2(6) \\ 3(1)+4(4) & 3(2)+4(5) & 3(3)+4(6) \\ 1(1)+1(4) & -1(2)+1(5) & -1(3)+1(6) \end{bmatrix}$ $= \begin{bmatrix} 1+8 & 2+10 & 3+12 \\ 3+16 & 6+20 & 9+24 \\ -1+4 & -2+5 & -3+6 \end{bmatrix}$ $= \begin{bmatrix} 9 & 12 & 15 \\ 19 & 26 & 33 \\ 3 & 3 & 3 \end{bmatrix}$ $\begin{bmatrix} 8 & 5 \\ 6 & 4 \end{bmatrix} \begin{bmatrix} 2 & -\frac{5}{2} \\ -4 & 4 \end{bmatrix}$ $= \begin{bmatrix} 16 & 20 & -20 + 20 \\ 12 - 16 & -15 + 16 \end{bmatrix}$ - 4 0 $\begin{array}{ccc} \blacksquare \text{ (e)} & \begin{bmatrix} -1 & 2 \\ 1 & 3 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$ $= \begin{bmatrix} -1(0) + 2(0) & -1(0) + 2(0) \\ 1(0) + 3(0) & 1(0) + 3(0) \end{bmatrix}$ $= \begin{bmatrix} 0+0 & 0+0 \\ 0+0 & 0+0 \end{bmatrix} - \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix}$

With annual description of the same for the transfer of the same Taken T

5. Let $A = \begin{bmatrix} 1 & 3 \\ 2 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 1 & 2 \\ -3 & -5 \end{bmatrix}$ and $C = \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$

verify whether

(i)
$$AB = BA$$

(iii)
$$A(B+C) = AB+AC$$
 (iv) $A(B-C)=AB-AC$

5(i)
$$A = \begin{bmatrix} 1 & 3 \\ 2 & 0 \end{bmatrix}, B \begin{bmatrix} 1 & 2 \\ -3 & -5 \end{bmatrix}$$

$$AB = \begin{bmatrix} -1(1) + 3(-3) & -1(2) + 3(-5) \\ 2(1) + 0(-3) & 2(2) + 0(-5) \end{bmatrix}$$

$$= \begin{bmatrix} -1 - 9 & 2 & 15 \\ 2 + 0 & 4 + 0 \end{bmatrix} = \begin{bmatrix} -10 & -17 \\ 2 & 4 \end{bmatrix} (i)$$
and $BA = \begin{bmatrix} 1 & 2 \\ -3 & 5 \end{bmatrix} \begin{bmatrix} -1 & 3 \\ 2 & 0 \end{bmatrix}$

$$= \begin{bmatrix} 1(-1)+2(2) & 1(3)+2(0) \\ -3(-1)+(-5)(2) & -3(3)+(-5)(0) \end{bmatrix}$$

$$= \begin{bmatrix} -1+4 & 3+0 \\ 3-10 & -9+0 \end{bmatrix} = \begin{bmatrix} 3 & 3 \\ 7 & 9 \end{bmatrix} (ii)$$

AB + BA From (i) and (ii)

$$A \begin{bmatrix} -1 & 3 \\ 2 & 0 \end{bmatrix}, B = \begin{bmatrix} 1 & 2 \\ -3 & -5 \end{bmatrix}, C = \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$$

$$A(BC) = ?$$

BC (First we find BC)

$$= \begin{bmatrix} 1 & 2 \\ -3 & -5 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$$
$$\begin{bmatrix} 1(2) + 2(1) & 1(1) + 2(3) \\ -3(2) + (-5)(1) & 3(1) + (-5)(3) \end{bmatrix}$$



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$$BC = \begin{bmatrix} 2+2 & 1+6 \\ -6 & 5 & -3 & 15 \end{bmatrix}$$

$$= \begin{bmatrix} 4 & 7 \\ -11 & -18 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 3 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 4 & 7 \\ -11 & -18 \end{bmatrix}$$

$$= \begin{bmatrix} 1(4)+3(-11) & -1(7)+3(-18) \\ 2(4)+0(-11) & 2(7)+0(-18) \end{bmatrix}$$

$$= \begin{bmatrix} 4-33 & -7-54 \\ 8+0 & 14+0 \end{bmatrix}$$

$$= \begin{bmatrix} -37 & -61 \\ 8 & 14 \end{bmatrix} (I)$$

(AB)C = ?

$$AB = \begin{bmatrix} -1 & 3 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & -5 \end{bmatrix}$$
 First we find AB

$$AB = \begin{bmatrix} -1 & 3 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 3 & .5 \end{bmatrix}$$
 First we find
$$= \begin{bmatrix} -1(1) + 3(-3) & -1(2) + 3(-5) \\ 2(1) + 0(-3) & 2(2) + 0(-5) \end{bmatrix}$$

$$= \begin{bmatrix} -1 - 9 & -2 - 15 \\ 2 + 0 & 4 + 0 \end{bmatrix}$$

$$= \begin{bmatrix} 10 & -17 \\ 2 & 4 \end{bmatrix}$$
Now, we find (AB)C
$$(AB)C = \begin{bmatrix} -10 & 17 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$$

$$= \begin{bmatrix} -10(2) + (-17)(1) & -10(1) & -10(1) &$$

$$(AB)C = \begin{bmatrix} -10 & 17 \\ 2 & 4 \end{bmatrix} \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$$
$$= \begin{bmatrix} -10(2) + (-17)(1) & -10(1) + (-17)(3) \\ 2(2) + 4(1) & 2(1) + 4(3) \end{bmatrix}$$

Class 9". Pilot Superone Mathematics $= \begin{bmatrix} -20 - 17 & -10 - 51 \\ 4 + 4 & 2 + 12 \end{bmatrix}$ $= \begin{bmatrix} 37 & -61 \\ 8 & 14 \end{bmatrix} (\mu)$ A(BC) = (AB) C From (i) and (ii) Prove that A(B+C) = AB+AC 5(iii) A(B+C)=?(B+C) . First we find (B+C) $= \begin{bmatrix} 1 & 2 \\ 3 & -5 \end{bmatrix} + \begin{bmatrix} 2 & 1 \\ 1 & 3 \end{bmatrix}$ $= \begin{bmatrix} 1+2 & 2+1 \\ -3+1 & 5+3 \end{bmatrix}$ $-\begin{bmatrix} 3 & 3 \\ -2 & -2 \end{bmatrix}$ $A(B+C) = \begin{bmatrix} -1 & 3 \\ 2 & 0 \end{bmatrix} \begin{bmatrix} 3 & 3 \\ -2 & -2 \end{bmatrix}$ $= \begin{bmatrix} -1(3)+3(-2) & -1(3)+3(-2) \\ 2(3)+0(-2) & 2(3)+0(-2) \end{bmatrix}$ $= \begin{bmatrix} 0 & -3-6 \\ 6+0 & 6+0 \end{bmatrix}$ $\begin{bmatrix} -9 & -9 \\ 6 & 6 \end{bmatrix} (t)$ $AB + AC = ? \quad Taking L.H.S.$ $= \begin{bmatrix} -3 & 6 & -3-6 \\ 6+0 & 6+0 \end{bmatrix}$ $= \begin{bmatrix} -1(1)+3(-3) & -1(2)+3(-5) \\ 2(1)+0(-3) & 2(2)+0(-5) \end{bmatrix}$

[2(1)+0(-3) 2(2)+0(-3)]

Pilot Superope Mathematics. $A = \frac{Ad_1 A}{|A|}$ $\mathbf{B}^{-1}\mathbf{A}^{-1} = \begin{bmatrix} -\frac{1}{6} & \frac{1}{3} \\ -\frac{1}{8} & -\frac{2}{8} \end{bmatrix} \begin{bmatrix} 1 & 0 \\ 1 & 0 \\ \frac{1}{8} & 2 \end{bmatrix}$ $\begin{bmatrix} -\frac{\pi}{3} \end{bmatrix} \begin{bmatrix} \frac{1}{8} & \frac{1}{2} \\ \frac{1}{6} & \frac{1}{3} & \frac{1}{3} & \frac{1}{6} & \frac{1}{6} & \frac{1}{3} & \frac{1}{2} \\ -\frac{1}{6} & \frac{1}{4} & \frac{1}{3} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{3} & \frac{1}{2} & \frac{1}{3} & \frac{1}{2} \\ -\frac{1}{6} & \frac{1}{4} & \frac{1}{24} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{3} & \frac{1}{6} & \frac{1}{3} & \frac{1}{2} & \frac{1}{3} & \frac{1}{6} & \frac{1}{3} & \frac{1}{3$

 $= \begin{vmatrix} 0 & t \\ 0 & 6 \\ -\frac{1}{8} & -\frac{t}{2} \end{vmatrix}$

 $(AB)^{4} = B^{-1}A$

From (i) and (ii)

"tor Superone Mathematics 66	Class 9th
6(a) $\mathbf{A} = \begin{bmatrix} -\frac{1}{2} & 0 \\ -1 & 2 \end{bmatrix}, \mathbf{D} = \begin{bmatrix} -3 & 1 \\ 2 & 2 \end{bmatrix}$, verify that: (DA) $\mathbf{A} = \begin{bmatrix} -1 & 0 \\ -1 & 2 \end{bmatrix}$	\cap
$(DA) = \begin{bmatrix} 3 & 1 \\ -2 & 2 \end{bmatrix} \begin{bmatrix} 4 & 0 \\ 1 & 2 \end{bmatrix}$	
$= \begin{bmatrix} 3(4) + 1(-1) & 3(0) + 1(-1) & 2(0) + 2(-1) & 2(0) + 2(-1) & 2(0) &$	21 (2)
$\begin{bmatrix} I2 & I & 0 + 2 \\ 8 + 2 & 0 + 4 \end{bmatrix}$	
$=\begin{bmatrix} II & 2 \\ I0 & 4 \end{bmatrix}$ $DA_{+} = \begin{bmatrix} I1 & 2 \\ -I0 & 4 \end{bmatrix}$	
$\begin{bmatrix} -i\theta & 4 \end{bmatrix}$ = (11)(4) (2)(-10) $-44 \cdot 20 - 64$	
$ \begin{bmatrix} 4 & 2 \\ 10 & 11 \end{bmatrix} $ Adi(DA)	
$ \begin{bmatrix} Adj (DA) \\ I\theta - II \end{bmatrix} $ $ \begin{bmatrix} Adj (DA) \\ DA \end{bmatrix} $ $ \begin{bmatrix} A - 2 \\ I\theta - II \end{bmatrix} $ $ \begin{bmatrix} A - 2 \\ A4 - 64 \\ I\theta - II \\ 64 - 64 \end{bmatrix} $	
$\begin{bmatrix} 4 & -2 \\ 10 & II \end{bmatrix} = \begin{bmatrix} 4 & 2 \\ 64 & 64 \\ 10 & II \\ 64 & 64 \end{bmatrix}$	

Pilot Superone Mathematics 67	Class 9th
$\begin{bmatrix} 1 & -1 \\ 16 & -32 \end{bmatrix}$ $\begin{bmatrix} 5 & 11 \\ 32 & 64 \end{bmatrix}$ $\begin{bmatrix} 32 & 64 \\ 32 & 64 \end{bmatrix}$	0
$A \begin{bmatrix} 1 & 0 \\ -10 & 2 \end{bmatrix}$	(),
A = (4)(2) - (-1)(0) = 8 = 0 - 8	O
$Adj A = \begin{bmatrix} 2 & 0 \\ 1 & 4 \end{bmatrix}$	
$A = A \operatorname{di} A = \begin{bmatrix} 2 & 0 \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 2 & 0 \\ 8 & 8 \end{bmatrix}$ $A = \begin{bmatrix} 1 & 1 \\ 1 & 1 \\ 8 & 8 \end{bmatrix}$	
$Adj A = \begin{bmatrix} 2 & 0 \\ j & 4 \end{bmatrix}$ $A = \begin{bmatrix} 2 & 0 \\ j & 4 \end{bmatrix}$ $A = \begin{bmatrix} 2 & 0 \\ 3 & 8 \\ j & 4 \\ k & 8 \end{bmatrix}$ $D = \begin{bmatrix} 3 & 1 \\ -2 & 2 \end{bmatrix}$ $D = \begin{bmatrix} 3 & 1 \\ 2 & 2 \end{bmatrix}$ $Adj D = \begin{bmatrix} 2 & -1 \\ -2 & 2 \end{bmatrix}$	
$D = \begin{bmatrix} 3 & 1 \\ -2 & 2 \end{bmatrix}$	
$ D = \begin{vmatrix} 3 & 1 \\ 2 & 2 \end{vmatrix}$	
(Au) D [2 3]	
$D^{-1} = \frac{Ad_1 D}{D} = \begin{bmatrix} 2 & -1 \\ 2 & 3 \end{bmatrix}$	

Well-state and the state of the

MATHEMATICS FOR 9TH CLASS (UNIT # 1)

Pilot Superone Mathematics 68 $=\begin{bmatrix} 2 & -t \\ 8 & 8 \\ 2 & 3 \\ 8 & 8 \end{bmatrix} = \begin{bmatrix} 1 & -\frac{1}{4} \\ \frac{1}{4} & \frac{3}{8} \end{bmatrix}$ $=\begin{bmatrix} 1 & 0 \\ \frac{1}{8} & \frac{1}{2} \end{bmatrix} \begin{bmatrix} \frac{1}{4} & -\frac{1}{8} \\ \frac{1}{4} & \frac{3}{8} \end{bmatrix}$ $=\begin{bmatrix} \frac{1}{4} \left(\frac{1}{4} \right) + 0 \left(\frac{1}{4} \right) & \frac{1}{4} \left(-\frac{1}{8} \right) + 0 \left(\frac{3}{8} \right) \\ \frac{1}{8} \left(\frac{1}{4} \right) + \frac{1}{2} \left(\frac{1}{4} \right) & \frac{1}{8} \left(-\frac{1}{8} \right) + \frac{1}{2} \left(\frac{3}{8} \right) \end{bmatrix}$ $=\begin{bmatrix} \frac{1}{16} + 0 & -\frac{1}{32} + 0 \\ \frac{1}{16} + \frac{1}{32} + \frac{1}{8} & -\frac{1}{64} + \frac{3}{16} \end{bmatrix}$ $=\begin{bmatrix} \frac{1}{16} & -\frac{1}{32} \\ \frac{5}{32} & \frac{11}{64} \end{bmatrix}$ (DA)-1 = A ID I From(i), (n)

SOLUTION OF SIMULTANEOUS LINEAR EQUATIONS

System of two linear equations in two variable in general form are.

ax + by = m, cx + dy = n where a, b, c, d, m, n are real numbers.

This system is also called simultaneous linear equations.

Cramer's Rule

Let
$$ax + by = m$$

$$cx + dy = n$$

writing the equations in matrix form

$$\begin{bmatrix} ax + by \\ cx + dy \end{bmatrix} = \begin{bmatrix} m \\ n \end{bmatrix}$$

Pilot Superme Mathematics

or
$$\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} m \\ n \end{bmatrix}$$

AX
B

When $A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}, X = \begin{bmatrix} x \\ y \end{bmatrix}, B = \begin{bmatrix} m \\ n \end{bmatrix}$

AX = B

$$X = A \cdot B$$

$$X = A \cdot B$$

$$X = \frac{A \cdot di \cdot A}{|A|} \times B ||A| \neq 0$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} dn & -bn \\ -cn & an \end{bmatrix} \begin{bmatrix} n \\ n \end{bmatrix}$$

Thus
$$x = \frac{dm - bn}{|A|} = \frac{A_x}{|A|}$$

And
$$y = \frac{an - cm}{|A|} = \frac{A_x}{|A|}$$

When $|A_x| = \begin{bmatrix} m & b \\ n & d \end{bmatrix}$

and
$$|A_y| = \begin{bmatrix} a & m \\ n & d \end{bmatrix}$$

Phot Superone Mathematics 70 Class 9

Exercise 1.6

- Use matrices if possible to solve the following system 0.1. of linear equations by
- The matrix inverse method **(i)**
- (**ii**)

Solution:-

1(i)
$$2x - 2y - 4$$

 $3x + 2y = 6$

Writing the equations in matrix form.

$$\begin{bmatrix} 2x & 2y \\ 3x + 2y \end{bmatrix} = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$$
Or
$$\begin{bmatrix} 2 & -2 \\ 3 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$$
Let
$$AX = 3$$
Where $4 \begin{bmatrix} 2 & -2 \\ 3 & 2 \end{bmatrix} A = \begin{bmatrix} x \\ y \end{bmatrix} B = \begin{bmatrix} 4 \\ 6 \end{bmatrix}$

$$[A] = \begin{bmatrix} 2 & 2 \\ 3 & 2 \end{bmatrix}$$

$$= (2)(2) \quad (-2)(3)$$

$$4 + 6 = 10 \neq 0$$

A is a non-singular matrix. Its multiplicative inverse is Λ^{-1}

AX = BNone

Pilot Superone M.	thematics	71		g.
or	X	$\Lambda^{-1}B$		
	Adı A	(2). (3)	X 10	\wedge
	Α 1	Α <u>Ι Α</u> 1Α		\cup
		$\begin{bmatrix} 2 & 2 \\ 3 & 2 \end{bmatrix}$	C	
		$\begin{bmatrix} \frac{1}{2} \\ \frac{1}{10} \end{bmatrix}$	7 1 1 1 1 2 2 1 2 2 1 2 2	
		3 10 1	$\begin{bmatrix} 75 \\ 2 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 & 2 \\ 3 & 1 \\ 10 \end{bmatrix} = \begin{bmatrix} 1 & 3 \\ 1 & 3 \end{bmatrix}$	
Non	х •	• #1 'B		
•		$\begin{bmatrix} 1 & 1 \\ 5 & 5 \\ -3 & 1 \\ 10 & 5 \end{bmatrix}$		
So, Esing Cran	\begin{bmatrix} \tau \\ \tau \end{bmatrix} =	$\begin{bmatrix} \frac{1}{5}(4) \\ \frac{3}{16}(4) \end{bmatrix}$	1 1 5 (6)	
3.00		1 ,	<i>y</i>	
317			6 11 5.	
50,	-	0	· .	
Lsing Cran				
`	2x + 2y = 6 $3x + 2y = 6$			•
	-			

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Pilos Su	perone Mathematics 72	Class 9 th
	$A = \begin{bmatrix} 2 & -2 \\ 3 & 2 \end{bmatrix}$	
	$A_{x} = \begin{bmatrix} 4 & -2 \\ 6 & 2 \end{bmatrix}$	
	$\mathbf{A}_{1} = \begin{bmatrix} 2 & 4 \\ 3 & 6 \end{bmatrix}$	
	$A \mid = \begin{vmatrix} 2 & -2 \\ 3 & 2 \end{vmatrix}$	
	$x = \frac{ A_x }{ A } = \frac{\begin{vmatrix} 4 & -2 \\ 6 & 2 \end{vmatrix}}{10}$	
	<u>(4)(2) - (- 2)(6)</u> 10	
	$-\frac{8+12}{10}-2$	
	$y = \frac{ A_y }{ A } = \frac{\begin{vmatrix} 2 & 4 \\ 3 & 6 \end{vmatrix}}{10}$	
	$y = \frac{1}{ A } = \frac{1}{ B }$ $= \frac{(2)(6) - (3)(4)}{ B }$ $= \frac{12 - 12}{ B } = 0$	
9,	$=\frac{12}{10}\frac{12}{0}=0$	
3 •	So. x 2. y 0	
7 (6)	2x + y = 3	
	6x + 5y = 1 Writing the equations in the matrix form	
	$\begin{bmatrix} 2x & +y \\ 6x & +5y \end{bmatrix} = \begin{bmatrix} 3 \\ l \end{bmatrix}$	
	וֹס וֹדֹבוֹ בֹּוֹ	

$$\begin{bmatrix} 2x & +y' \\ 6x & +5y \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$$
$$\begin{bmatrix} 2 & 1 \\ 6 & 5 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 1 \end{bmatrix}$$

ĢГ.

Pilot Superone Mathematics 73 Class 9th Let A X = BWhere $A = \begin{bmatrix} 2 & I \\ 6 & 5 \end{bmatrix}$, $X = \begin{bmatrix} x \\ 1 \end{bmatrix}$ $B = \begin{bmatrix} 3 \\ I \end{bmatrix}$

$$A_1 = \begin{bmatrix} 2 & I \\ 6 & 5 \end{bmatrix}$$

$$(2x)(5) = (1x)(6) = 10 - 6 = 4$$

A is a non-singular matrix

$$AX = B$$

$$X = A^{T}B$$

$$Adj A = \begin{bmatrix} 5 & -1 \\ -6 & 2 \end{bmatrix}$$

$$\mathbf{A}^{\mathsf{T}} \cdot \frac{\mathbf{A}\mathbf{d}_{\mathsf{T}}\mathbf{A}}{|\mathbf{A}|} = \begin{bmatrix} 5 & -1 \\ 6 & 2 \end{bmatrix}$$

$$\begin{bmatrix} 5 & -1 \\ 4 & 4 \\ 6 & 2 \\ 4 & 4 \end{bmatrix} = \begin{bmatrix} 3 & -1 \\ 4 & 3 \\ 2 & 2 \end{bmatrix}$$

Now

$$\mathbf{X} = \mathbf{A}^{\mathsf{T}} \mathbf{B}$$

$$\begin{bmatrix} 1 \\ 1 \end{bmatrix} = \begin{bmatrix} 4 & -4 \\ 3 & 1 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 3 \\ 1 \end{bmatrix}$$
$$\begin{bmatrix} \frac{3}{4} & \frac{3}{4} & \frac{1}{4} \\ \frac{3}{4} & \frac{3}{4} & \frac{1}{4} \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$
$$\begin{bmatrix} \frac{3}{4} & \frac{3}{4} & \frac{1}{4} & \frac{1}{4} \\ \frac{3}{2} & \frac{3}{4} & \frac{1}{4} & \frac{1}{4} \end{bmatrix} \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

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Pilot Superone Mathematic	;s 74	Class	<u>)`</u>
	[17 1]		
	1 4 4		
	212		\cap
	11.5		0
		:	
		1	
$\frac{7}{2}$:		
Using Cramer's (
2v			
Car -	ē. 1		
	A 2 7 6 5		
,	$A_i = \begin{bmatrix} 3 & I \\ I & 3 \end{bmatrix}$		
•••	$\begin{pmatrix} 2 & 3 \\ 6 & I \end{pmatrix}$		
	j2 <i>t</i> ° 6 3'		
	_		
0	(2K5) (EK	(6) 10 6 4	
N .	² 	, 51	
2.	$\chi = \frac{124\chi}{1\Lambda^4}$	4	
N. do	(3)(5) (1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(1)(15 4	
	<u>14</u> 7	4	
	4 . 5		

Well-state and the state of the

Prior Superone Mathematics 75 Class 9th

$$y = \frac{A_{5,1}}{A_{1}} = \frac{\begin{vmatrix} 2 & 3 \\ 16 & 1 \end{vmatrix}}{4}$$

$$-\frac{(2)(1) \cdot (3)(6)}{4} - \frac{2 \cdot 18}{4}$$

$$= \frac{16}{4} = -4$$

So.
$$x = \frac{7}{2}, y + 4$$

1(iii) $4x + 2y + 8$

$$3x - y = -1$$

Writing the equations in matrix form

or
$$\begin{bmatrix} 4x & +2y \\ 3x & y \end{bmatrix} = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$
$$\begin{bmatrix} 4 & 2 \\ 3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$$

where
$$\mathbf{A} = \begin{bmatrix} 4 & 2 \\ 3 & i \end{bmatrix}$$
, $X = \begin{bmatrix} x \\ y \end{bmatrix}$ $B = \begin{bmatrix} 8 \\ -1 \end{bmatrix}$

$$\Lambda = \begin{vmatrix} 4 & 2 \\ 3 & -4 \end{vmatrix}$$
= (4)(-1) (2)(3)
-4 6 = 10

$$AX = B$$

 $X = A^{-1}B$

$$Ad_{1}A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$A = \begin{bmatrix} A & 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$A = \begin{bmatrix} A & 1 & 2 \\ 3 & 4 \end{bmatrix}$$

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Pilot Superone Mathematics	76 Class 9 th
	$= \begin{bmatrix} \frac{-1}{-10} & \frac{-2}{-10} \\ \frac{-3}{-10} & \frac{4}{-10} \end{bmatrix} = \begin{bmatrix} \frac{1}{10} & \frac{1}{5} \\ \frac{3}{10} & \frac{2}{5} \end{bmatrix}$
	= A 'B
	$= \begin{bmatrix} \frac{1}{10} & \frac{1}{5} \\ \frac{3}{10} & \frac{-2}{5} \end{bmatrix} \begin{bmatrix} 8 \\ -1 \end{bmatrix}$
	$= \begin{bmatrix} \frac{1}{10}(8) + \frac{1}{5}(-1) \\ \frac{3}{10}(8) + \frac{2}{5}(-1) \end{bmatrix}$
	$\left[\frac{3}{10}(8) + \frac{2}{5}(-1)\right]$
•	$= \left[\frac{\frac{4}{5} - \frac{1}{5}}{\frac{12}{5} + \frac{2}{5}} \right]$
	$= \begin{bmatrix} \frac{3}{5} \\ \frac{14}{5} \end{bmatrix}$
So. x	$=\frac{3}{6}$
,	$=\frac{14}{5}$
Using Cramer's Ruk	
4x + 2y	
3x y	
A	$=\begin{bmatrix}4 & 2\\3 & -1\end{bmatrix}$

Pilot Superone Mathematics 77	Class 9 ^m
$\mathbf{A}_{\mathbf{K}} = \begin{bmatrix} 8 & 2 \\ -I & -I \end{bmatrix}$	
$A_y = \begin{bmatrix} 4 & 8 \\ 3 & -I \end{bmatrix}$	
$ \mathbf{A} = \begin{vmatrix} 4 & 2 \\ 3 & -1 \end{vmatrix}$	
=(4)(-1) -(2)(3)	
=-4-6=-10	
$x = \frac{ A_1 }{ A_1 } = \frac{\begin{vmatrix} 8 & 2 \\ -i & -1 \end{vmatrix}}{-10}$	
(8)(-1) - (2)(-1) -10	
$=\frac{-8+2}{-10}=\frac{-6}{-10}=\frac{3}{5}$	
$y = \frac{ A_y }{ A } = \frac{\begin{vmatrix} 4 & 8 \\ 3 & -1 \end{vmatrix}}{-10}$	
$=\frac{(4)(-1)-(8)(3)}{-10}=-$	<u>4 - 24</u> - 10
$=\frac{28}{-10}=\frac{14}{5}$	
3 14	
So, $x = \frac{1}{5}$, $y = \frac{14}{5}$ 1(fv) $3x - 2y = -6$ 5x - 2y = -10 Writing the equations in matrix form $\begin{bmatrix} 3x & -2y \end{bmatrix} = \begin{bmatrix} -6 \end{bmatrix}$	
5x - 2y = -10	
Writing the equations in matrix form	
$\begin{bmatrix} 3x & -2y \\ 5x & -2y \end{bmatrix} = \begin{bmatrix} -6 \\ 10 \end{bmatrix}$	

$$\begin{bmatrix} 3x & -2y \\ 5x & -2y \end{bmatrix} = \begin{bmatrix} -6 \\ 10 \end{bmatrix} ,$$

Pilot Superone Mathematics 78	Class 9 th	
or $ \begin{bmatrix} 3 & -2 \\ 5 & -2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} * \begin{bmatrix} -6 \\ -10 \end{bmatrix} $		
Let $AX = B$		\wedge
Where $A = \begin{bmatrix} 3 & -2 \\ 5 & -2 \end{bmatrix} X = \begin{bmatrix} x \\ y \end{bmatrix} B = \begin{bmatrix} 6 \\ -t\theta \end{bmatrix}$		\cup
$A = \begin{vmatrix} 3 & -2 \\ 5 & -2 \end{vmatrix}$	0	
=(3)(-2)-(-2)(5))	
= -6 + 10 = 4		
$AX = B$ $X = A^{1}B$		
· · · · · · · · · · · · · · · · · · ·		
$Adj A = \begin{bmatrix} -2 & 2 \\ -5 & 3 \end{bmatrix}$		
[-2 2]	ļ	
$A^{1} = \frac{Adj A}{ A } = \begin{bmatrix} -2 & 2 \\ -5 & 3 \end{bmatrix}$	<u> </u>	
$\begin{bmatrix} -2 & 2 \end{bmatrix}$		
$=\begin{bmatrix} \frac{-2}{3} & \frac{2}{4} \\ -5 & 3 \\ -7 & 4 \end{bmatrix}$		
$X = A^{-1}B$		
$=\begin{bmatrix} 3 & 3 \\ -5 & 3 \\ 7 & 4 \end{bmatrix}$ $X = A^{-1}B$ $=\begin{bmatrix} -\frac{2}{4} & \frac{2}{4} \\ -\frac{5}{4} & \frac{3}{4} \end{bmatrix} \begin{bmatrix} -6 \\ -10 \end{bmatrix}$	ı	
$= \begin{bmatrix} 4 & 4 \\ 5 & 3 \end{bmatrix} \begin{bmatrix} -b \\ -t\theta \end{bmatrix}$		
$X = A^{-1}B$ $= \begin{bmatrix} -\frac{2}{4} & \frac{2}{4} \\ -\frac{5}{4} & \frac{3}{4} \end{bmatrix} \begin{bmatrix} -6 \\ -10 \end{bmatrix}$ $= \begin{bmatrix} -\frac{2}{4}(-6) & +\frac{2}{4}(-6) \\ \frac{5}{4}(-6) & +\frac{3}{4}(-6) \end{bmatrix}$	[رور-	
	/	
$\begin{bmatrix} 3 (-6) + \frac{3}{4}($	10)	
•		

Pilot Superone Mathematics 79 Class 9th

$$\begin{bmatrix} 17 & -20 \\ 4 & -4 \\ 30 & -30 \\ 4 & -4 \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -R \\ -A \\ \theta \end{bmatrix} = \begin{bmatrix} -2 \\ \theta \end{bmatrix}$$

So, x = 2, y = 0

Using Cramer's Rule:

$$3x + 2y = 6$$

$$5x - 2y = -10$$

$$A = \begin{bmatrix} 3 & -2 \\ 5 & -2 \end{bmatrix}$$

$$\mathbf{A}_{\mathrm{T}} = \begin{bmatrix} -6 & 2 \\ 10 & -2 \end{bmatrix}$$

$$A_i = \begin{bmatrix} 3 & -6 \\ 5 & -l\theta \end{bmatrix}$$

$$|A| = \begin{vmatrix} 3 & -2 \\ 5 & -2 \end{vmatrix}$$

$$= (3)(-2) - (5)(-2)$$

= -6 + 10 = 4

$$x = \frac{|A_{3,1}|}{|A_{1}|} = \frac{|-6|-2|}{|10|-2|}$$

$$= \frac{(-6)(-2)(-2)(-10)}{4}$$

$$=\frac{+12-20}{4}-\frac{-8}{4}$$
 - 2

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Pilot Superone Mathematics 80 Class 9th

$$\begin{vmatrix} 3 & -6 \\ 5 & -10 \\ 1 & 1 \end{vmatrix} = \begin{vmatrix} 3 & -6 \\ 5 & -10 \\ 4 \end{vmatrix}$$

$$= \frac{(3)(-10) - (-6)(5)}{4}$$

$$= \frac{-30 + 30}{4} = 0$$

So,
$$x = -2$$
, $y = 0$
 $3x - 2y = 4$
 $-6x + 4y = 7$

Writing the equations in matrix form

$$\begin{bmatrix} 3x & -2y \\ -6x & +4y \end{bmatrix} = \begin{bmatrix} 4 \\ 7 \end{bmatrix}$$
$$\begin{bmatrix} 3 & -2 \\ -6 & 4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 7 \end{bmatrix}$$

where
$$A = \begin{bmatrix} 3 & -2 \\ -6 & 4 \end{bmatrix} X = \begin{bmatrix} x \\ y \end{bmatrix}, B = \begin{bmatrix} 4 \\ 7 \end{bmatrix}$$

$$A : = \begin{bmatrix} 3 & -2 \\ -6 & 4 \end{bmatrix}$$

A is a singular matrix, therefore, solution is not possible

$$4x + y = 9$$
$$-3x - y = 5$$

Writing the equations in matrix form.

$$\begin{bmatrix} 4x & +y \\ -3x & -y \end{bmatrix} = \begin{bmatrix} 9 \\ -5 \end{bmatrix}$$

or
$$\begin{bmatrix} 4 & 1 \\ -3 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 9 \\ -5 \end{bmatrix}$$

Pilot Superone Mathematics 81 Class
$$9^m$$

Let $A \times B$

Where $A = \begin{bmatrix} 4 & I \\ 3 & I \end{bmatrix} \times \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 9 \\ -5 \end{bmatrix}$

$$|A| = \begin{bmatrix} 1 & I \\ -3 & -I \end{bmatrix} = (4)(-1)(-1)(-3)$$

$$= -4 + 3 = -1$$

$$A \times B \times A = A^{-1}B$$

$$A = \begin{bmatrix} -I & -I \\ 3 & I \end{bmatrix}$$

$$A^{-1} = \begin{bmatrix} -I & -I \\ 3 & I \end{bmatrix} = \begin{bmatrix} -I & -I \\ 3 & I \end{bmatrix}$$

$$X = A^{-1}B$$

$$X = A$$

Pilot Superone Mathematics $A = \begin{bmatrix} i & I \\ .3 & -I \end{bmatrix}$ $A_{x} = \begin{bmatrix} 9 & I \\ 5 & -I \end{bmatrix}$ $A_{3} = \begin{bmatrix} 4 & 9 \\ -3 & -5 \end{bmatrix}$ $|A| = \begin{vmatrix} I & I \\ 3 & I \end{vmatrix}$ (4)(-1)-(1)(-3)= -4+3 = -1 $x = \frac{|A_x|}{|A|} = \frac{\begin{vmatrix} 9 & 1 \\ 5 & -1 \end{vmatrix}}{|A|}$ (9)(1) - (1)(-5) win.don's $=\frac{-9+5}{-1}=\frac{4}{-1}=4$ $y = \frac{|A_x|}{|A|} = \frac{|A_y|}{|A|}$

$$= \frac{-20 + 27}{-1} = \frac{7}{1} = -7$$
So, $x = 4$, $y = -7$
 (vii) $(2x - 2y) = -10$

Writing the equations in matrix form.

 $=\frac{(4)(-5)-(9)(-3)}{-1}$

Pilot Superone Mathematics 83	Class 9 ^a
$\begin{bmatrix} 2x & 2y \\ -5y & 2y \end{bmatrix} \begin{bmatrix} 4 \\ 10 \end{bmatrix}$ or $\begin{bmatrix} 2 & 2 \\ 5 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 10 \end{bmatrix}$	0
Let XX H	
Where $A = \begin{bmatrix} 2 & 2 \\ 5 & 2 \end{bmatrix} X = \begin{bmatrix} x \\ 1 \end{bmatrix} B \begin{bmatrix} 3 \\ 10 \end{bmatrix}$	
$ A = \begin{vmatrix} 2 & -3 \\ -5 & -2 \end{vmatrix}$	
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	5)
$\mathbf{X} = \mathbf{A}^{-1}\mathbf{B}$ $\mathbf{Adj} \ \mathbf{A} = \begin{bmatrix} -2 & 2 \\ 5 & 2 \end{bmatrix}$	
$\Lambda^{1} = \frac{\text{Adj } A}{1 \text{ A}} := \begin{bmatrix} -2 & 2 \\ 5 & 2 \end{bmatrix}$	
$A^{T} = \frac{\text{Adj } A}{ A } = \begin{bmatrix} 5 & 2 \\ -IJ & \\ & \\ \end{bmatrix}$ $\begin{bmatrix} -2 & 2 \\ IJ & IJ \\ 5 & 2 \\ -IJ & -IJ \end{bmatrix} = \begin{bmatrix} I \\ 7 \\ 3 \\ \end{bmatrix}$ $X = A^{T}B$	/ -/ -/
$\begin{bmatrix} IA & IA \\ S & 2 \\ -IA & -IA \end{bmatrix} \begin{bmatrix} I \\ S \\ \overline{I} \end{bmatrix}$ $X = A^{T}B$ $= \begin{bmatrix} I & I \\ -I & I \\ -I & I \end{bmatrix} \begin{bmatrix} I \\ -I0 \end{bmatrix}$	

Well-state and the state of the

<u>Pilot</u>	Superone Mathematics		Class 9 th	
		1 2149 +	$-\frac{1}{7}(-10)$	
	=	·	$\frac{7}{1}$	\wedge
		$= \begin{bmatrix} \frac{1}{n}(4) & +\left(-\frac{5}{14}(4) & +\left(-\frac{5}{14$	$-\frac{1}{7}\left[(-10)\right]$	\cup
		$\begin{bmatrix} 4 & 10 \\ 7 & 7 \end{bmatrix}$	$[\underline{n}] \wedge$	
		$= \begin{bmatrix} \frac{4}{7} & +\frac{10}{7} \\ \frac{10}{7} & +\frac{10}{7} \end{bmatrix} =$		•
	$\begin{bmatrix} x \\ y \end{bmatrix}$	$\begin{bmatrix} 2 \\ 0 \end{bmatrix}$		
	So, x 2. y	-0		
	Using Cramer's Rule			
	2x - 2 y			
	5x - 2y =	= - 10		
	0	$=\begin{bmatrix} 2 & -2 \\ -10 & 2 \end{bmatrix}$		
	A. ÷ ≠ A.	$= \begin{bmatrix} 1 & -2 \\ 10 & -2 \end{bmatrix}$		
A	OKA A	$= \begin{bmatrix} 2 & 4 \\ 5 & -10 \end{bmatrix}$		
3	V			
j. arara	. 41	$= \begin{vmatrix} 2 & 2 \\ -5 & -2 \end{vmatrix}$		
317		= (2)(-2)-(-2) (- 5)	
AN .		4 10 = -16		
AN'		+	Z! I	
4 .	x	$\frac{ \mathbf{A}_{\lambda} }{ \mathbf{A} } = \frac{-10}{-1}$, −2 u	
		4(2) - (-2)		

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MATHEMATICS FOR 9TH CLASS (UNIT # 1)

writing the equations in matrix form

$$\begin{bmatrix} 3x & 4y \\ x & +2y \end{bmatrix} = \begin{bmatrix} 4 \\ 8 \end{bmatrix}$$
or
$$\begin{bmatrix} 3 & 4 \\ y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 4 \\ 8 \end{bmatrix}$$
Let
$$AX = B$$

Let AX = B

Where $A = \begin{bmatrix} 3 & 4 \\ 1 & 2 \end{bmatrix} X = \begin{bmatrix} x \\ y \end{bmatrix} B = \begin{bmatrix} 4 \\ 8 \end{bmatrix}$ $|A| = \begin{bmatrix} 2 & -4 \\ 1 & 2 \end{bmatrix} - 3(2) \quad (4)(1)$ 6 + 4 = 10

$$AX = B$$

$$X \cdot A^{-1}B$$

$$Adj A = \begin{bmatrix} 2 & 4 \\ -1 & 3 \end{bmatrix}$$

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Pilot Superone Mathematics 86 Class 9th

 $\frac{Adj}{X} = \begin{bmatrix} 2 & \frac{1}{4} \\ -1 & \frac{3}{3} \\ 10 & 10 \end{bmatrix}$ $\begin{array}{c} \lambda - A B \\ -1 & \frac{3}{10} \end{bmatrix} \begin{bmatrix} 4 \\ 8 \end{bmatrix}$ $= \begin{bmatrix} \frac{2}{10} & 4 \\ -\frac{1}{10} & \frac{3}{10} \end{bmatrix} \begin{bmatrix} 4 \\ 8 \end{bmatrix}$ $= \begin{bmatrix} \frac{2}{10} & 4 \\ -\frac{1}{10} & 4 \end{bmatrix}$ $= \begin{bmatrix} \frac{8}{10} & +\frac{32}{10} \\ -\frac{1}{10} & +\frac{24}{10} \end{bmatrix}$ $= \begin{bmatrix} \frac{8}{10} & +\frac{24}{10} \\ -\frac{1}{10} & +\frac{24}{10} \end{bmatrix}$

$$\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} \frac{10}{10} \\ \frac{10}{20} \\ \frac{1}{10} \end{bmatrix} = \begin{bmatrix} 4 \\ 2 \end{bmatrix}$$

So. x = 4, y = 2Using Cramer's Rule:

$$3x - 4y = 4$$
$$x + 2y = 8$$

Fibrt Superone Mathematics 87 Glass 9th

A
$$\begin{bmatrix} 3 & -1 \\ 1 & 2 \end{bmatrix}$$

A $= \begin{bmatrix} 4 & -4 \\ 2 & 2 \end{bmatrix}$

A $= \begin{bmatrix} 3 & 4 \\ 1 & 8 \end{bmatrix}$

$$|A| = \begin{bmatrix} 3 & 4 \\ 1 & 8 \end{bmatrix}$$

$$|A| = \begin{bmatrix} 4 & -4 \\ 3 & 2 \end{bmatrix}$$

$$x = \frac{|A_x|}{|A|} = \frac{|A_x|}{|10|}$$

$$= \frac{(4)(2) - (-4)(8)}{10}$$

$$= \frac{8 + 32}{10} = \frac{40}{10} - 4$$

$$y = \frac{|A_x|}{|A|} = \frac{|3|}{|4|}$$

$$(3)(8) - (4)(1)$$

$$= \frac{24 - 4}{10} = \frac{20}{10} = 2$$

So.

$$x = 4, y = 2$$

Solve the following word problems by using

- (t) matrix inversion method
- (ii) Cramer's rule
- The length of a rectangle is 4 times its width. The perimeter of the rectangle is 150cm. Find the dimensions of the rectangle.

MATHEMATICS FOR 9TH CLASS (UNIT # 1)

Pilot Superone Mathematics 88 Class 9*

- Iwo sides of a rectangle differ by 3 5cm. Find the dimensions of the rectangle its perimeter is 67cm.
- The third angle of an isosceles triangle is 16° less than
 the sum of the two equal angles. Find three angles of
 the triangle.
- One acute angle of a right triangle is 12° more than twice the other acute angle. Find the acute angles of the right triangle.
- 6. Two ears that are 600 km apart are moving towards each other. Their speeds differ by 6 km per hour and the cars are 123 km apart after 1/2 hours. Find the speed of each car.
- Q.2. The length of a rectangle is 4 times its width. The perimeter of the rectangle is 150 cm. find the dimensions of the rectangle.

Suppose length of rectangle

According to the given conditions

$$4x = y$$

and $2x + 2y = 150$
Thus $4x - y = 0$ (i)
 $2x + 2y = 150$ (ii)

Writing the equations in matrix form.

$$\begin{bmatrix} 4x & y \\ 2x & +2y \end{bmatrix} = \begin{bmatrix} 0 \\ 150 \end{bmatrix}$$
or
$$\begin{bmatrix} 4 & -1 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ 150 \end{bmatrix}$$
Let
$$A X = B$$
Where $A = \begin{bmatrix} 4 & -1 \\ 2 & 2 \end{bmatrix} . X = \begin{bmatrix} x \\ y \end{bmatrix} . B = \begin{bmatrix} 0 \\ 150 \end{bmatrix}$

Pilot Superone Mathematics Class 9° =(4)(2)-(-1)(2)= 8 + 2 = 10 AX -B $X = A^{T}B$ Adj A = $\begin{bmatrix} 2 & I \\ -2 & 4 \end{bmatrix}$ $\mathbf{X} = \mathbf{A}^{\mathsf{T}} \mathbf{R}$ $= \begin{bmatrix} 2 & 1 \\ 10 & 10 \\ 2 & \frac{4}{10} \end{bmatrix} \begin{bmatrix} 0 \\ 150 \end{bmatrix}$ www.dow. $= \begin{bmatrix} \frac{2}{10}(0) & +\frac{1}{10}(150) \\ \frac{2}{10}(0) & +\frac{4}{10}(150) \end{bmatrix}$ $= \begin{bmatrix} 0 & +15 \\ 0 & +60 \end{bmatrix}$

 $\begin{bmatrix} x \\ y \end{bmatrix} - \begin{bmatrix} 15 \\ 60 \end{bmatrix}$ So. $x = 15, y \approx 60$

Thus

width = 15 cm

MATHEMATICS FOR 9TH CLASS (UNIT # 1)

Pilot Superone Mathematics 90 Class 9* Length 6 cm Using Cramer's Rule: 4x > = 0

Ther's Rule:

$$\frac{4x}{4x} = 0$$

$$2x + 2y = 150$$

$$A_x = \begin{bmatrix} \frac{d}{d} & -l \\ 2 & 2 \end{bmatrix}$$

$$A_y = \begin{bmatrix} \frac{d}{d} & -l \\ 2 & 150 \end{bmatrix}$$

$$A_y = \begin{bmatrix} \frac{d}{d} & -l \\ 2 & 2 \end{bmatrix}$$

$$= (4)(2) - (-1)(2)$$

$$= 8 + 2 = 10$$

$$= \frac{|A_x|}{|A|} = \frac{\begin{vmatrix} 0 & -l \\ 150 & 2 \end{vmatrix}}{|I|}$$

$$= \frac{(0)(2) & (-1)(150)}{10}$$

$$= \frac{0 + 150}{10} = \frac{150}{10} = 15$$

$$y = \frac{|A_y|}{|A|} = \frac{\begin{vmatrix} d & 0 \\ 2 & 150 \end{vmatrix}}{|I|}$$

$$\frac{(4)(150) - (0)(2)}{10} = \frac{600}{10} = 60$$

So.
$$x = 15, y = 60$$

Q.3. Two sides of a rectangle differ by 3.5 cm. Find the dimensions of the rectangle if its perimeter is 67 cm.

Suppose:

Pilot Superone Mathematics 91
Length of a rectangle 1, em

Walta of a rectangle vern

According to the conditions

A y 35

and

Writing the equations in matrix form

$$\begin{bmatrix} x \\ 2x + 2x \end{bmatrix} = \begin{bmatrix} 3.5 \\ 6 \end{bmatrix}$$

or $\begin{bmatrix} I & -I \\ 2 & 2 \end{bmatrix} \begin{bmatrix} x \\ 1 \end{bmatrix} = \begin{bmatrix} 3.5 \\ 6 \end{bmatrix}$

Lei

Where
$$A = \begin{bmatrix} 1 & 1 \\ 2 & 2 \end{bmatrix}$$
, $A = \begin{bmatrix} x \\ y \end{bmatrix}$ $B = \begin{bmatrix} 3 & 5 \\ 6 & 7 \end{bmatrix}$

$$A \rightarrow \begin{bmatrix} 1 & -1 \\ 2 & 2 \end{bmatrix}$$

$$-(1)(2)$$
 (1)(2)
 $+2+2=4$

$$X = A^{-1}B$$

$$Adj A = \begin{bmatrix} 2 & t \\ -2 & t \end{bmatrix}$$

$$\frac{Adj}{jA} = \begin{bmatrix} 2 & 1 \\ -2 & 4 \end{bmatrix} = \begin{bmatrix} 2 & 1 \\ 1 & 1 \\ -2 & 1 \end{bmatrix}$$

$$X = A^{-1}B$$

$$= \begin{bmatrix} 2 & 1 \\ 1 & 1 \\ -\frac{2}{3} & \frac{1}{4} \end{bmatrix} \begin{bmatrix} 3.5 \\ 6^{-} \end{bmatrix}$$

Pilot Superone M.	sthematics	92	Class 9 th
		$= \begin{bmatrix} \frac{2}{4}(35) & +\frac{1}{4}(35) & +$	
		$= \begin{bmatrix} \frac{1}{2} & +\frac{1}{2} \\ \frac{1}{2} & +\frac{1}{2} \end{bmatrix}$	Q.
	$\begin{bmatrix} x \\ y \end{bmatrix}$	$\begin{bmatrix} -4 \\ 4 \\ 60 \\ \bar{4} \end{bmatrix} = \begin{bmatrix} 18.5 \\ 15 \end{bmatrix}$	
So		= 18.5	
l'sing Cra	Length	្មៅស ≒ 18.5 cm - 15 cm e:	
_	x y	= 3.5	
	2x + 2y	_	
		$= \begin{bmatrix} I & I \\ 2 & 2 \end{bmatrix}$	
90		$= \begin{bmatrix} 3.5 & -1 \\ 67 & 2 \end{bmatrix}$	
•	Ay	$= \begin{bmatrix} I & 3 & 5 \\ 2 & 6 & 7 \end{bmatrix}$	
•		[I - I]	

 $A_{3} = \begin{bmatrix} I & 3.5 \\ 2 & 67 \end{bmatrix}$ $A_{1} = \begin{vmatrix} I & -I \\ 2 & 2 \end{vmatrix}$ (1)(2) - (-1)(2) = 2 + 2 - 4

Pilot Superone Mathematics

$$x = \frac{A_{x1}}{|A|} = \frac{\begin{vmatrix} 3.5 & -1 \\ 6^7 & 2 \end{vmatrix}}{4}$$

$$= \frac{(3.5)(2) - (-1)(67)}{4} = \frac{7 + 67}{4}$$

$$-\frac{74}{4} = 18.5$$

$$y = \frac{|A_{x}|}{|A|} = \frac{\begin{vmatrix} 1 & 3.5 \\ 2 & 67 \end{vmatrix}}{4}$$

$$= \frac{(1)(67) - (2)(3.5)}{4} = \frac{67 - 7}{4}$$

$$= \frac{60}{4} = 15$$
8.5. $y = 15$

So,
$$x = 18.5$$
, $y = 15$
Length = 18.5 cm
Width 15 cm

Q.4. The third angle of an isosceles is 16" less than the sum of the two equal angles. Find three angles of the triangle.

Solution:-

Suppose measure of each equal angle

Let third angle - v*'

According to the conditions

$$2x - y = 16$$

$$2x + y = 180^{\circ}$$

(sum of the angles)

Writing the equations in matrix form.

$$\begin{bmatrix} 2x - y \\ 2x + y \end{bmatrix} = \begin{bmatrix} 16 \\ 180 \end{bmatrix}$$

MATHEMATICS FOR 9TH CLASS (UNIT # 1)

Pilot Superone Mathematics 94 $\begin{bmatrix} 2 & I \\ 2 & I \end{bmatrix} \begin{bmatrix} x \\ 1 \end{bmatrix} * \begin{bmatrix} 16 \\ 180 \end{bmatrix}$ l.et Where $A = \begin{bmatrix} 2 & -1 \\ 2 & 1 \end{bmatrix} A = \begin{bmatrix} x \\ y \end{bmatrix} B = \begin{bmatrix} 16 \\ 180 \end{bmatrix}$ $|A_1 = \begin{vmatrix} 2 & -1 \\ 2 & 1 \end{vmatrix}$ ±(2)(1) (1)(2) $\approx 2 + 2 = 4$ AX = B $X = A \cdot B$ Adj A $=\begin{bmatrix} t & t \\ -2 & 2 \end{bmatrix}$ $A^{-1} = \frac{Ad_1 A}{|A|} = \frac{\begin{bmatrix} 1 & 1 \\ -2 & 2 \end{bmatrix}}{A}$ winn.dow. $= \begin{bmatrix} 1 & \underline{t} \\ 4 & 4 \\ -2 & 2 \end{bmatrix} \begin{bmatrix} 16 \\ 180 \end{bmatrix}$ $= \begin{bmatrix} \frac{1}{4}(16) & +\frac{1}{4}(180) \\ \frac{2}{4}(16) & +\frac{2}{4}(180) \end{bmatrix}$

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Pilot Superone Mathematics	95	Class 9th
	$\begin{bmatrix} 4+45 \\ 8+90 \end{bmatrix}$	-
	[-X + 90]	
[x]	= [49]	
So, x	= 49°	

y = 82° Measure of each equal angle

49° Measure of third angle R2º

Using Cramer's Rule:

ter's Rule:

$$2x - y = 16$$

$$2x + y = 180$$

$$A = \begin{bmatrix} 2 & 1 \\ 2 & 1 \end{bmatrix}$$

$$A_{\pi} = \begin{bmatrix} 16 & 1 \\ 180 & 1 \end{bmatrix}$$

$$A_{\gamma} = \begin{bmatrix} 2 & 16 \\ 2 & 180 \end{bmatrix}$$

 $|\mathbf{A}| = \begin{vmatrix} 2 & -1 \\ 2 & 1 \end{vmatrix}$ =(2)(1) (-1)(2)=2+2=4 $x = \frac{|A_x|}{|A|} = \frac{\begin{vmatrix} 16 & -1 \\ 180 & 1 \end{vmatrix}}{\begin{vmatrix} 1 & 1 \end{vmatrix}}$ $=\frac{(16)(1)}{4}\frac{(-1)(180)}{4}$ $=\frac{16+180}{4}$

win.dow. $=\frac{196}{4}=49$

Prior Superone Mathematics $y = \frac{A_1}{A_1} = \frac{\begin{vmatrix} 2 & 16 \\ 2 & 180 \end{vmatrix}}{4}$ $\frac{(2)(180) - (16)(2)}{4}$ $=\frac{360-32}{4}=\frac{328}{4}=82$

So,
$$x = 49, y = 82^{\circ}$$

Measure of each equal angle 49°

Measure of third angle

Q.5. One scute angle of a right triangle is 12° more than twice the other acute angle. Find the acute angles of the right triangle.

Solution.-

Let one acute angle $= x^{\circ}$ and the other acute

according to the conditions

$$x + y = 90^{\circ}$$

$$2x = y - 12$$
or
$$2x - y = +12$$
and
$$x + y = 90^{\circ}$$

Writing the equations in matrix form

$$\begin{bmatrix} 2x \cdot y \\ x + y \end{bmatrix} = \begin{bmatrix} 12 \\ 90 \end{bmatrix}$$
or
$$\begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -12 \\ 90 \end{bmatrix}$$
Let
$$A X = B$$
Where $A = \begin{bmatrix} 2 & -1 \\ 1 & 1 \end{bmatrix} X = \begin{bmatrix} x \\ y \end{bmatrix} B = \begin{bmatrix} -12 \\ 90 \end{bmatrix}$

Class 9th <u>Pilot Siperone Mathematics</u> $|A - |_{I=I}^{2-A}$ $=(2)(1) \cdot (-1)(1)$ = 2 + 1 = 3AX = B $X = A^{-1}B$ Adj A $\begin{bmatrix} I & I \\ -I & 2 \end{bmatrix}$ $A^{-1} = \frac{Adj A}{A} = \begin{bmatrix} 1 & 1 \\ -1 & 2 \end{bmatrix}$ Х $= \begin{bmatrix} i & i \\ 3 & 3 \\ -1 & 2 \\ 3 & 3 \end{bmatrix} \begin{bmatrix} 12 \\ 90 \end{bmatrix}$ www.down. $\begin{bmatrix} \frac{1}{3}(-12) & +\frac{1}{3}(90) \\ -\frac{1}{3}(-12) & +\frac{2}{3}(90) \end{bmatrix}$ $\begin{bmatrix} 4+30\\ 4+60 \end{bmatrix}$ $\begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 26 \\ 64 \end{bmatrix}$ r 26. y So One of the acute angle 26"

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Pilot Superone Mathematic 98 (Llass 3°)
Other soute angle 64

Using Cramer's Rule:

$$\begin{array}{ccc}
2s & & & 12 \\
3 & 3 & & 90 \\
A & \begin{bmatrix} 2 & I \\ I & I \end{bmatrix} \\
A & \begin{bmatrix} I^2 & I \\ 90 & I \end{bmatrix} \\
A & \begin{bmatrix} 2 & I2 \\ I & 90 \end{bmatrix}
\end{array}$$

$$|A| = \begin{vmatrix} 2 & -1 \\ 1 & -1 \end{vmatrix} = (2)(1) + (-1)(1)$$

$$= 2 + 1 = 3$$

$$v = \frac{.1}{|A|} = \frac{\begin{vmatrix} -12 & -1 \\ 90 & 1 \end{vmatrix}}{3}$$

$$= \frac{12 + 90}{3} = \frac{78}{3} + 26$$

$$1 = \frac{14.1}{141} = \frac{\begin{bmatrix} 2 & 12 \\ 1 & 90 \end{bmatrix}}{1}$$

$$(2)(\underline{90}) \quad (-12)(\underline{1})$$

Pilot Supering Mathematics 199 190 12

Su a 26.4 64

One acu e angle 26

Other acute angle 64°

Q.6. Two cars that are following apart are moving towards each other. Their speeds differ by 6km per hour and cars are 123km apart after $4\frac{1}{5}$ hours. Find the speed of each ear,

Solution:

Let speed of one car - x km hr Speed of the other car - x km hr

Distance envered by first c.u.m. $4\frac{1}{2}$ hours $-\frac{9}{5}$ i km

Distance covered by the other car in

$$\frac{4}{2} \frac{1}{2} hours = \frac{9}{2} + \lambda m$$

$$\frac{x - y - 6}{2} = \frac{(First condition)}{2^{1 + \frac{9}{2}} x - \frac{500}{2} + \frac{123}{2}} \qquad (Second condition)$$

$$\frac{9}{2} + \frac{9}{2} x - \frac{477}{2}$$

$$x + x + \frac{477}{2} \times \frac{2}{9}$$

and

r 1 6

x + 1 - 106

Writing the equations in matrix, orm

Pilor Superone Mathematics ______100__ A COLUMN (X) (r $\begin{bmatrix} 1 & 1 & x & 106 \\ 1 & 1 & 4 & 6 \end{bmatrix}$ Or Let AX B Where $f = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$ $\lambda = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ $\mathcal{B} = \begin{bmatrix} 106 \\ 16 \end{bmatrix}$ $A_{i} = \begin{bmatrix} 1 & 1 \\ 1 & 4 \end{bmatrix}$ then the obtaining 41.3 AX B

Pilot Superone Mathematics 101

______L<u>us 2"</u>

Seattle Const

 $\lambda = 1/B$

$$\begin{bmatrix} 1 & 1 \\ 2 & 2 \\ 1 & 1 \\ 2 & 2 \end{bmatrix} \begin{bmatrix} 106 \\ 6 \end{bmatrix}$$

$$\begin{bmatrix} 1 & (106) & 1 & (6) \\ 1 & (106) & 1 & 1 \\ 2 & (106) & 1 & 2 & (6) \end{bmatrix}$$

Thus.

speed of the first car 56km br speed of the Other car - 50km hr USIT

$$I = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix}$$

$$t_1 = \begin{bmatrix} 1 & 106 \\ 1 & 6 \end{bmatrix}$$

$$t_1 \begin{vmatrix} 1 & 1 \\ 1 & -1 \end{vmatrix}$$
 (1)(-1) (1)(1)

Written/Composed by <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E-mail <u>raoshahzadiftikhar@cmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 1)

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PINITH.

REAL AND COMPLEX NUMBERS

CN 1

Real Numbers:

Set of Natural Numbers

123 1 Natural Numbers

Set of whole Numbers

d ,a / 2 3 - -

Set of Integers

1 2 10123

Rational Numbers

Q PACKAGEN

Irrational Numbers

 $Q = \{X \mid X \neq \frac{R}{q} \mid p, q \notin Z \mid xq \neq \emptyset\}$

For example $\pi \sqrt{3} = \sqrt{3} = \sqrt{2}$

Real Numbers

The union of Q and Q' is a set of rear numbers

It is denoted by R

 $R = Q \cup Q'$

Remember:

3

(i) きくりょうしき

For each prime number p/\sqrt{q} is an irrational

Square root of all positive non-square integers (iii) are irrational

Types of Rational Numbers (a)

The decimal representation of rational numbers are of two types, terminating and recurring

Pilot Superone Mat nematics 112 Class 9"

(i) Fernmating Decimal Fractions

The decimal fraction in which there are finite number

- The decimal fraction in which there are finite number of digits in its decimal part is called a terminating occumal fraction for example $\frac{4}{3} 9.8$ and $\frac{3}{4} 9.5$
- (ii) Recurring and Non-terminating Decimal Fraction.

 The decimal fraction (non-terminating 1 in which some digits in the same repeated again and again in the same order in its decimal part is called a recurring decimal fraction—or example $\frac{2}{9} = 0.2222$
- (b) Irrational Vumbers:
 Decimal representation for irrational numbers are neither temmating nor repeating in blocks for example $\sqrt{2} = 1.414213562$ wander

Pilot Superone Mathematics 113 Class 9th

Exercise 2.1

Q.1. Identify which of the following are rational and irrational numbers

(i)
$$\sqrt{3}$$
 (ii) $\frac{1}{6}$ (iii) π (iv) $\frac{15}{2}$ (v) 725 (vi) $\sqrt{29}$

Solutions:

$$\frac{1}{6}$$
 $\frac{15}{2}$ 7.25 (Rational)
 $\sqrt{3}$ π , $\sqrt{29}$ (Irrational)

Q.2. Convert the following fractions into decimal fractions.

(v)
$$\frac{17}{25}$$
 (ii) $\frac{19}{4}$ (iii) $\frac{57}{8}$ (v) $\frac{205}{18}$ (v) $\frac{5}{8}$ (vi) $\frac{25}{38}$

Solution:-

2(i)
$$1^7$$
 68
25 25 17.00
0.68 200
200
200
200
200
215
200
200
200
4 4 4 19.00
= 4.75
4, 19.00
16
30
28

Writter/Composed by <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u> , ε-mail <u>raoshshzadifökhar@omail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 2)

Filot Superone Mathematics	114Class 9 ^a
2(iii) 57	* 125
B	8 5 7 000
7 125	56 10
, 120	΄ Ϋ́
	20 76
	40 #0
	x
2(iv) <u>205</u>	H 3898
2(iv) <u>205</u> 18	18 205 0000
11 3889	IK.
11 3007)
-	70 54
	160 144
	160
	111
	16
2(v) 5	625
2(v) 5 8	8 5.000
0.625	48 20
••	16
	40
	10
	x 65 ⁷ 49
2(m) 25	³⁸ 25.00000
38	228
65789	220 190
	300 266
	340
	304
	360 342
	18

Plot Superone Mathematics	115	Class 9™
AT A TRACE A CO.		

- Q.3. Which of the statements are true and which are false?
- (i) $\frac{2}{3}$ is an trational number
- (ii) π is an irrational number
- (iii) $\frac{1}{9}$ is a terminating fraction.
- (iv) $\frac{3}{4}$ is a terminating fraction

Solution:-

- (i) $\frac{2}{3}$ is an irrational number False
- (ii) π is an irrational number True
- (iii) $\frac{I}{g}$ is a terminating fraction False

Explanation:

$$\frac{I}{g} = \theta I$$
 non-terminating.

(iv)
$$\frac{3}{4}$$
 is a terminating fraction True

Explanation:

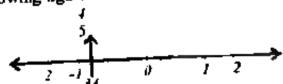
(v)
$$\frac{4}{5}$$
 is a recurring fraction. False

Pilot Superone Mathematics 116 Class 9*

- Q 4. Represent the following numbers on the number line.
 - (a) $\frac{2}{3}$ (ii) $-\frac{4}{5}$ (iii) $t^{\frac{3}{4}}$
 - (iv) $-2\frac{5}{8}$ (v) $2\frac{3}{4}$ (vi) $\sqrt{5}$
- 4(1) To represent the rational number $\frac{2}{3}$ divide unit length between 0 and 1 anto 3 equal parts
- (a) Take 2 parts on right of 0
- (iii) Point M represents $\frac{2}{3}$ on the number line in the following figure.



- 4(ii) Represent -5 on the number line.
- (i) To represent the rational number $-\frac{4}{5}$ divide um, length between 0 and I into 5 equal parts
- (ii) Take 4 parts on left of '0'
- (iii) Point M represents $\frac{4}{5}$ on the number line in the following figure

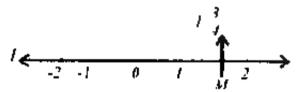


Pilo, Saperone Mathematics 117 Class 9th

4(iii) Represent I_{J}^{J} on the number line

Solution:-

 $I\frac{3}{4} + I + \frac{3}{4}$ therefore $I\frac{3}{4}$ has between I and 2 on the number line.



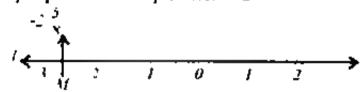
The distance between I and 2 is divided into four equal parts. From I, we take 3 parts

Point M represent I_I^3 on the number line.

4(iv) Represent $-2\frac{5}{8}$ on the number leve

Rationa, number $-2\frac{5}{8}$ has between - 2 and -3

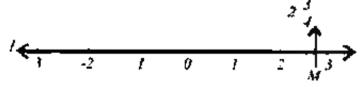
We divide the distance between 2 and 3 into eight equal part and take 5 parts from 2



4(v) Represent $2\frac{3}{4}$ on the number line.

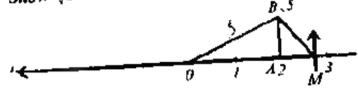
Number $2\frac{3}{4}$ hes between 2 and 3. Divided the distance

between 2 and 3 into 4 equal parts. Take 3 parts from 2



Prior Superone Mathematics 118 Class 9^m Point 1/ shows $2\frac{3}{4}$ on the number line in the above figure

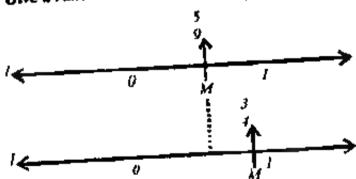
4(vi) Show \5 on the number line.



- (c) Construct a $\triangle OAB$ which $m \overline{OA} = 2$ units and 1 BA + 1
- (ii) Take 0 us centre and draw an arc of radius OB it cuts the number line at $M = \sqrt{5}$. $(m OB)^2 = (mOA)^2 + (mAB)^2$ (Pythagorean Theorem) $(m OB)^2 = 4 + 1 = 5$ $m OB = \sqrt{5}$

Thus m $\overline{OB} = m\overline{OM} = \sqrt{5}$

Q.5. Give a rational number between $\frac{3}{4}$ and $\frac{5}{9}$



(i) on line l a number $\frac{5}{9}$ has been shown between θ and l by M.

Pilot Superone Mathematics 119 Class 9th

(ii) on line l a number $\frac{3}{4}$ has been shown between θ and l by M (the same interval)

Result

There are a number of rational numbers between $\frac{5}{9}$ and $\frac{3}{4}$ For example $\frac{57}{100}$ $\frac{58}{100}$ $\frac{59}{100}$, $\frac{60}{100}$ $\frac{74}{100}$ etc.

- Q.6. Express the following recurring decimals as the rational number $\frac{\rho}{q}$ where ρ , q are integers and $q \neq 0$.
- (i) 0.5 (ii) 0.13 (iii) 0.57 Solution:-
- 6(i) 0 5

Let x = 0.5That x = 0.5555

Only one digit 5 is being repeated, we multiply by 10 on both sides.

x = 0.5555 (1) and $10x = (0.5555) \times 10$ That x = 5.5555 (2)

That * 5 5555 (11)

Subtracting (i) from (ii)

 $g_{X} = 5$ $x = \frac{5}{4}$

6(ii) 0 <u>13</u>

Let $x = 0.\overline{13}$ That x = 0.13131313

Here, a block of 13 is being repeated, we multiply both sides by 100.

<u> Class 9* </u> Pilot Superone Mathematics 120 $x = 0 \overline{B} \overline{B} \overline{B} \overline{B}$, $\overline{B} = .60$ 160x 13 13 13, 13, 13 ...(n) Subtracting (4, from (11) 100x - x = 1399x = 13x 13 Thus. $0.1\vec{3} + \frac{13}{99}$ 6(id) 0 67 $x = 0 \overline{67}$ l.et x = 0.67676767Here, a block of 67 is being repeated, we multiply both OF sides by 100. U 67676767 ... (i) 100x + 67 67676767 (10) Subtracting (i) from (u) 100x - x = 6799x - 67 Thus $0\overline{67} = \frac{67}{99}$ Proporties of Real Numbers Properties of real numbers w.r.t. addition. (a)

- (f) Closure Property $a + b \in R, \forall a, b \in R$
- (ii) Commutative Property $a+b+b+a, \forall a, b \in R$
- (III) Associative Property $(a + b) + c + a + (b + c), \forall a, b, c \in R$

Class 9* Pilot Superone Mathematics 121 Additive identity (iv) $a \cdot a \cdot a = 0 \cdot a \quad \forall a \in R$ (Gesephed addinive identity) Addunc laverse (v) a (-a) 0 (-a) · a Properties of real numbers under multiplication Clasure Property O. abe R TR b E R Commutative Property (ii) ab borabeR Associative Property (iii) (abuc a/bc) va.b.c e R Multiplicative Identity (iv) u el a = 1 xa Ya e R Multiplicative Inverse (v) $a \times \frac{1}{a} = 1 - \frac{1}{a} \times a \quad \forall a \in R \text{ and } a \neq 0$ Multiplication is distributive over addition and (vi) SECTION. Va b c e R (Left distributive law) alb+c) ab+ac (Right distributive law) la - bie ac · bc Properties of Equality of Real Numbers Reflexive property (i) a ava+R Symmetric Property (ii) If a - without a VabeR Transitive Property (iii) If a = b and b = c, then a = c, $\forall a, b, c \in R$ Cancellation Property for Addition (iv) If a = c, then a + c = b + c, $\forall a, b, c \in R$ Multiplicative Property (7) If a > b, then ac = bc, $\forall a, b, c \in R$ Cancellation Property for Addition (vi) If a + b = b + c, then a = b. $\forall a, b, c \in R$ (ancellation Property for Multiplication (vii)

Pilot S	uperone Mathematics 122	Class 9*
	Il ac bc c≠0 then a b. Va.b. c €	r R
(c)	Properties of Inequalities of Real Na	mbers
1.2	Properties of inequalities of real	numbers are a
	follows	
(i)	Trichotomy Property	
	V abck	
	a < b or a bor	a > 0
(a)	Transitive Property	
	V a, b, c ∈ R	
	(a) $a < h$ and $h < v \Rightarrow a < c$	
	(b) $a > b$ and $b = c \Rightarrow a > c$	
(iii)	Additive Property	
	∀ a.b.c ∈ R	and
	(M) 4 10 m 4 1 2 3 1	and
	$a < b \Rightarrow c \cdot a < c + b$	
	(b) $a > b \Rightarrow a + c > b + c$	
	$a > b \Rightarrow c + a > c + b$	
(iv)	Multiplicative Property	
	(a) $\forall a, b, c \in R \text{ and } c > 0$	d
	(1) (1) - 1 - 11	and .
	$a > b \rightarrow ca > cb$	and
	(myst o com oc	and
	$a < b \Rightarrow ca < cb$	
	$(b) \forall a, b, c \in R \text{ and } c < 0$	
	(i) $a > b > ac < bc$	and
	$a > b \Rightarrow ca < cb$	
	(ii)a · b → ac > bc	and
	$a < b \rightarrow ca > cb$	
(v)	Multiplicative Inverse Property	
	$\forall a,b \in \mathbb{R} \text{ and } a \neq 0, b \neq 0$	
	(a) $a < b \Leftrightarrow \frac{1}{a} > \frac{1}{b}$	
	(b) $a > b \Leftrightarrow \frac{l}{a} < \frac{l}{b}$	
	u (/	

Pilot Superone Mathematics 123 Class 9th Exercise 2.2 0.1. Identity the property used in the following. (i) $a \cdot b \quad b + a$ (ii) (abje = a(be) (iii) $7 \times 1 = 7$ (iv) x > y or x = y or x < y(v) ab = ba. (vi) $a \cdot c + b + c \Rightarrow a - b$ (vil) 5+(-5)=0 ... (viii) $7 \times \frac{1}{7} = 1$. (ix) $a > b \Rightarrow ac > bc (c > 0)$ Solution .a+b=b+a ... W. (Commutative wit taddition) (ab)c = a(bc). (Associative w r t multiplication)av – (Multiplicative wirl Identity) (id) 7×1 7 (iv) x > y or x = y or x < y. (Tuchotomy) ı (v) $ab = ba... \searrow ...$ (Commutative w.r t Multiplication) (vi) $a+\mathbf{E}=b+c\Rightarrow a=b$ (Cancellation property of addition) (vii) 5+(-5)=0... (Additive inverse) (viii) $7 \times \frac{1}{7} = 1$ (Multiplicative inverse) (ix) $a > b \Rightarrow ac > bc (c > 0) \dots$ (Multiplicative property) Q.2. Fill in the following blanks by stating the properties of real numbers used. 3x + 3(y + x)=3x+3y+3x. $=3x-3x+3y, \qquad \dots$ (ii) -0+3v(in) = 3₃,

Class 9" Prior Superone Mathematics

$$\frac{2(0)}{3x+3(y-x)} = \frac{3x+3y-3x}{3x+3y-3x}$$

Distributive property of multiplication over subtraction.

(ii)
$$3x + 3y - 3x$$

= $3x + 3y$ (Commutative)

(iii)
$$3x - 3x + 3y$$

= $0 + 3y$ (Addition Inverse)

(iv)
$$0 + 3y$$

- 3y (Addition Identity)

Q.3. Give the name of property used in the following.

(i)
$$\sqrt{24} + 0 - \sqrt{24}$$

(ii) $\frac{2}{3} \left(5 + \frac{7}{2} \right) \left(-\frac{2}{3} \right) (5) + \left(-\frac{27}{3} \right) \left(\frac{2}{3} \right)$

(ii)
$$\frac{1}{3}(5+\frac{1}{2})(-\frac{1}{3})(5)(-\frac{1}{3})(\frac{1}{3})$$

(iii)
$$\pi + (-\pi) = 0$$
 ...

(iv)
$$\sqrt{3} \sqrt{3}$$
 ...
(v) $\left(-\frac{8}{8}\right)\left(-\frac{8}{5}\right) = 1$...

Solution:-

(b)
$$\sqrt{24} + 0 = \sqrt{24}$$
 . (Additive [dentity]

(ii)
$$-\frac{2}{3}\left(5+\frac{7}{2}\right)=\left(-\frac{2}{3}\right)(5)+\left(-\frac{2}{3}\right)\left(\frac{7}{2}\right)$$

Distribut ve property of multiplication over addition

(iii)
$$\pi + (-\pi) = 0$$
 .. (Additive Inverse,

(c)
$$\sqrt{3}$$
 is a real number (Closure property w.r.t multiplication)

(v)
$$\left(\frac{5}{8}\right)\left(-\frac{8}{5}\right) = 1$$

(Multiplication Inverse)

Concept of Radicals and Radicands

If n is positive integer greater than 1 and a is a real number, then any real number x such that x" = a is called the nth root of a, and in symbols is written as

Pilot Superone Mathematics 125 Class 9*

 $x = \sqrt[n]{a}$ or $x = (a)^{l \cdot n}$

In the radical $\sqrt[3]{a}$, the symbol $\sqrt{}$ is called the radical sign, n is called the index of the radical and the real number a under the radical sign is called the radicand or base

Note

 $\sqrt[3]{a}$ is usually written as \sqrt{a}

Properties of Radicals

Let $a, b \in R$ and $m \mid n$ be positive integers. Then,

2

(ii) $\sqrt[a]{\frac{a}{b}} = \sqrt[b]{a} \qquad .$

(ái) √¶a = °¶a

(iv) $\sqrt[n]{a^m} = (\sqrt[n]{a})^m$

(y) $\sqrt[n]{a^n}$ a

downloa.

Pilot Superone Mathematics 126

Exercise 2.3

- Write each redical expression in exponential notation 1. and each exponential expression in radical notation. Do not simplify:
 - (i) ¥-64
- (ii)
- (iti) 7¹⁻³
- (iv) v 23
- (i) $\sqrt[3]{-64} = (-64)^{1/3}$ (Exponential form)

- (ii) $2^{3/5} = \sqrt[5]{2^3}$ (Radica) form)
- (iii) $7^{1/3} = -\sqrt[3]{7}$ (Radical form)
- (iv) $y^{-2-3} = \sqrt[3]{y^{-2}}$ (Radical form)
- Q.2. Tell whether the following statements are true or false?
 - (i) $5^{7.5} = \sqrt{5}$ (u) $2^{2.3} = \sqrt{4}$

 - (iii) $\sqrt{49} = \sqrt{7}$ (iv) $\sqrt[3]{x^{27}} = x^3$

Solutions:-

 $2(i) \quad 5^{1/4} = \sqrt{5}$

(False)

513-15

Explanation

2(ii) 2²⁻³ · 3/4

(True)

$$2^{2/3}$$
 $\sqrt[3]{2^2} = \sqrt[3]{4}$

Explanation

$$2(iii) \quad \sqrt{49} = \sqrt{7}$$

(False)

$$\sqrt{49}$$
 7

Explanation

$$2(iv) \quad \sqrt[3]{x^{2^{7}}} = x^{3}$$

(False)

$$\sqrt[4]{x^{27}} - (x^{27})^{1/3}$$

Explanation

Pilot Superone Mathematics 127 Class 9th

Q.3 Simplify the following radical expressions.

(iv)
$$\sqrt[3]{-\frac{\frac{3}{27}}{27}}$$

Solutions:

3(i)
$$\sqrt{125}$$

= $\sqrt{(-5)^3} = [(-5)^3]^{1/3}$
= $(-5)^{1\times 1/3}$

3(u)
$$\sqrt{32}$$

$$= \sqrt[4]{2^5} - \sqrt[4]{2^4 \times 2}$$

$$= 2^{4 \times 2} + 2^{4 \times 4}$$

$$= 2^{4 \times 4} \times 2^{4 \times 4}$$

$$= 2 \sqrt[4]{2}$$

$$\sqrt[3]{\frac{3}{32}} = \left(\frac{3}{2^5}\right)^{1/5}$$

$$\sqrt[3]{3}$$

$$3609 \quad \sqrt[4]{-\frac{8}{27}}$$

$$= \sqrt{\left(-\frac{2}{3}\right)^3} \quad \left[\left(-\frac{2}{3}\right)^3\right]^{3}$$

Prior Superone Mathematics 128 Class 9^{th} $\left(-\frac{2}{3}\right)^{3cl-3} = \frac{2}{3}$

Base and Exponent

In the exponential notation of tread as a to the nth power) we call 'a' as the base and 'w' exponent or the power to which the base is raised.

Laws of Exponents

If $a, b \in R$ and m, n are positive integers then

$$(a^{m})^{n} = a^{nat}, (ab)^{n} = a^{n}b^{n}$$

$$\left(\frac{a}{b}\right)^{n} = \frac{d^{n}}{b^{n}}, (ab)^{n} = a^{n}b^{n}$$

$$a^{m}a^{n} = a^{m}, (ab)^{n} = a^{n}b^{n}$$

$$a^{m}a^{n} = a^{m}a^{n}, (ab)^{n} = a^{n}b^{n}$$



<u>Pilot Superone Mathematics 129</u> Class 9th

Exercise 2.4

Q.1. Use laws of exponents to simplify.

(i)
$$\frac{(243)^{-2/3}(32)^{-1/3}}{\sqrt{(196)^{-1}}}$$
 (ii)
$$(2x^{5}y^{-1})(-8x^{-1}y^{2})$$
 (iii)
$$\left(\frac{x^{-2}y^{-1}z^{-1}}{x^{4}y^{-1}z^{6}}\right)^{-3}$$
 (iv)
$$\frac{(81)^{n}3^{5}(3)^{4n-1}(243)}{(9^{2n})(3^{3})}$$

Solution:-

í

$$I(i) = \frac{(243)^{2/3}(32)^{-1.5}}{\sqrt{(196)^3}}$$

$$\frac{(3^5)^{2/3}(2^5, 15)}{[(14^7)^3]^{1/2}}$$

$$\frac{3^{3(-2/5)}(2^{3(-1/5)})}{14^{2/3}(1)^{1/2}}$$

$$= \frac{7}{14^{1/3}} = \frac{3^{10/3}(2^{-1/5})}{2^{1/3}(2^{-1/5})}$$

$$= \frac{7}{3^{10/3}} = \frac{7}{3^{10/3}}$$

$$= \frac{7}{3^{3/3}} = \frac{7}{3^{3/3}}$$

$$= \frac{7}{3^{3/3}} = \frac{7}{3^{3/3}}$$

$$= \frac{7}{3^3 \sqrt[3]{3^3}} = \frac{3^{3/3}}{3^3}$$

$$= \frac{7}{3^3 \sqrt[3]{3^3}} = \frac{3^{3/3}}{3^3} = \frac{3^{3/3}}{3^3}$$

$$= \frac{7}{3^3 \sqrt[3]{3^3}} = \frac{3^{3/3}}{3^3} = \frac{3^{3/3}}{3^3}$$

$$= \frac{7}{3^3 \sqrt[3]{3^3}} = \frac{3^{3/3}}{3^3} = \frac{3^{3/3}}$$

Phot Superone Mathematics 130 Class
$$9^{th}$$

$$= \left(\frac{y^{2+3}}{x^{2+2}}\right)^{-3}$$

$$= \left(\frac{y^{2}}{x^{2+2}}\right)^{-3}$$

$$= \frac{y^{3-1}}{x^{3-1}} = \frac{y^{3-1}}{x^{3-2}} = \frac{x^{13}z^{12}}{y^{3}}$$

$$= \frac{(81f^{2} \cdot 3^{3} - (3)^{3n-1} \cdot (243)}{(9^{3n})(3^{3})}$$

$$= \frac{(3^{4}f^{2} \cdot 3^{3} - 3^{4n-1} \cdot (3)^{3}}{(3^{4} \cdot x^{3})^{3}}$$

$$= \frac{3^{4n+3}}{3^{4n+3}} = \frac{3^{4n+4} \cdot 3^{4} - 3^{4n+4}}{3^{4n+3}}$$

$$= \frac{3^{4n+6} \cdot (3 \cdot 1)}{3^{4n+3}} = 3^{4n+4-4n-3} \times (2)$$

$$= 3 \times 2^{3-5} \cdot 6$$
Q.2. Show that:
$$\left(\frac{x^{3}}{x^{3}}\right)^{3+2} \times \left(\frac{x^{3}}{x^{4}}\right)^{3+2} \times \left(\frac{x^{4}}{x^{4}}\right)^{n+4} = 1$$

$$I.H.S = \left(\frac{x^{2}}{x^{3}}\right)^{3+3} \times \left(\frac{x^{3}}{x^{4}}\right)^{3+2} \times \left(\frac{x^{4}}{x^{4}}\right)^{n+4}$$

$$= (x^{2} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= (x^{2} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{2} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{3} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+2} \times (x^{3} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot b^{3})^{3+3} \times (x^{3} \cdot a^{3})^{n+4}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a^{3})^{3+3}$$

$$= x^{10} \cdot b^{3+3} \times (x^{3} \cdot a^{3})^{3+3} \times (x^{3} \cdot a$$

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Pilot Superone Mathematics Class 9* $\frac{2^{1/2}.(27)^{1/2}(60)^{1/2}}{(180)^{1/2}(4)^{-1/3}(9)^{1/4}}$ 3(i) $\frac{2^{1/3} \cdot (3^3)^{1/3} \cdot (2^2 \cdot 3 \cdot 5)^{1/2}}{(2^2 \cdot 3^2 \cdot 5)^{1/2} \cdot (2^2)^{-1/3} \cdot (3^2)^{1/4}}$ $=\frac{2^{1/3} 3^{3\times1/3} 2^{2\times1/2} 3^{1/2} 5^{1/2}}{2^{2\times1/2} 3^{2\times1/2} 5^{1/2} 2^{2(-1/3)} 3^{2\times1/2}}$ $=\frac{2^{1/3}}{2}\frac{3}{3}\frac{3}{5}\frac{2}{10}\frac{3^{1/2}}{2^{-2/3}}\frac{5^{1/2}}{3^{1/2}}=2^{1/3}+2/3$ 1+2 3 = 2 3 = 23 = 21 = 2 3(ii) $-\frac{5^8}{5^9} - 5^{8-6} = 5^2 = 25$ 3(iv) $(x^3)^2 \div x^{3^2} x \neq 0$ = $x^{3(2)} + x^3$

Pilot Superone Mathematics 132 Class 9^{th} $x^{0} \div x^{9} = \frac{x^{0}}{x^{9}} - \frac{1}{x^{9-6}} = \frac{1}{x^{3}}$

Complex Numbers

A number $\sqrt{-I}$ has been found that square of it is "-1" It is called the imaginary unit. It is denoted by a (101a) that I' = -I It is not a real number. The swiss mathematician Leonard Fuler (1707 - 1783) was the first to use the symbol I for the number $\sqrt{-I}$

Numbers like $\sqrt{-1}$, $\sqrt{-3}$, $\sqrt{-4}$ etc are called imaginary numbers.

Definition of a Complex Numbers

A number of the form z = a + bi where a and b are real numbers and $v = \sqrt{-1}$ is called a complex number

Set of Complex Numbers

Set of complex numbers is denoted by C

 $C = \{-\{z = a + bi, \text{ where } a, b \in R \text{ and } i \in I\}$

The number 'a is real part and b is imaginary part of the complex number a + bi

These are denoted as a Re (z) and b Im (z)

Conjugate of a Complex Number

Conjugate of a + bisa bi, then a + bi and

 $\frac{1}{2}$ a bi

Now $\overline{z} = a + bt$ i.e., conjugate of a original complex number

Equality of Complex Numbers

 $\forall a. b. c. d \in R$

If a + h = c + dt then a = c and h = d

Properties of Complex Numbers

(i) $z_1 - z_2$ (Reflexive Law)

(ii) $z_1 = z_2 \Rightarrow z_2 = z_1$. (Symmetric I aw

(iii) $z_1 + z_2, z_2 = z_3 \rightarrow z_1 = z_2$. (Transitive Law)

Prior Superone Mathematics Exercise 2.5 0.1. Evaluate: (i) t^2 (ii) t^{50} (iii) t^{12} (iv) $(-1)^3$ (v) $(-1)^5$ (vi) t^{27} 1(1) $(-1)^{1}$ i = -11(ii) $_{1}^{2}(-I)^{23} = (-1)^{24}(-I) = -I$ 1(14) = 62/6 = (-1)4 = 1 $I(iv) = (-i)^{\delta}$ $= [(-1)^2]^d = (-1)^d = 1$ $I(v) = (-1)^3$

- (-) × (i) $\mathcal{F}_{\mathbf{s}}^{\mathbf{s}'} \times (-i) = (i^2)^2 \times (-i)$ $=(-1)^t \times (-1)=-1$ I(vi) 1²⁷ $= (i^2)^{13} \times 1$

 $=(-1)^{B}xi-i$

Pilot Superone Mathematics 134 Class 9th ___ Write the conjugate of the following numbers. 0.2. (i) 2 + 31 (ii) 3 - 51 (iii) i (iv) 3 + 4i(v) - 4i(vi) = 3Solution:z(i) = z = 2 + 3i $\tilde{z} = 2 - 3i$ 2(ii) z = 3 - 5i $\hat{x} = 3 + 5i$ $2(ui) \quad z = -i$ $\hat{z} = i$ 2(vi) z = -3 + 4c $\overline{z} = -3$ 4i $2(v) \quad z = -4 - t$ 2 = · 4 +1 2(vi) z = 1 - 3 $\bar{z} = -i - \bar{z}$ Q.3. Write the real and imaginary part of the following numbers.

(i)
$$l+i$$
 (ii) $-l+2i$ (iii) $3i+2$

(iv)
$$2 - 2i - (v) = -3i$$
 (vi) $2 + 0i$

Solutions:-

Class 9th Pilot Superone Mathematics $Re(z) = I \quad Im(z) = I$ $z \neq -1 + 2i$ 3(ii) Re(z) = 1 Int(z) = 2z = 3i + 23(iii) $Re(z) = 2 \ln(z) = -3$ z - 2 2i 3(iv) $Re(z) = 2 \cdot hn(z) - 2$ z = -3i3(0) $Re(z) = 0 \cdot Im(z) = -3$ z 2 + 01 3(vi) Re(z) = 2. lm(z) = 0Q.4. Find the value of x and y if x + iy + 1 = 4 - 3iHere 19 =- 31 y = -3and $x + 1 \cdot 4$ x 4 1

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Phlot Superone Mathematics 136

Exercise 2.6

0.1. Identify the following statements as true or false.

(i)
$$\sqrt{-3}\sqrt{-3}$$
 3 (ii) $i^{23} = i$

(iii)

Complex conjugate of $(-6i + i^2)$ is (-1 + 6i)(lv)

Difference of a complex number z = a + bi and (v) its conjugate is a real number

If (a + 1) - (b + 3)i = 5 + 8i, then a = 6 and b = -11. (vi)

Product of a complex number and its conjugate (vii) is always a non-negative real number

Solutions:-

1(i)
$$\sqrt{3}\sqrt{3} = 3$$

False

 $\sqrt{3}i \times \sqrt{3}i$ $\sqrt{3}\sqrt{3}$ ℓ^2

Explanation

$$I(ii) \quad i^I = -i$$

False

· 1022 x1

Explanation

 $I(H) = i^{(a)} + -1$

True

 $= (-1)^3 = 1$

Explanation

I(iv) Complex Conjugate of $(-6i + i^2)$ is (-1 + 6i)

True

$$6i + i^2$$

Explanation

$$-6i \quad I = -1 \quad 6i$$

Difference of a complex number z = a + bi and its 1(v) conjugate is a real number False

Pilot Superone Mathematics 137 Class 9th

z - a + bi

Explanation

and

$$z = a - bi$$

$$z - \overline{z} = (a + bi) - (a - bi)$$

$$= a + bi - a + bi$$

$$= 2bi - (an imaginary number)$$

$$I(vi)$$
 If $(a - 1) (b + 3i) = 5 + 8i$

Solution:-

(a 1)
$$(b+3i)$$
 5 · 8;
a 1 b 3; = 5 + 8;
a b = 5 + 8; + 1 + 3;
a b = 6 + 1;
a 6

and

I(vit) Product of a complex number and its conjugate is always a real non-negative real number

Example:

$$(2 - 3i) (2 - 3i)$$
= 2(2 + 3i) + 3i(2 + 3i)
= 4 + 6i - 6i - 9i²
= 4 - 9i²
= 4 - 9(-1) - 4 + 9 = 13

It is a non-negative real number (True)

Q.2. Express each complex number in the standard form a + bi, where a and b are real numbers.

(i)
$$(2+3y+(7-2i)$$

(ii)
$$2(5+4i)-3(7+4i)$$

(iii)
$$(-3+5i, -(4+9i)$$

$$(iv) 2i^2 + 6i^3 + 3i^{16} - 6i^{19} + 4i^{23}$$

Solution:-

$$2(i) (2+3i) + (7-2i) = 2+3i+7-2i$$

Class 9" Pilot Superone Mathematics 138 - 2 + 7 + 31 21 = 9 + 1 2(iii) - (3 + 5i, -(4 + 9i)3 51 4 91 3 4 - 5i 9i = -1 14t $2(iv) = 2i + 6i^3 + 3i^{16} - 6i^{19} + 4i^{25}$ 2i2 + 6i3 + 3i16 - 6i19 + 4i25 $=2(-1)+6i^{2}i+3(i^{2})^{8}-6(i^{2})^{9}i+4(i^{2})^{12}i$ $= -2 + 6(-1)i + 3(-1)^0 - 6(-1)^0 I + 4(-1)^{12}I$ = -2 - 6i + 3(1) + 6(-1)i + 4(1)i2 61 + 3 + 61 + 41 -2+3 6i+6i+4i 1 + 41 Q.3. Simplify and write your answer in the form a + bi. (i) (-7 + 3i)(-3 + 2i)(a) (2-\(\sqrt{4}\)(3\\sqrt{-4}) (iii) (\sqrt{5} - 3i)* (h) $(2-3i)(\overline{3-2i})$ Solumen 3(i) (7+3i) (3+2i) (-7)(-3+2i)+3i(-3+2i)21 141 91 + 612

$$21 \quad 14i \quad 9i + 6i^{2}$$

$$21 \quad 14i \quad 9i + 6(-1)$$

$$21 \quad 23i \quad 6 \quad 15 \quad 23i$$

$$3(ii) \quad (2 \quad \sqrt{-4}) \quad (3 - \sqrt{-4})$$

$$(2 \quad 2i) \quad (3 \quad 2i)$$

$$2(3 \quad 2i) \quad 2i/3 \quad 2i)$$

$$6 \quad 4i \quad 6i + 4i^{2}$$

$$6 \quad 10i + 4(-1)$$

$$6 \quad 10i \quad 4 \quad 2 \quad 10i$$

$$3(iii) \quad (\sqrt{5} \quad 3i)^{2}$$

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$$(\sqrt{5})^2 + (3))^2 = 2\sqrt{5} \times 3i$$

$$= 5 + 9i^3 - 6\sqrt{5}i$$

$$= 5 + 9(-1) - 6\sqrt{5}i$$

Pilot Superone Mathematics 139

$$= 5 - 9 - 6\sqrt{5}i$$

$$= 4 6\sqrt{5}i$$

3(iv)
$$(2-3i)(\sqrt{3-2i})$$

= $(2-3i)(3+2i)$ (Taking conjugate)
= $2(3+2i)-3i(3+2i)$
= $6+4i-9i-6i^2$
= $6+4i-9i-6(-1)$
= $6+4i-9i+6$
= $12-5!$

Q.4. Simplify and write your enswer in the form a + bi.

$$Q = \frac{2}{1+i}$$

$$(11) \qquad \frac{2+3i}{4-i}$$

(iv)
$$\frac{2-6i}{3+i} = \frac{4+i}{3+i}$$

(a)
$$\left(\frac{l+l}{l-l}\right)^2$$

(vi)
$$\frac{1}{(2+3i)(1-i)}$$

Solution:-

4(i)
$$\frac{-2}{1+i} \times \frac{1-i}{1-i}$$

$$\frac{-2(1-i)}{1-i^2} - \frac{-2+2i}{1-(-1)}$$

$$\frac{-2+2i}{1+1} = \frac{-2+2i}{2}$$

$$= -1+1i = -1+i$$
4(ii)
$$\frac{2+3i}{1+1} = \frac{-2+2i}{2}$$

Vicitary on the Complete Compl

Class 9th Pilot Superone Mathematics. $=\frac{2+3i}{4}\times\frac{4+i}{4+i}$ $=\frac{(2+3i)(4+4)}{4^2+2}$ $\frac{2(4+6+3)(4+6)}{16-(-1)}$ $= \frac{8 + 2i + 12i + 3i^2}{16 + 1}$ $\frac{8+14+3(-1)}{17}$ $=\frac{8+143-3}{12}$ $-\frac{5+14i}{17} = \frac{5}{17} + \frac{14}{17}4$ $4(ini) \quad \frac{9-7i}{3+i}$ $\frac{9-7i}{3+1} \times \frac{3-7i}{3}$ $= \frac{(9-74) \times (3-i)}{3^{3}-i^{2}}$ $= \frac{73-i)-7i(3-i)}{9-(-1)}$ $= \frac{27-30i+7(-1)}{10} = \frac{20-30i}{10} = 2-3i$ 4(iv) $\frac{2-6i}{3+i} - \frac{4+i}{3+i}$ $= \left(\frac{2-6!}{3+1} \times \frac{3-1}{3+i}\right) \left(\frac{4+1}{3+i} \times \frac{3-1}{3-1}\right)$ $-\left(\frac{2(3-i)-6l(3-i)}{3^2-i^2}\right)-\left(\frac{4(3-i)+i(3-i)}{3^2-i^2}\right)$

............

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$$\frac{6 - 2i - 18i + 6i^{2}}{9 - (-1)} = \frac{12 - 4i + 3i - i^{2}}{9 - (-1)}$$

$$\frac{6 - 20i + 6(-1)}{10} = \frac{12 - i - (-1)}{10}$$

$$\frac{6 - 20i - 6}{10} = \frac{12 - i + 1}{10}$$

$$\frac{- 20i}{10} = \frac{13}{10} = \frac{-20i - 13 + 1}{10}$$

$$\frac{-13 - 19i}{10} = \frac{-13}{10} - \frac{19}{10}i$$

$$4(v) = \left[\frac{1 + i}{1 - i} \times \frac{1 + i}{1 + i}\right]^{2}$$

$$= \left[\frac{(1 + i)^{2}}{1 - i^{2}}\right]^{2} - \left[\frac{(1 + 2i + i)^{2}}{1 - (-1)}\right]^{2}$$

$$- \left[\frac{(2 + 3i)(1 - i)}{2}\right]$$

$$\frac{2i}{2}\right]^{2} = \sqrt[3]{4 - i}$$

$$\frac{1}{(2 - 3i)} (2 - 3i) \times \frac{(1 + i)}{(1 - i)(1 + i)}$$

$$\frac{2}{(4 - 9i)} (1 - i) = \frac{1}{(4 - 9i)(1 + i)}$$

$$\frac{2 + 2i - 3i - 3i^{2}}{(4 + 9i)(1 + 1)} = \frac{1}{(13)(2)}$$

$$\frac{2 + 3i}{26} = \frac{5 - i}{26} = \frac{5}{10} = \frac{16}{16}i$$

With the state of the state of

Prior Superone Mathematics 142 Class 9th

Q.5. Calculate (a) \bar{z} (b) z + z (c) $z - \bar{z}$ (d) $z \bar{z}$, for each of the following.

(5)
$$z-2+i$$

(iii)
$$z = \frac{1+i}{1-i}$$

(iv)
$$z = \frac{4}{2} + \frac{3i}{4i}$$

Solution.-

$$z = -t$$

(a)
$$z = 0 \cdot i$$

 $\bar{z} = 0 + i$

$$(b) \qquad z + z$$

$$= -i + i$$

$$= 0$$

$$\begin{aligned} \langle c \rangle & z - \widehat{z} \\ &= -i - \langle i \rangle \\ &= -i - i \\ &= 2i \end{aligned}$$

(4)
$$zz$$

= $(-1)(1)$
- i^2
= $-(-1)$
- 1

$$5(ii) \qquad z = 2 + i$$
(a) $\overline{z} = 2 + i$

(b)
$$2 + \overline{z}$$

 $-(2+i)+(2-i)$
 $2+i+2-i$
 $=4$

(c)
$$z = \overline{z}$$

 $-(2+i)-(2-i)$
 $= 2+i-2+i$
 $-2i$

(d)
$$z\overline{z}$$

 $(2+i)(2-i)$
 $= 4-(i^2)$
 $= 4-(-1)$
 $= 4+1=5$

$$5(iii) z \frac{l+a}{l-i}$$

(a)
$$=\frac{1+i}{1-i} \times \frac{1+i}{1+i}$$

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$$\frac{(I+i)^2}{1+i^2} - \frac{1-i^2+2i}{1+1}$$

$$\frac{I-J+2i}{2} = 1=0+i$$

$$\bar{z} = 0 - i$$
(b) $z + \bar{z}$

$$1-1 - 0$$
(c) $z - \bar{z}$

$$= i - i - i$$

$$- i + i = 2i$$
(d) $z \bar{z}$

$$= (i) (-i)$$

$$- (-i)^2 - (-1) = i$$

$$\frac{4-3i}{2+4i} \times \frac{(2-4i)}{2-4i}$$

$$= \frac{(4-3i)(2-4i)}{(2)^2 - (4i)^2}$$

$$- \frac{4(2-4i) - 3i(2-4i)}{4-16i^2}$$

$$- \frac{8-16i - 6i + 12i^2}{4-16i - 1}$$

$$= \frac{8-22i + 12(-1)}{4+16} - \frac{-4-22i}{20}$$

$$= \frac{4}{20} - \frac{22}{20}i$$

$$z = -\frac{1}{5} - \frac{11}{10}i$$
(a) $\bar{z} = \frac{1}{5} - \frac{11}{10}i$

..............

Phot Superorg Mathematics 144 Class 9th ...

(b)
$$z + \overline{z} = \left(-\frac{1}{5} - \frac{11}{10}i\right) + \left(-\frac{1}{5} - \frac{11}{10}i\right)$$

$$= \frac{1}{5} - \frac{11}{10}i - \frac{1}{5} + \frac{11}{10}i$$

$$= \frac{1}{5} - \frac{1}{5} - \frac{1}{10}i - \left(-\frac{1}{5} - \frac{11}{10}i\right)$$

$$= \frac{1}{5} - \frac{11}{10}i + \frac{1}{5} - \frac{11}{10}i$$

$$= \frac{11}{10}i - \frac{11}{10}i$$

$$= -\frac{22}{10}i = \frac{11}{5}i$$
(d) $z = -\frac{11}{5} - \frac{11}{10}i + \left(-\frac{1}{5} + \frac{11}{10}i\right)$

$$= \frac{1}{5}i + \frac{121}{100}i - \frac{1}{5}i$$

$$= \frac{1}{25}i + \frac{121}{100}i - \frac{1}{100}i$$

$$= \frac{1}{25}i + \frac{121}{100}i - \frac{1}{100}i$$

$$= \frac{125}{100}i + \frac{1}{100}i - \frac{1}{100}i$$

$$= \frac{125}{100}i + \frac{1}{100}i - \frac{1}{100}i$$

$$= \frac{1}{25}i + \frac{121}{100}i - \frac{1}{100}i$$

$$= \frac{1}{25}i + \frac{$$

(v) $\frac{1}{2}(z+z)$ is a real part of z

Pilot S	uperone Mathematics	145	Class 9 ⁴
	(vi) $\frac{1}{2i}(z-\overline{z})$	is the (magnary part	of z
Solut	ions:		
6(i)	$z \leq 2 + 3i$		
	and		
	w 5 41		
	z + w - 2 + w	(To show)	
	$\overline{z} = 2 - 3i$		
	ਸਾਂ 5 + <i>4।</i>		
	Now,		
	z + w = 2 + 3i + 5	4	
	7 i		
	$\overline{z+w}=7+i$	Ø	
	$z\pm w=(2\cdot 3i)+($	3 + 40	-
	2 3145	+ 4i	
	7+3	ſω	
	z + w - '∰ * w	(From 1 and 1i)
6(ü)	z - ₩ = Ī H	-	
	We find $z = w$		
	2 w (2 + 3i) 1	5 H)	
	=2 + 3i 5 +	41	
	3 + 71		
	z w = 3 7t	(i)	
	ž 23i		
	$\overline{w} \rightarrow 5 + J_1$		
	z = w - (2 - 3i) = 6 z = 3i - 5 = 6		

Victorium description of the factor old Days of Versa Sales To Course & Course

MATHEMATICS FOR 9TH CLASS (UNIT # 2) ______

Pilot S	uperone Mathematics	146 Class 9th
	= 3 7i	(11)
	$\overline{z-w} - \overline{z} - \overline{w}$	(From 1 and ii)
6(iii)	ZW "Z W	
	We find zw	
	zw (2 + 31)(5 -	41)
	×2(5 41) + 3	3i(5 - 41)
	10 - 8i + 1	Si 12i ²
	10 + 7i - 7	2(-1)
	10 + 7i + 1	2
	= 22 + 7i	
	zw 22 7i	0
	$\overline{z} = 2 - 3i$	
	w = 5 + 4i	
	z ₩ (2 - 31)(5 +	4i)
	2(5 + 4i)	31(5 + 4i)
	· 10 + 8i - 1	5i ~ 12i ²
	= 10 7i - 1.	2(I)
	- 10 71 + 1	2
	= 22 71	(0)
	$z''w' = \overline{z}''w'$	(From 1 and ii)
6(<i>i</i> v)	$\left(\frac{\overline{z}}{M}\right) = \frac{\overline{z}}{\overline{M}}$	(w ≠ 0)
	We find $\frac{z}{w}$	
	2 2 + 32	
	w 5 - 4i	
	$\frac{2+3i}{5+4i} \times \frac{5}{5}$	<u>+ 4i</u> + 4i

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Prior Superone Mathematics 147 Glass 9°

$$\frac{(2+3i)(5+4i)}{(5i'-(4i))^2}$$

$$= \frac{2(5+4i)+3i(5+4i)}{25-16i^2}$$

$$- \frac{10+8i-15i+12i}{25-16i-1i}$$

$$= \frac{10+23i+12(-1)}{4i} - \frac{10-23i-12}{4i}$$

$$= \frac{-2+23i}{4i}$$

$$\frac{z}{w} = \frac{-1}{4i} + \frac{23}{4i}$$

$$0)$$
Now,
$$\frac{z}{w} = \frac{2-3i}{5+4i}$$

$$- \frac{2-3i}{5+4i} \times \frac{5-4i}{5-4i}$$

$$\frac{z}{w} = \frac{(2-3i)(5-4i)}{(5i'+(4i)^2}$$

$$- \frac{2(5-4i)-3i(5-4i)}{25-16i^2}$$

$$= \frac{10-8i-15i+12i^2}{25-16(-1)}$$

$$\frac{10-23i-12}{4i}$$

$$= \frac{-2-23i}{4i}$$

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$$\frac{z}{w} = \frac{z}{w} \qquad \text{(From 1 and 11)}$$

$$6(v) = \frac{1}{2}(z + z)$$

$$= \frac{1}{2}[2 + 3i + 2 - 3i]$$

$$= \frac{1}{2}[4 + i]$$

$$= 2 \quad (2 \text{ is a real part of } z)$$

$$6(vi) = \frac{1}{2}(z - \overline{z})$$

$$= \frac{1}{2}[(2 + 3i) \quad (2 - 3i)]$$

$$= \frac{1}{2}[2 + 3i - 2 + 3i]$$

$$= \frac{1}{2}[6 + i]$$

$$3i \quad (3 \text{ is imaginary part of } z)$$
Q.7. Solve the following equations for real x and y.

(i) \quad (2 - 3i)\quad (x + yi) \quad 4 \quad i

(ii) \quad (3 - 2i)\quad (x + yi) \quad 4 \quad i

(iii) \quad (3 + 4i)² \quad 2(x - yi) \quad x + yi

Solution:-

7(i) \quad (2 - 3i)\quad (x + yi) \quad 4 + i
\quad (2x + yi) \quad 3i(x + yi) \quad 4 + i
\quad (2x + 2yi \quad 3xi \quad 3yi^2 \quad 4 + i
\quad (2x + 2yi \quad 3xi \quad 3yi \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2y \quad 3xi) \quad 4 + i
\quad (2x + 3y) + (2x + 3y) \quad 4 + i
\quad (3x + 3y) \quad 4 +

and

Pilot Superone Mathematics 149 Multiply eq (ii) by 3 and eq (iii) by 2 6x + 9x- 12 (m) to fix 2 tivi From (12) + (111) 131 14 $3 = -\frac{I4}{I3}$ Putting $y = \frac{I4}{I3}$ in Ω $2x + 3\left(\frac{JJ}{JJ}\right) = J$ $2x \cdot \frac{42}{13} +$ $2x^{-1}4 - \frac{12}{13}$ $2x - \frac{10}{13}$ $x + \frac{10}{2 \times 13}$ Thus (3-2i)(x+yi) = 2(x-2yi)+2i-1 $3x + 3yi - 2xi - 2yi^{2} - 2x - 4yi + 2i - 1$ 3x + 3yi - 2xi - 2y(-1) - 2x - 4yi + 2i - 13x + 3yi - 2xi + 2y - 2x - 4yi + 2i - 13x - 2x + 3yi + 4yi - 2xi + 2yi = -1 - 2i $\Rightarrow x + 2y + 7yi - 2xi = 1 + 2i$ (x + 2y) + (7y - 2x)y = 1 + 2iThus x + 2vm

Pilot Superone Mathematics	150		Class 9 ^a
and	7y 2x	2	(ii)
(10)	2x + 4y	-2	
Multiplying eq. (i) l	b y 2		
	Hy	0 A	dding (ui), (ii)
	y	0	
	x + 2(0)	I	
Putting v 0 m eq	(n		
	x + 0	-1	
	r	1	
I hus x	-1y	= 0	
7(iii) (3 + 41) ²			
$9 + 24i + 16i^2 - 3$	2x + 2yi	= x + yî	
9 + 24i + 16i - 1)	2x + 2y4	* x - yi =	= O
91 241 16	3x + yî	≠ 0	
	- lr + yi	· 16 9	241
	-3x + yt	7 240	!
Thus	-3x	. 7	(i)
and	y	24	(ii)
		$-\frac{7}{3}$	
- 1	x	3	From (t)
*\ } *!\	$-\frac{7}{3}$, y	_ 3.6	
Thus x	$-\frac{3}{3}$	- 24	
\vee			

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Pilot Superone Mathematics 157 Class 9th



LOGARITHMS

Scientific Notation:

Scientist have developed a concise precise and convenient method to write very small or very large numbers, that is called scientific notation of expressing an ordinary number

A number in the form $a \times 10^n$ where $1 \le a \le 10$ and n is an integer in called the scientific notation.

Exercise 3.1

Q.1.	Express	each	of	the	following	numbers	in
	scientific	notati	on.				

~+-+			
(i)	5700	(ii)	49.800,000
(ät)	96 000, 000	(iv)	4169
(v)	83 000	(vi)	0.00643
(vii)	0.0024	(viii)	60 000, 000
(ix)	0.00000000395	(x)	275,000

Solution:-

$$I(i) = 5700$$

$$= 5.700 \times 1000$$

$$= 5.7 \times 10^{3}$$

$$I(ii) = 49,800,000$$

$$= 4.9800000 \times 10000000$$

 4.98×10^{7}

Pilot Superone Mathematics 158 1(iii) 96, 000, 000 9 6000000 × 1000v000 $= 96 \times 10^{7}$ 1(iv) 416.9 4.169 x 100 = 4.169 × 10² 1(v) 83000 = 8 3000 × 10000 = 83 x 104 l (vi) 0.00643 $=\frac{6.43}{1000}=\frac{6.43}{10^3}-6.43\cdot10^{-3}$ 1(vii) 0074 · 74 = 74 - 74,18 \$ I(viii) 60, 000, 000 - 6 0000000 ×10000000 · 6 × 10 16x) 0.00000000395 $\frac{3.95}{1000000000} = \frac{3.95}{10^9}$ 3 95 10 2 $I(x) = \frac{275000}{0025}$ 27500 × 100000 25 $\frac{2.75 \times 10^5}{2.5 \times 10^{-3}}$ Q.2. Express the following numbers in ordinary

notation.

(A) 6×10 4

(ii) 5.06×10^{10}

Prior Superone Mathematics 159 Class 9th (iii) 9 018 \times 10 6 (iv) 7 865 \times 10⁸

Solution:-

$$6 \times \frac{1}{10^4} - 0006$$

$$= 9018 \times \frac{1}{10^5} = 000009018$$

Logarithm of a Real Number

If $a^x = y$, then x is called the logarithm of 'y' to the base 'a' and is written as $log_a y = x$, where a > 0, $a \ne I$ and y > 0.

If
$$a^{x} = y$$

then $log_{a}y = x$ and
if $log_{a}y = x$
then $a^{x} = y$

Thus $a^x = y$ and $log_a y = x$ are equivalent equations $a^x = y \text{ is exponential form and}$ $log_a y = x \text{ is logarithmic form}$

Remember:

$$a^0 = I \Rightarrow log_a' = 0$$
 and $a' = a \Rightarrow log_a' = I$

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Exercise 3.2	
Q.1. Find the common logarithms of	the following
numbers.	
	9.326
(iii) 0 00032 (iv) 0	3206
Solution:-	
1(i) log 232 92	
(i) Integral part has three (3) digits	
ch = 3 + 1 = 2	
(ii) To find mantissa, we round off 232 92	to 232 9
Log Table	Mean
	Differences
01 2 3 4 5 6 7 8 5	123456789
-	<u> </u>
23 3650	17
(tit) We see the log table and find the row co	rresponding to 23.
the) We proceed horizontally and	reach column
corresponding to 2. The number at	the intersection in
365 5	
(v) Proceeding ahead we find a num	ber in the mean
difference column under 9 It is 17 N	Mantissa is 3033 ·
17 3672	
log 232 92 2 3672	
1(11) log 29 326	
(i) Integral part has (2) digits.	
ch = 2 - 1 = 1	
(iii) To find mantissa, we round off 29 32	6 to 29 32 7
Log Table	Mean
	Differences
0 1 2 3 4 5 6 7 8 9	123456789
★	1
29 4669	

Pilot Superone Mathematics 161 Class 9th

- (iti) We read the log table and find the row corresponding to 29
- (iv) We proceed horizontally and reach column corresponding to 3 The number at the intersection is 4669
- (v) Proceed ahead and we find a number in the mean differences column under 1 it is 4. Mantissa is 4669 + 4 = 4673

. log 29 326 1 4673

I(iii) log 0.00032

(1) There are three zeros on the right of the decumal point:-

ch = 4

Log Table											Mana
		_							_		Differences
	0		2	3	4	5	6	7	8	9	123456789
	+										
<i>32</i>	5051									i	
/		_									<u> </u>

(ii) Corresponding to 32 in the log table, we proceed horizontally and under 0 find a number 5051

Mantissa = 5051

Thus $log 0 00032 = \frac{1}{4} 5051$

1(0v) log 0.3206

(i) The integral part of 0.3206 is 'o' and there is no zero on the right of decimal point

ch = 1

			I	Log	Tal	blc					Mean Differences
<u>_</u> .	0	I	2	3	4	3	6	7	8	9	123456789
32	5051		_								8

	161	Class 9 th
Prior Superone Mathematics	104	

- Corresponding to 32 in the log table, we proceed m horizontally and under θ find a number 5051
- We proceed ahead and find in the mean difference (iii) column under 6 number 8.

$$log \ 0. \ 3206 = \overline{1} \ 5059$$

- Q.2. If log 31.09 = 1. 4926, find the values of following.
 - log 3 109 (i)
- log 310.9 (ii)
- log 0 003109 tiin
- log 0.3109 (iv)

Solution:-

- (Given) 1 4926 log 31 09 (2)
- (Mantissa does not change) log 3 109 = 0.49262(i)
- log 3109 2.4926 2(ii)
- $log \ 0 \ 003109 = \hat{3} \ 4926$ 2(iii)
- log 0 3 109 1 4926 Z(iv)
- Q.3. Find the numbers whose common logarithms are:
 - 1 7427 3 5621 (iii) a.
- Let the number = x 310

here ch

Anti-log Table	Mean Differences
0 1 2 3 4 5 6 7 8 9	123456789
56 30-48	2

- Corresponding to 56 in the antilog table, we proceed (i) horizonially and under 2, find a number 3648
- We proceed ahead and find in the mean difference (ii) column under ? number 2

Now 3648 + 2 3650 ch 3 therefore, there are four digits in the number Required Number x - 3650

3(ii) Let the number a

here $ch = \overline{2}$

Therefore, there will be ONE zeros on the right side of decimal point

		A	nti-	log	T	abl	e				Mean Differences
	0	1	2	3	4	5	6	7	ĕ	g	123456789
74			35	21	_						y

- (i) Corresponding to 74 in the antilog table, we proceed horizontally and under 2, find a number 5521
- (iii We proceed ahead and find in the mean difference column under 7 number 9

ch = 2, therefore, there are four digits in the number Required Number x = 0.5530

- Q.4. What replacement for the unknown in each of the following will make the statement true?
 - (i) log₃ 81 L

(ii) $leg_a 6 = 0.5$

(iii) $log_5 n = 2$

(iv) $10^6 = 40$

4(i)
$$log_3 8l - L$$

 $3^L - 8l$ (Writing in the exponential form)
 $3^L = 3^4$
 $L = 4$

4(ii) $log_a 6 = 0.5$ $6 = a^5$ (Writing in the exponential form) $6 = a^{5.10}$

Pilot Superone Mathematics 164 6 = 017 $6^2 = (a^{1/2})^2$ (Squaring) $36 = a^{1/2 \times 2}$ 36 = aa = 36Thus 4(iii) logs" = 2 $n = 5^2$ (Writing in the exponential form) n = 25 $10^{9} = 40$ 4(iv) $3^{t} = log 40$ (Taking log) $p \log 10 = 1$ 6021 (using log table) P = 16021 (log 10 =1) O.S. Evaluate: (i) $log_2 \frac{1}{128}$ (ii) log 512 to the base $2\sqrt{2}$ $S(i) = \log_2 \frac{1}{128}$ Let $x = log_2^{1/28}$ $2^{x} = \frac{I}{I28}$ (Writing in exponential form) $2^{2} = 2^{-7}$ Thus x = -75(ii) = log 512 to the base $2\sqrt{2}$ Let $x = log_2 \sqrt{2}$ $(2\sqrt{2})^2 = 512$ (Writing in exponential form) $\sqrt{2 \times 2 \times 2} = 512$ $(\sqrt{8})^x = 512$ $(8^{1/2})^x = 8^3$ $8^{x/2} = 8^3$

Prior Superone Mathematics 165 $\frac{x}{2} = 3$ Thus Hence x 3 x 2 = 6 Q.6. Find the value of x from the following statements. (i) $\log_2 x = 5$ (ii) $\log_{8x} x = x$ (iii) $\log_{10} 8 = \frac{x}{2}$ (iv) $\log_{10} 84 = 2$ (v) $\log_3 x = 4$ 6(i) log_x =5 $x = 2^5$ (Writing in exponential form) $6(ii) \quad \log_{BI}{}^9 = 5$ $(81)^x = 9$ (Writing in exponential form) $(\mathbf{y}^2)^{r} = 9$ 02 = a 2x = Ior $x = \frac{1}{2}$ 6(ii) $log_{64}^{8} = \frac{x}{2}$ $(64)_2^{\frac{3}{2}} \approx 8$ (Writing in exponential form) $8^{2\sqrt{\frac{2}{1}}} = 8$ $S^{x} = S$ Thus x = 1 $6(tv) \log_x 4 = 2$ $x^2 = 64$ (Writing in exponential form) Thus 6(v) log3 x -4 $x = 3^t$ (Writing in exponential form)

Wightenance described delegate and the Return Cld Devent March Telegate Ache IV Courses & service

Thus

Polit Superone Mathematics 166 Class
$$g^{th}$$

(Laws of Logarithm)

Law (i)

 $log_{a}^{(mn)} = log_{a}^{m} + log_{a}^{m}$

Proof

Let $log_{a}^{m} = x$, $log_{a}^{n} = y$
 $a^{x} = m$ (i)

and $a^{y} = n$ (ii)

 $a^{x} \times a^{y} = m \times n$ from (.) × (ii)

 $a^{x+y} = mn$
 $log_{a}^{mn} = x + y$ (Writing log form)

 $= log_{a}^{m} + log_{a}^{m}$ (Writing values of x , y)

Law (ii)

 $log_{a}^{mn} = log_{a}^{m} - log_{n}^{m}$

Proof

Let $log_{a}^{m} = x$

and $log_{a}^{m} = y$ (Writing in exponential form)

 $a^{x} = m$ (i) Dividing (i) by (it)

 $\frac{a^{x}}{a^{y}} = \frac{m}{n}$ (Writing in log form)

 $log_{a}^{mn} = x - y$ (Putting values of x , y)

 $log_{a}^{mn} = log_{a}^{m} - log_{a}^{m}$

Law (iii)

 $log_{a}^{mn} = n + log_{a}^{m}$

Proof.

Let $log_{a}^{mn} = x$

Pilot Superone Mathematics 167 or $a^x = m^h$ Let $log_a^m = y$ or a m (i) a* =m* $= (\alpha^y)^n$ From (i) $a^{I} = a^{m}$ So x yn = ny, loga" - n loga" Law (iv) (Change of base) $log_a^m = log_b^n \times log_a^b = \frac{log_b^n}{log_b^a}$ **Proof** Let $\log_b^A = x \Rightarrow n - b^x$ $\log_a^a = \log_a^b = x \log_a^b$ (Taking log to base a) $\log_a^n - \log_b^n \log_a^b$ $\log_b{}^b \times \log_a{}^b - \log_a{}^a = 1$ or $log_a^b = \frac{l}{log_b^a}$ Putting value of log_a^b in (i)

With a way of the state of the

 $log_a^n = \frac{log_b^n}{log_b^a}$

Class 9° Pilot Superone Mathematics 158

Exercise 3.3

Q.1. Write the following into sum or difference

(i)
$$log(A \times B)$$

(ii)
$$log \frac{15.2}{30.5}$$

(iii)
$$\log \frac{21 \times 5}{8}$$
 (iv) $\log \sqrt[3]{\frac{7}{15}}$

(iv)
$$\log \sqrt[3]{\frac{7}{15}}$$

(v)
$$\log \frac{(22)^{1/3}}{5^3}$$

$$(vi) \quad \log \frac{25 \times 47}{29}$$

Solution:-

$$I(i) = \log(A \times B)$$

$$= \log A + \log B$$

$$I(ii) = log \frac{15.2}{30.5}$$

1(iii)
$$\log \frac{25 \times 5}{8}$$

$$I(iv)$$
 $log\sqrt[3]{\frac{7}{15}}$

$$= \log\left(\frac{7}{15}\right)^{1/3}$$

$$\frac{1}{3}[\log 7 - \log 15]$$

$$I(v) = \log \frac{(22)^{1/3}}{5^3}$$
$$= \log (22)^{1/3} - \log 5^3$$

$$=\frac{1}{3}\log 27 - 3\log 5$$

$$I(vi) log \frac{25 \times 49}{29} = log 25 + log 47 - log 29$$

Pilot Superone Mathematics 169 Class 9"

Express as a single logarithm.

$$\log x - 2\log x + 3\log (x + 1) - \log (x^2 - 1)$$

Solution:-

$$log x - 2log x + 3log(x + 1) - log(x^{2} - 1)$$

$$= log x - logx^{2} + log(x + 1)^{3} - log(x^{2} - 1)$$

$$= log \frac{x(x + 1)^{3}}{x^{2}(x^{2} - 1)}$$

$$= log \frac{(x + 1)^{3}}{x(x^{2} - 1)}$$

$$= log \frac{(x + 1)^{3}}{x(x + 1)(x - 1)}$$

$$= log \frac{(x + 1)^{3}}{x(x + 1)(x - 1)}$$

Q.3. Write the following in the form of a single logarithm.

(i)
$$\log 2l + \log 5$$
 (ii) $\log 25 - 2 \log 3$

(III)
$$2 \log x - 3 \log y$$
 (iv) $\log 5 + \log 6 \log 2$

Solution:-

$$3(i) \log 2l + \log 5$$

$$= \log 25 \cdot \log 3^2$$

$$=\log\frac{25}{3^2}$$

$$3(iii) \quad 2\log x - 3\log y$$

$$= \log x^2 + \log y^3$$
$$= \log \frac{x^2}{y^3}$$

$$=\log\frac{5\times6}{2}$$

Class 9" Pilot Superone Mathematics 170 Calculate the following: (i) $log_3 2 \times log_2 81$ (ii) $log_3 3 \times log_3 25$ Solution: $log_3 2 \times log_2 81$ 4(1) $=\frac{\log 81}{\log 3} \quad \frac{\log 3^4}{\log 3}$ $-\frac{4 \log 3}{\log 3} - 4$ 4(ii) log: 3 × log3 25 log 25 log 5 $\frac{2\log 5}{\log 5} = 2$ Q.5. If $\log 2 = 0.3010$, $\log 3 = 0.4771$, $\log 5 = 0.6990$ then find the values of the following. log 14 log 32 (I)

(iv) $\log \frac{\delta}{3}$

Solution:-

(v)

5(i)
$$\log 32$$

 $-\log 2^5$
 $= 5 \log 2 - 5(0 3010) - 1 5050$
5(ii) $\log 24$
 $= \log 8 \times 3$
 $= \log 2^3 \times 3 - \log 2^3 + \log 3$
 $= 3 \log 2 + \log 3$
 $= 3 (0 3010) + 0.4771$
 $= 0.9030 + 0.4771 = 1 3801$
5(tii) $\log \sqrt{3\frac{1}{3}}$

(iii) $log \sqrt{3\frac{1}{3}}$

log 30

Pilot Superong Mathematics 173 Class 9th

$$= log \binom{10}{3}^{1/2}$$

$$= \frac{1}{2} log \binom{10}{3}$$

$$= \frac{1}{2} log \binom{2 \times 5}{3}$$

$$= \frac{1}{2} [log 2 + log 5 - log 3]$$

$$= \frac{1}{2} [0 \ 3010 + 0 \ 6990 - 0 \ 4771]$$

$$= \frac{1}{2} (5229) = 0 \ 2615$$

$$5(iv) log \frac{8}{3}$$

$$= log 2^{3} - log 3$$

$$= log 2^{4} - log 3$$

$$= log 2 - log 3 = 3(0 \ 3010) - 0 \ 4771$$

$$= 0 \ 9030 - 0 \ 4771 = 0 \ 4259$$

$$5(v) log 30$$

$$= log 2 \times 3 \times 5$$

$$= log 2 + log 3 + log 5$$

$$= 0 \ 3010 \ 0 \ 4771 + 0 \ 6990$$

$$= 1 \ 4771$$

Priot Superone Mathematics 172 Exercise 3.4 Use log tables to find the value of: O.J. (ii) (789.5)^{1/8} 0.8176 × 13 64 (iv) $\sqrt[4]{2709} \times \sqrt[4]{1239}$ 0.678×9.01 0.0234 (v) $\frac{(1\ 23)(0\ 6975)}{(0.0075)(1278)}$ (vi) $\sqrt[3]{0.7214 \times 20.37}$ (vii) $\frac{83 \times \sqrt[3]{92}}{127 \times \sqrt[3]{246}}$ (viii) $\frac{(438)^3 \sqrt{0.056}}{(388)^4}$ 1(t) 0.8176 × 13 64 Let $x = 0.8176 \times 13.64$ $log x = log(8176 \times 13.64)$ (Taking log) ≈ log 8176 + log 13 64 $=\overline{1}.9125 + 1.1348$ $\log x = 1.0473$ Antilog (log x) = Antilog 1 0473 (Taking anti-log) $x \Rightarrow 11.15$ I(ii) (789 5)14 Let $x = (789.5)^{1/8}$ $\log x = \log (789.5)^{1/5}$ $=\frac{1}{8} \log 7895$ $=\frac{1}{9}[28974]=03622$ Antilog $(\log x) = Antilog (0.3622) = 2.302$ $I(iii) = \frac{0.678 \times 9.01}{0.0234}$

Let $x = \frac{0.678 \times 9.01}{0.6234}$

Pilot Superone Mathematics 173 $\log x = \log \frac{0.678 \times 9.01}{0.023d}$ Taking \log log 0.678 + log 9 01 log 0.0234 $= \vec{1} \cdot 8312 + 0.9547 \cdot (\overline{2} \cdot 3692)$ $= \overline{1} 8312 + 0.9547 \quad \overline{2} - 3692$ $=-1 + 8312 + 0.9547 + 2 \quad 3692 - 2.4167$ Antilog (log x) = Antilog 2.4167 Taking anti-log x = 2611(iv) \$\frac{1}{2.709} \times \frac{1}{2.39} Let $x = \sqrt[3]{2.709} \times \sqrt[3]{1.230}$ $x = (2709)^{1/3} \times (1239)^{1/3}$ $log x = log (2.709)^{1/5} \times (1.239)^{1/7}$ (Taking log) $= \frac{1}{5} \log 2 \ 709 + \frac{1}{7} \log 1 \ 239$ $=\frac{1}{5}(0.4328)+\frac{1}{2}(0.0931)$ = 0.0866 + 0.0133log x = 0.0999 (Taking anti-log) Antilog $(\log x) = Antilog 0.0999$ x = 7.258 $I(v) = \frac{(1.23)(0.6975)}{(0.0075)(1278)}$ Let $x = \frac{(1.23)(0.6975)}{(0.0075)(1278)}$ $log x = log \frac{(1.23)(0.6975)}{(0.0075)(1.278)}$ (Taking log) log x = log 1 23 + log 0 6975 - log 0 0075 - log 1278 $= 0.0899 + 1.8435 \cdot (3.8751) (3.1065)$ $= 0.0899 \quad I + 8435 + 3 \quad 8751 - 3.1065$ $10482 = -10482 \quad 1 + 1$

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Pilot Superone Mathematics 174 2 9518 log x Antilog $(\log x) = Antilog \frac{x}{2}$ 9518 (Taking anti-log) $1(vi) = \sqrt[3]{\frac{0.7214 \times 2037}{608}}$ Let $x = \sqrt[3]{\frac{0.7214 \times 20.37}{60.8}}$ $x = log \left(\frac{0.7214 \times 20.37}{60.8} \right)^{1.3}$ (Taking log) $\log x = \frac{1}{3} [\log 7214 + \log 20.37 - \log 60.8]$ $=\frac{1}{3}\tilde{11} 8582 + 1.3090 - 1.7839$ $=\frac{1}{3}[-1 + 8582 + 13090 + 17839]$ $=\frac{1}{2} \left[-0.6167 \right] = -0.2056$ = -0.2056 - I + 1 T 7944 Antilog $(\log x) = Antilog \overline{1} + 7944$ (Taking anti-log) x 6229 $\int_{I(vii)} \frac{83 \times \sqrt[3]{92}}{127 \times \sqrt[3]{24}}$ Let $x = \frac{83 \times \sqrt[3]{92}}{127 \times \sqrt[3]{246}}$ $x = \frac{83 \times (92)^{1.1}}{127 \times (246)^{1/5}}$ (Taking log) $\log x = \log 83 + \frac{1}{3} \log 92 \log 127 - \frac{1}{5} \log$

Pilot Superone Mathematics 175 $=19191 + \frac{1}{3}(19638) - (21038) - \frac{1}{5}(23909)$ = 1 9191 + 0 6546 2 1038 0.4782 2 5737 2 582 = 0083 = - 0083 - 1 + 1 log x 1 9917 Antilog $(\log x) = Antilog \overline{I}$ 9917 (Taking anti-log) $I(viii) = \frac{(438)^3 \sqrt{0.056}}{(388)^4}$ i Let $r = \frac{(438)^3 \sqrt{0.056}}{(388)^4}$ $x = \frac{(438)^3 \times (056)^{12}}{(388)^4}$ $\log x = 3 \log 438 + \frac{1}{2} \log(056) - 4 \log 388$ (Taking log) = $3(2.6415) + \frac{1}{2}(2.7482) + 4(2.5888)$ 7 9245 + 1 3741 10 3552 $\log x = -3.0566 = -3.0566 - 1 + 1$ J 0134 Antilog (log τ) = Antilog 4 9434 (Taking anti-log) x = 0.0008778Q.2. A gas is expanding according to the law $pv^n = C$, find C when p = 80, $y = 3.1 m = \frac{5}{4}$ Solution - $C = pv^*$

Pilot Superone Mathematics 176. Class 9*

Putting values of p, v, n

$$C = 80(3.1)^{3.4}$$
 $log C = log 80 \pm \frac{5}{4} log 3.1$ (Taking log)

= 1.9031 + $\frac{5}{4}$ (0.4970)

= 1.9031 + $\frac{2.4570}{4}$

= 1.9031 + 0.6143

 $log C = 2.5174$

Antilog (log C) = Antilog 2.5174 (Taking anti-log)

 $C = 329.2$

Q.3. The formula $p = 90 (5)^{-910}$ applies to the demand of a product, where q is the number of units and p is the price of one unit. How many units will be demanded if the price is Rs 18.00?

Solution:-

$$p = 90(5)^{-\sqrt{10}}$$

$$18 \log 90(5)^{-\sqrt{10}}$$

$$\log 18 = 90(5)^{-\sqrt{10}}$$
 (Taking log)
$$= \log 90 + \log 5^{-\sqrt{10}}$$

$$\log 18 \log 90 \quad \frac{9}{10} \log 5$$

$$12552 = 1.9542 - \frac{q}{10}(0.6990)$$

$$= 1.9542 - 0699 q$$

$$0699q = 19542 \mid 2552$$

$$0699q = 6990$$

$$q = \frac{06990}{0699} = \frac{6990}{0699}$$

$$10 \qquad \text{Units}$$

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Prior Superone Mathematics 177 Q.4. If $A = \pi r^2$, find A, when $\pi = \frac{22}{7}$ and r = 15. Solution:-A 75 Putting $\pi = \frac{22}{7} r = 15$ 4 22×1157 (Liking tog) log 22 log 7 + 2 log 15 - 13424 | 0845] + 2(17761) 13424 08451 + 23522 log A 28491 Antitog (log A) - Initlog 2 8495 (Taking anti-log) Q.5. If $V = \frac{1}{3} \pi r^2 h$, find V, when $\pi = \frac{22}{7}$, r = 2.5 and h = 4.2Solution- $1 = \frac{1}{3} \pi r h$ Putting values of $h \neq \pi$ V = 1 x 22 x 12 5 8 x 4 2 log $V = log \frac{1}{4} \times \frac{22}{7} \times (2.5)^2 \times 4.2$ (Taking log) log 22 2 log 25 + log 42 log 3 log -13424 200 3979) + 06232 | 04771 | 0.8451 13424 - 1958 + 6232 - 0477 | 08451 lov t 1 4392 Antilog (log F) Antilog / 4392 (Taking anti-log) 1 2"49

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Class 9"



ALGEBRAIC EXPRESSIONS AND ALGEBRAIC FORMULAS

Types of Algebraic Expressions

- Po ynomial express ons
- (ii) Rational Expression
- (101) Irrational expression

(i) Polynomial expressions.

A polynomial consists of one or more than one terms. The exponent of variable or variables is zero or positive integer. For example 12 - x, 3x - 4y, $x^2 - 2x + 1$, $\sqrt{3}x$ are polynomial expressions, where as $\frac{2}{x^3}$, $x + \frac{1}{x}$, $\sqrt{3}x - \frac{1}{\sqrt{3x}}$ and

35x $\frac{6}{x}$ are not polynomials.

(n) Rational Expression.

 $\frac{p(x)}{q(x)}$ is a rational expression where as p(x), q(x) are

polynomials and $q(x) \neq 0$.

(iii) Irrational expression.

If an algebraic expression cannot be written in the form $\frac{p(x)}{q(x)}$ where p(x), q(x) are polynomials and $q(x) \neq 0$ in called an irrational expression. For example \sqrt{x} , x', $\sqrt[4]{x'y'}$ and

 $\sqrt{x^2+1}$, $\frac{1}{\sqrt{x+2}}$ are irrational expressions

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Exercise 4.1

Identify whether the following algebraic expressions O.Iare polynomials (Yes or No)

(i)
$$3x^2 + \frac{1}{x} - 5$$

(n)
$$3x^3 - 4x^2 - x\sqrt{x} + 3$$

(iii)
$$x^2 - 3x + \sqrt{2}$$

(iii)
$$x^2 - 3x + \sqrt{2}$$
 (iv) $\frac{3x}{2x-1} + 8$

Solutions:

$$I(0) = 3x^2 + \frac{1}{x} + 5$$

No

Reason $\frac{1}{2}$

$$I(ii) = 3x^3 + 4x^2 + x\sqrt{x} + 3$$

No

Reason⁻ √x

$$t(iii)$$
 $x^2 = 3x + \sqrt{2}$

$$I(iv) = \frac{2x}{2x-1} + 8$$

No

Reason:

State whether each of the following expression is a 0.2 rational expression or not.

$$(1) \quad \frac{3\sqrt{x}}{3\sqrt{x}+5}$$

(ii)
$$\frac{x^3-2x^2+\sqrt{3}}{2+3x-x^3}$$

(iii)
$$\frac{x^2 + 6x + 9}{x^2 - 9}$$

(iv)
$$\frac{2\sqrt{x}+3}{2\sqrt{x}+3}$$

Salutions:

$$2(i) \qquad \frac{3\sqrt{x}}{3\sqrt{x}+5}$$

Since $3\sqrt{x}$ and $3\sqrt{x} + 5$ are not polynomials therefore, the given expression is not an algebraic rational

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2(ii)
$$\frac{x^3 + 2x + \sqrt{3}}{2 + 3x + x^2}$$

It is rational expressions as $x^3 - 2x^2 + \sqrt{3}$ and $2 + 3x - x^2$ are polynomials

$$2(iii) = \frac{x^2 + 6x + 9}{x^2 - 9}$$

It is a rational expression. Both denominator and numerator are polynomials

$$2(iv) \quad \frac{2\sqrt{x}+3}{2\sqrt{x}-3}$$

It is not a rational expression $2\sqrt{x} + 3$ and $2\sqrt{x} = 3$ are not polynomials

Q.3 Reduce the following rational expressions to the lowest forms.

(i)
$$\frac{120x^2y^2z^3}{30x^3yz^2}$$
 (ii) $\frac{8a(x+1)}{2(x^2-1)}$

(iii)
$$\frac{(x+y)^2 - 4xy}{(x-y)^2}$$
 (iv)
$$\frac{(x^2 - y^2)(x^2 - 2xy + y^2)}{(x-y)(x^2 + xy + y^2)}$$

(v)
$$\frac{(x+2)(x^2-1)}{(x+1)(x^2-4)}$$
 (vi) $\frac{x}{2x}\frac{4x+4}{8}$

(vii)
$$\frac{64x^3-64x}{(8x^2+8)(2x+2)}$$
 (viii) $\frac{9x^3-(x^2-4)^2}{4+3x^2-x^2}$

Solutions:

$$360 = \frac{120x^2y^3z^5}{30x^3yz^2}$$

Class 9th Pilot Superone Mathematics 188 30×413-12f-1 41 / 8a(x+1)3(ii) 2(x) 1) $-\frac{2 \times 4a(x+1)}{2(x+1)(x-1)} = -\frac{4a}{x-1}$ $3(iii) = \frac{(x+y)^2}{(x-y)^2} \frac{4xy}{x^2}$ $=\frac{x^{2}+y^{2}+2xy-4xy}{(x-y)^{2}}$ $\frac{x}{x} = \frac{2xy + y}{2xy + y}, = 1$ $3(b) = \frac{(x'-y)(x'-2xy+y')}{(x-y)(x'+3y+y')}$ $=\frac{(x_1^2 + y_1^2)(x_1^2 - 2xy_1 + y_1^2)}{(x_1^2 + y_1^2)}$ $= \sqrt{2} (2x + y^2 + (x - y))^2$ $J(v) = \frac{(x+2)(x-1)}{(x+1)(x-4)}$ $=\frac{(x+2)(x^2-1^2)}{(x+1)(x^2-2^2)}$ $-\frac{(x+2)(x+1)(x-1)}{(x+1)(x+2)(x-2)} = \frac{x-1}{x-2}$ $3(vt) = \frac{x^2 + 4x + 4}{2x^2 + 8}$ x' - 2x = 2x + 4

Pilot !	Superone Mathematics	189	Class 9 th
	$\frac{x_1x-2)-2(x-2)}{2(x-2^5)}$		
	$= \frac{(x-2)(x-2)}{2(x-2)(x+2)}$		
	$=\frac{x-2}{2(x+2)}$		Δ
3(vii)	$\frac{64x^3 - 64x}{(8x^3 + 8)(2x + 2)}$		C
	$=\frac{64x(x^4-1)}{8(x^2+1)(2)(x+1)}$		
	$=\frac{64x[(x^2)^2]}{16(x^2+1)(x+1)}$		
	$=\frac{64x(x^3+1)(x^3-1)}{16(x^3+1)(x+1)}$		
	$= \frac{4x(x-40)(x+18x-1)}{(x-1)(x+1)}$)	
	4x(* +1)		
3(viii)	$\frac{9x^{4}-(x-4)^{2}}{4+3x-x}$		
	$=\frac{(3x)^3-(x)^3}{4+3x}$ (4)		
	$\frac{[3x+(x^2-4)][3x-(x^2-4)]}{(4+3x-x^2)}$	4)	
	$(s\to x-4)(3x_{\pm x})$	4)	
	$(4+3\sqrt{-1})$		
	$= \frac{(x + 3x + 4)(4 + 3x - 4)}{(4 + 3x - 3)}$	<u>S</u>	

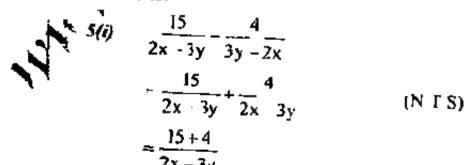
Pilot Superone Mathematics Q4 Finality (a) $\frac{x^{3}\sqrt{-2\tau}}{2\tau}$ for (i) x - 3, y = -1, z = 2 (ii) x = -1, y = -9, z = 4(b) $\sum_{x \in \mathbb{Z}} \frac{5z^2}{1-for} for x = 4, y = -2, z = 1$ Solutions: Putting x 3, y = -1, z = -2 $=\frac{(3)^{2}(-1)}{(3)(-2)}$ =(27)(-1)+4 $=\frac{-27+4}{4}=\frac{-23}{-4}$ = 23 = 3 $4(a)(ii) \frac{x^2y}{x^2} 2z$ $p_{\text{utting}} = x = 1.y - 9.2 - 4$ $(-1)^{2}(-9)-2(4)$ (-1)(4) $=\frac{(-1)(-9)}{4}$ 8 $=\frac{98}{4}=-\frac{1}{4}$

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4(b) $\frac{x^3y^3 - 5y^3}{xyy}$ Putting x = 4, y = 2, y = 1 $= \frac{(4)^2(-2)^3 - 5(-i)^4}{(4)(-2)(-1)}$ $= \frac{(16)(-8) - 5(1)}{8}$ $= \frac{-128 - 5}{8}$ $= \frac{-133}{8} = -16\frac{5}{6}$

- Q.5 Perform the indicated operation and simplify.
- (i) $\frac{15}{2x-3y} \cdot \frac{4}{3y-2x}$ (ii) $\frac{1+2x}{1-2x} \cdot \frac{1-2x}{1+2x}$
- (iii) $\frac{x^2-25}{x^2-36} \frac{x+5}{x+6}$ (iv) $\frac{x}{x-y} \frac{y}{x+y} \frac{2xy}{x^2-y^2}$
- (v) $\frac{x}{x^2+6x+9} = \frac{x+2}{2x^2-18}$
- $= (vi) \qquad \frac{1}{x-1} \frac{1}{x+1} \frac{2}{x^2+1} \frac{4}{x^2-1}$

Solutions:



Class 9" 192 Pilot Superone Mathematics $=\frac{19}{2x-3y}$ $5(d) = \frac{1+2x}{1-2x} \cdot \frac{1-2x}{1+2x}$ (1+2x)(1+2x) - (1-2x)(1-2x)(1-2x)(1+2x) $=\frac{(1+4x+4x^2)\cdot(1-4x+4x^2)}{(11^2-(2x)^2)}$ $= \frac{1 + 4x + 4x^{2} + 1 + 4x + 4x^{2}}{1 - 4x^{2}}$ $=\frac{g_{x}}{1-4x}$ 5(iii) $\frac{x}{36}$ $\frac{25}{36}$ $\frac{x+5}{x+6}$ $\frac{(x+5)(x-5)}{(x+6)(x-6)} \frac{x+5}{x+6}$ $= \frac{(x+5)(x-5) - (x+5)(x-6)}{(x+6)(x-6)}$ $= \frac{25}{x^2} \frac{(x^2-x+30)}{6^2}$ $= \frac{25-x^2}{x^2-6^2}$ - 1 + 1 × +5 1+5 1-36

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Plot Superone Mathematics 193 Class 9th

$$S(iv) = \frac{x}{x-y} - \frac{y}{x+y} - \frac{2xy}{x^2-y^2}$$

$$= \frac{x}{x-y} - \frac{y}{x+y} - \frac{2xy}{(x-y)(x+y)}$$

$$= \frac{x(x+y) - y(x-y) - 2xy}{(x-y)(x+y)}$$

$$= \frac{x^2 + xy - xy + y^2 - 2xy}{(x-y)(x+y)}$$

$$= \frac{x^2 + y^2 - 2xy}{(x-y)(x+y)}$$

$$= \frac{(x-y)^2}{(x-y)(x+y)}$$

$$= \frac{x-y}{x+y}$$

$$5(v) = \frac{x-2}{x^2 + 6x + 9} - \frac{x+2}{2x^2 - 18}$$

$$= \frac{x-2}{x^2 + 3x + 3x + 9} - \frac{x+2}{2(x^2 - 9)}$$

$$= \frac{x-2}{x(x+3) + 3(x+3)} - \frac{x+2}{2(x^2 - 3^2)}$$

$$= \frac{x-2}{(x+3)(x+3)} - \frac{x+2}{2(x+3)(x-3)}$$

$$= \frac{2(x-2)(x-3)}{2(x+3)(x+3)(x-3)}$$

$$= \frac{2x^2 - 10x + 12}{2(x+3)^2(x-3)}$$

$$= \frac{2x^2 - 10x + 12}{2(x+3)^2(x-3)}$$

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Pilot Superone Mathematics 194 Class 9th $= \frac{x^2 - 15x + 6}{2(x+3)(x-3)}$ $5(vi) \frac{1}{x-1} - \frac{1}{x+1} - \frac{2}{x^2+1} - \frac{4}{x^4-1}$ $= \left(\frac{1}{x-1} - \frac{1}{x+1}\right) - \left(\frac{2}{x^2+1} + \frac{4}{(x^2+1)(x^2-1)}\right)$ $= \left(\frac{x+1-x+1}{(x-1)(x+1)}\right) - \left(\frac{2}{x^2+1} + \frac{4}{(x^2+1)(x^2-1)}\right)$ $= \frac{2x}{x^2-1} - \left(\frac{2(x^2-1)+4}{(x^2+1)(x^2-1)}\right)$ $= \frac{2x}{x^2-1} - \frac{2x^2-2+4}{(x^2+1)(x^2-1)}$ $= \frac{2x}{x^2-1} - \frac{2x^2+2}{(x^2+1)(x^2-1)}$ $= \frac{2x}{x^2-1} - \frac{2(x^2+1)}{(x^2+1)(x^2-1)}$ $= \frac{2x}{x^2-1} - \frac{2(x^2+1)}{(x^2+1)(x^2-1)}$

Q.6 Perform the indicated operation and simplify

(i)
$$(x^2-49)$$
, $\frac{5x+2}{x+7}$ (ii) $\frac{4x-12}{x^2-9} + \frac{18-2x^2}{x^2+6x+9}$

(iii)
$$\frac{x^4 - y^6}{x^2 - y^2} + (x^4 + x^2y^2 + y^4)$$
 (iv) $\frac{x^2 - 1}{x^2 + 2x + 1} \cdot \frac{x + 5}{1 - x}$

Pilot Superone Mathematics 195 Class 9th $(v) = \frac{x^2 + xy}{y(x+y)}, \frac{x^2 + xy}{y(x+y)} \div \frac{x^2 - x}{xy - 2y}$

Solutions:

6(i)
$$(x^2-49)$$
. $\frac{5x+2}{x+7}$
 $(x^2-7^2) \times \frac{5x+2}{x+7}$
 $= (x-7)(x+7) \times \frac{5x+2}{x+7}$
 $= (x-7)(5x+2)$
 $= 5x^2 - 33x - 14$
6(ii) $\frac{4x-12}{x^2-9} \div \frac{18-2x^2}{x^2+6x+9}$
 $= \frac{4(x-3)}{(x-3)(x+3)} \div \frac{2(3^2-x^2)}{x(x+3)+3(x+3)}$
 $= \frac{4}{x+3} \div \frac{2(3+x)(3-x)}{(x+3)(x+3)}$
 $= \frac{4}{x+3} \div \frac{2(3-x)(3-x)}{x+3}$
 $= \frac{4}{x+3} \times \frac{2(3-x)}{x+3}$
 $= \frac{4}{x+3} \times \frac{2(3-x)}{x+3}$
 $= \frac{4}{x+3} \times \frac{2(3-x)}{x+3}$
 $= \frac{2}{3-x}$

Pilot Superone Mathematics 196 Class 9th

$$= \frac{(x^2)^3 - (y^2)^3}{x^2 - y^2} \div (x^4 + x^2y^2 + y^4)$$

$$= \frac{(x^2 - y^2)(x^4 + x^2y^2 + y^4)}{(x^2 - y^2)} \times \frac{1}{x^4 + x^2y^2 + y^4}$$

$$= 1$$

$$6(iv) \quad \frac{x^2 - 1}{x^2 + 2x + 1} \frac{x + 5}{1 - x}$$

$$= \frac{x^2 - 1^2}{x^2 + x + x + 1} \times \frac{x + 5}{-(x - 1)} \qquad \text{N.T.S}$$

$$= \frac{(x - 1)(x + 1)}{x(x + 1) + 1(x + 1)} \times \frac{-(x + 5)}{(x - 1)}$$

$$= \frac{(x + 5)}{(x + 1)(x + 1)} \times \frac{-(x + 5)}{(x - 1)}$$

$$= \frac{(x + 5)}{x + 1}$$

$$6(v) \quad \frac{x^2 + xy}{y(x + y)} \times \frac{x^2 + xy}{y(x + y)} \div \frac{x^2 - x}{x^2 - x}$$

$$= \frac{x(x + y)}{y(x + y)} \times \frac{x(x + y)}{y(x + y)} \times \frac{xy - 2y}{x^2 - x}$$

$$= \frac{x(x + y)}{y(x + y)} \times \frac{x(x + y)}{y(x + y)} \times \frac{y(x - 2)}{x(x - 1)}$$

$$= \frac{x(x - 2)}{y(x - 1)}$$

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Pilot Superone Mathematics

Algebraic Formulae

(i)
$$(a + b)^2 = a^2 + 2ab + b^2$$

$$= a^2 + 2ab + b^2$$

(ii)
$$(\mathbf{a} - \mathbf{b})$$

(ii)
$$(a-b)^2 = a^2 - 2ab + b^2$$

(iii)
$$(a+b)^2 + (a-b)^2 = 2(a^2 + b^2)$$

(iv)
$$(a+b)^2 - (a-b)^2 = 4ab$$

(v)
$$(a+b+c)^2 = a^2+b^2+c^2+2ab+2bc+2ca$$

$$= a^2 + b^2 + c^2 + 2(ab + bc + ca)$$

(vi)
$$(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3$$

$$= a^3 + b^3 + 3ab(a + b)$$

(VII)
$$(a-b)^3 = a^3 - 3a^2b + 3ab^2 - b^3$$

$$= a^3 - b^3 - 3ab(a - b)$$

(viii)
$$a^2 - b^3 = (a + b)(a^2 - ab + b^2)$$

$$= (a - b)(a^2 + ab + b^2)$$

Priot Superone Mathematics 198

Class 9th

Exercise 4.2

Q.1(i) If
$$a + b = 10$$
 and $a \cdot b = 6$, then find the value of $a^2 + b^2$

(ii) If
$$a + b = 5$$
 and $a - b = \sqrt{17}$ the find the value of ab.

1(i) If
$$a+b-10$$
 and $a-b=6$, then find the value of a^2+b^2

Solutions:

$$a + b = 10$$

Given

$$a-b=6$$

$$a^2 + b^2 = ?$$

We know that

$$2(a^2 + b^2) = (a + b)^2 + (a - b)^2$$

Putting value of a + b and a - b

$$= (10)^2 + (6)^2$$

= 100 + 36

$$2(a^2 + b^2) = 136$$

$$a^2 + b^2 = \frac{136}{2}$$

(Dividing by 2)

$$a^2 + b^2 = 68$$

I(ii) If a+b=5 and $a-b=\sqrt{17}$ the find the value of ab.

Solution:

$$a+b=5$$

Given

$$\mathbf{a} \sim \mathbf{b} = \sqrt{17}$$

We know that

$$(a + b)^2 - (a - b)^2 = 4ab$$

Putting values of a + b and a - b

$$(5)^2 - (\sqrt{17})^2 = 4ab$$

Pilot Su	perone Mathematics	199	Class 9 th
OF.	4ab = 8		
or	$ab = \frac{8}{4}$		
	ab = 2		
0.2	If $a^2 + b^2 + c^2 = 45$ and	a+b+c=-	-1, find the value
-	of ab + bc + ca		-
Solutio	$a^2 + b^2 + c^2 + 4$	5	Given
	a+b+c=1		
	ab + bc + ca = ?	•	
			+ 2(ab + bc + ca)
	Putting $a + b + c = -1$,	$a^2 + b^2 + c^2$	45
	_	15 + 2 (ab + b	
	1-45 = 2	2(ab + bc + ca	r)
	_44 = 2	2(ab + bc + ca	a)
	-22 = 8	ab + bc + ca	(Dividing by 2)
or	ab + bc + ca =	-22	
Q.3	If m + n + p = 10 and s value of m ² + n ² + p ²	nus + np + my	p = 27, find the
Solutio	-		Given
	mn+np+mp =	= 27	
	$m^2 + n^2 + p^2 =$	= ?	
	Formula		
	$(m+n+p)^2 =$	$= m^2 + n^2 + p^2$	² +2(mn + որ + <mark>m</mark> p)
	Putting mn + np + mp	= 27, m + n +	p = 10
	<u>-</u>	$= m^2 + n^2 + p^2$	
	100 =	= m ² + n ² + p	² + 54
or	$m^2 + n^2 + p^2$	= 100 – 54 ⁻	
	*	= 46	

Pilot Superone Mathematics 200 Class Q.4 If $x^2 + y^2 + z^2 = 78$ and xy + yz + zx = 59, Find the value of x + y + z $x^2 + y^2 + z^2 = 78$ Solution Given xy + yz + zx = 59x+y+z=?Formula $(x + y + z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$ Putting xy + yz + zx = 59, $x^2 + y^2 + z^2 = 78$ $(x + y + z)^2 = 78 + 2(59)$ = 78 + 118 $(x + y + z)^2 = 196$ $x + y + z = \pm \sqrt{196}$ (Taking square root) $x+y+z=\pm 14$ Q.5 If x + y + z = 12 and $x^2 + y^2 + z^2 = 64$, find the value of xy + yz + zx Solution: x+y+z=12Given $x^2 + y^2 + z^2 = 64$ xy + yz + 2x = ?Formula $(x + y + z)^2 = x^2 + y^2 + z^2 + 2(xy + yz + zx)$ Putting value of x + y + z = 12, $x^2 + y^2 + z^2 = 64$ $(12)^2 = 64 + 2(xy + yz + zx)$ 144 = 64 + 2(xy + yz + zx)144 - 64 = 2(xy + yz + zx)80 = 2(xy + yz + zx)2(xy + yz + zx) = 80Thus xy + yz + zx = 40(Dividing by 2)

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Prior Superone Mathematics 201 Class 9^{th} Q.6 If x + y = 7 and xy = 12, then find the value of $x^3 + y^3$. x + y = 7Solution: xy = 12 $x^3 + y^3 = ?$ Fourmula. $(x+y)^3 x^3 + y^3 + 3xy(x+y)$ Putting value of x + y = 7, xy = 12 $(7)^3 = x^3 + y^3 + 3(12)(7)$ $343 = x^3 + y^3 + 252$ $343 - 252 = x^3 + y^3$ $91 = x^3 + y^3$ $x^3 + v^3 = 91$ OF If 3x + 4y = 11 and xy = 12, then find the value of $27x^3 + 64y^3$. Given 3x + 4y = 11Solution: xy = 12 $27x^3 + 64y^3 = ?$ Formula $(3x + 4y)^3 = (3x)^3 + (4y)^3 + 3(3x)(4y)(3x + 4y)$ Putting \forall alue of 3x + 4y = 11, xy = 12 $(11)^3 = 27x^3 + 64y^3 + 3 \times 3 \times 4(xy)(11)$ $1331 = 27x^3 + 64y^3 + 3 \times 3 \times 4 \times 12 \times 11$ $1331 = 27x^3 + 64y^3 + 4752$ $1331 - 4752 = 27x^3 + 64y^2$ $-3421 = 27x^3 + 64y^3$ $27x^3 + 64y^3 = 3421$ Œ If x - y = 4 and xy = 21, then find the value of $x^3 - y^3$ x-y - 4 Given Solution: xy = 21

Pilot Superone Mathematics 202 Class 9th

 $(x-y)^{3} - x^{3} - y^{3} - 3xy(x-y)$ Putting value of x - y = 4, xy = 21 $(4)^{3} = x^{3} - y^{3} - 3(21)(4)$ $64 = x^{3} - y^{3} - 252$ $64 + 252 - x^{3} - y^{3}$ $316 = x^{3} - y^{3}$ $x^{3} - y^{3} = 316$

O۲

Q.9 If 5x - 6y = 13 and xy = 6, then find the value of $125x^3 - 216y^3$

Solution:

$$5x - 6y = 13$$
 Given
 $xy = 6$
 $125x^3 - 216y^3 = ?$

Formula

$$(5x-6y)^3 = (5x)^3 + (6y)^3 - 3(5x)(6y)(5x-6y)$$
Putting value of $5x \cdot 6y = 13$, $xy = 6$

$$(13)^3 = 125x^3 - 216y^3 - 3 \cdot 5 \cdot 6 + xy \cdot (13)$$

$$2197 = 125x^3 - 216y^3 - 1170 \cdot 6$$

$$2197 = 125x^3 - 216y^3 - 7020$$

$$2197 + 7020 = 125x^3 - 216y^3$$

$$9217 = 125x^3 - 216y^3$$

$$125x^3 - 216y^3 = 9217$$

OF

Q.10 If
$$x + \frac{1}{x} = 3$$
, then find the value of $x^3 + \frac{1}{x^3}$

Solution:

$$x + \frac{1}{\pi} = 3$$
Given
$$x^3 + \frac{1}{x^3} = ?$$

Formula

Pilot Superone Mathematics 203 Class 9th $\left(x + \frac{1}{x}\right)^3 = x^3 + \frac{1}{x^3} + 3(x)\left(\frac{1}{x}\right)\left(x + \frac{1}{x}\right)$

Putting value of $x + \frac{1}{x} = 3$

$$(3)^3 = x^3 + \frac{1}{x^3} + 3(3)$$

$$27 = x^3 + \frac{1}{x^3} + 9$$

$$27 - 9 = x^3 + \frac{1}{x^3}$$

$$18 = x^3 + \frac{1}{x^3}$$

ог

$$x^3 + \frac{1}{x^3} = 18$$

Q.11 If $x = \frac{1}{x} = 7$, then find the value of $x^3 = \frac{1}{x^3}$

Solution:

$$x + \frac{1}{2} = 7$$

Given

$$x^3 - \frac{1}{x^3} = ?$$

Formula

$$\left(x - \frac{1}{x}\right)^{11} = x^3 - \frac{1}{x^3} - 3(x)\left(\frac{1}{x}\right)\left(x - \frac{1}{x}\right)$$

Putting value of $x - \frac{1}{x} = 3$

$$(7)^3 = x^3 - \frac{1}{x^3} - 3(7)$$

$$343 = x^3 - \frac{1}{x^3} - 21$$

Pilot Superone Mathematics Class 9th $343 + 21 = x^3 - \frac{1}{13}$ $364 = x^3 - \frac{1}{3}$ $x^3 - \frac{1}{x^3} = 364$ OI Q.12 If $\left(3x + \frac{1}{3x}\right) = 5$, then find the value of $27x^3 + \frac{1}{27x^3}$ $3x + \frac{1}{3y} = 5$ Solution: Given $\left(3x + \frac{1}{2w}\right)^3 = (5)^3 \qquad \text{(Cubing)}$ $(3x)^3 + \left(\frac{1}{3x}\right)^2 + 3(3x)\left(\frac{1}{3x}\right)\left(3x + \frac{1}{3x}\right) = 125$ $27x^3 + \frac{1}{27x^3} + 3 \times (5) = 125$ $27x^3 + \frac{1}{22x^3} = 125 - 15$ $27x^3 + \frac{1}{27x^3} = 110$ Q.13 If $\left(5x - \frac{1}{5x}\right) = 6$, then find the value of $\left[125x^{2} - \frac{1}{125x^{2}}\right]$ $5x - \frac{1}{5x} = 6$ Solution: (Given) $\left(5x - \frac{1}{2}\right)^3 \approx (6)^3 \qquad \text{(Cubing)}$

Pilot Superone Mathematics 205 Class 9^{4x} $(5x)^{3} = \frac{1}{(5x)^{3}} - 3(5x) \left(\frac{1}{5x}\right) \left(5x - \frac{1}{5x}\right) = 216$ $125x^{3} - \frac{1}{125x^{3}} - 3(6) = 216$ $125x^{3} - \frac{1}{125x^{3}} = 216 + 18$ $125x^{3} = \frac{1}{125x^{3}} = 234$

Q.14 Factorize:

(i)
$$x^3 - y^3 - x + y$$

(ii)
$$8x^3 - \frac{1}{27y^3}$$

14(i)
$$x^3 y^3 x + y$$

Solution: $= x^3 - y^3 - (x - y)$
 $= (x - y)(x^2 + xy + y^2) - (x - y)$
 $= (x - y)[x^2 + xy + y^2 - 1]$
14(ii) $8x^3 - \frac{1}{27x^3}$

Solution:
$$= (2x)^{3} \left(\frac{1}{3y}\right)^{3}$$

$$= \left(2x - \frac{1}{3y}\right) \left[(2x)^{2} + (2x)\left(\frac{1}{3y}\right) + \left(\frac{1}{3y}\right)^{2}\right]$$

$$= \left(2x - \frac{1}{3y}\right) \left[4x^{2} + \frac{2x}{3y} + \frac{1}{9y^{2}}\right]$$

Pilot Superone Mathematics 206 Class 9th (ii)
$$(x^3 y^3)(x^6 + x^3y^3 + y^6)$$

(iii) $(x - y)(x + y)(x^2 + y^2)(x^2 + xy + y^2)(x^2 - xy + y^3)$
 $(x^4 x^2y^2 + y^4)$
(iv) $(2x^2 - 1)(2x^2 + 1)(4x^4 + 2x^2 + 1)(4x^4 - 2x^2 + 1)$
Solutions: $(x^2 - y^2)(x^4 - x^2y^2 + y^4)$
Formula $(x^2 + y^2)(x^4 - x^2y^2 + y^4)$
Formula $(x^3 + y^3)(x^6 + x^3y^3 + y^6)$
Solution: $(x^3 - y^3)(x^3 + y^3)(x^2 + xy + y^2)(x^2 - xy + y^2)$
 $(x^4 - x^2y^2 + y^4)$
Solution: $(x^3 - y^3)(x^3 + y^3)($

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Prior Superone Mathematics 207 Class 9th SURDS

An irrational radical with rational radicand is called a surd.

Hence $\sqrt{2}$, $\sqrt{3}$, $\sqrt{\frac{3}{7}}$ are surds.

Va is said if

- (i) a is rational
- (ii) the result \$\sqrt{a}\$ is irrational

e.g., $\sqrt{\pi}$ and $\sqrt{3+\sqrt{17}}$ are not suids as π and $3 = \sqrt{17}$ are not rational

In √a n is degree of the surd

 $a = \sqrt{b}$ is called conjugate of $a + \sqrt{b}$.

If we change the denominator from its surd form to rational form, then this process is rationalization

Pilot Superone Mathematics 208 Class 9*

Exercise 4.3

Q.! Express each of the following surd in the simplest form.

(i)
$$\sqrt{180}$$

(iii)
$$\frac{3}{4}\sqrt[3]{128}$$

(iv)
$$\sqrt[5]{96x^4y^7z^4}$$

$$I(i) = \sqrt{180}$$

Solution: $= \sqrt{2 \times 2 \times 3 \times 3 \times 5}$ $= \sqrt{2^2 \times 3^2 \times 5}$ $= 2 \times 3 \sqrt{5}$ $= 6\sqrt{5}$

$$I(ii) = 3\sqrt{162}$$

Solution: $= 3\sqrt{9 \times 9 \times 2}$ $= 3\sqrt{9^2 \times 2}$ $= 3 \times 9 \sqrt{2}$ $= 27\sqrt{2}$

$$I(iii) = \frac{3}{4}\sqrt{128}$$

Solution: $= \frac{3}{4}\sqrt[3]{2^3 \times 2^3 \times 2}$ $= \frac{3}{4} \times 2 \times 2 \times \sqrt[3]{2}$ $= 3\sqrt[4]{2}$ $= 3\sqrt[4]{2}$ $= 3\sqrt[4]{2}$

Pilot Superone Mathematics 209 2xyz 3/3xy2z3

Q.2 Simplify

$$0 \qquad \frac{\sqrt{18}}{\sqrt{3}\sqrt{2}}$$

(ii)
$$\frac{\sqrt{21}\sqrt{9}}{\sqrt{63}}$$

(iii)
$$\sqrt[4]{243}x^{\frac{1}{5}}y^{\frac{10}{5}}z^{\frac{1}{5}}$$
 (iv) $\sqrt[4]{125}$

$$(iv) = \frac{4}{5}\sqrt{125}$$

Solutions:

$$2(i) \qquad \frac{\sqrt{18}}{\sqrt{3}\sqrt{2}}$$

Solution:

$$\sqrt{\frac{18}{3 \times 2}}$$

$$\sqrt{\frac{3 \times 2 \times 3}{2 \times 3}} = \sqrt{3}$$

$$2(ii) \qquad \frac{\sqrt{21}\sqrt{9}}{\sqrt{63}}$$

$$\sqrt{\frac{21 \times 9}{63}}$$

$$\sqrt{\frac{21 \times 3 \times 3}{21 \times 3}} \quad \sqrt{3}$$

Solution:

MATHEM	ATICS FOR 9" CLASS	(UNIT#4)	==
	ncs 210	Class 9th	
Pilot Superone Mathema	(11.5		
Solution: $\frac{4}{5}\sqrt{5}$			
$\frac{4}{5} \times 5^{\frac{1}{3}}$			
= 4 × 5 ÷	4		
$2(u) \qquad \sqrt{21} \times \sqrt{7} \times \sqrt{3}$!	
Solution: $\sqrt{21 \times 7}$			
1(21) ² 1'	= (21) ^{2**} = 21		
0.3 Simplify by com	ıbıning similar tern	ts.	
(a) $\sqrt{45} - 3$	√20 + 4√5		
1779	$5\sqrt{27} - 3\sqrt{75} + \sqrt{30}$	Q	
(iii) √3(2√3	i+3√3)		
(1v) $2(6\sqrt{5})$	-3√5)		
$3(i)$ $\sqrt{45}$ $3\sqrt{20} + 6$	4v5		
	5 3\4×5+4\5		
$=\sqrt{3}$	$\sqrt{5} = \sqrt{2} \cdot \times 5 + 4\sqrt{5}$		
·	$3 \times 2\sqrt{5} + 4\sqrt{5}$		
	3 6 41		
-	1) 5		
$3(ii) = 4\sqrt{12} \cdot 5\sqrt{27}$	3√75 + √300 1×3 + 5√9×3 - 3√2	$\frac{1}{5 \times 3} + \sqrt{100 \times 3}$	
. Solution: 4√4	1×3+5√3'×3-3v2	5 - 3 + 10 × 3	
4√:	×3+342 ×3-3	E E	

Pilot Superone Mathematics 211

8
$$\times 3 = 15 \times 3 = 10 \times 3$$
 $\sqrt{3} \{8 + 15 = 15 \times 10\}$
 $\sqrt{3} \{18\} = 18 \times 3$

3(iii) $\sqrt{3}(2\sqrt{3} + 3\sqrt{3})$

Solution: $(\sqrt{3})(\sqrt{3})(2 + 3)$
 $3 + 5 = 15 = (\sqrt{3})^2 \{5\}$

3(iv) $2(6\sqrt{5} - 3\sqrt{5})$

Solution: $2(\sqrt{5})(6 - 3)$
 $2(\sqrt{5})(3) = 6\sqrt{5}$

Q.4 Simplify:

(i) $(3 + \sqrt{3})(3 - \sqrt{3})$ (ii) $(\sqrt{5} + \sqrt{3})^2$

(iii) $(\sqrt{5} + \sqrt{3})(\sqrt{3} + \sqrt{3})$ (iv) $(\sqrt{2} + \frac{1}{\sqrt{3}})(\sqrt{2} - \frac{1}{\sqrt{3}})$

(v) $(\sqrt{3} + \sqrt{5})(\sqrt{3} + \sqrt{3})(\sqrt{3} + \sqrt{3})(\sqrt{2} + \sqrt{3})$

4(i) $(3 + \sqrt{3})(3 - \sqrt{3})$

Solution: $(3)^2 + (\sqrt{3})^2 + (\sqrt{3})$

MATHEMATICS FOR 9^{TH} CLASS (UNIT # 4)

======================================
Prior Superone Mathematics 212 Class 9th
4(m) (v2+ 1/3) (2 (3)
Solution: $(\sqrt{2})^{-1} \frac{1}{\sqrt{3}} + \cdots$
2 3
6 1 5 3 3
$4(v) = (\sqrt{x} + \sqrt{y} + \sqrt{x} - \sqrt{y})(x + y)(x^2 + y^2)$
Solution: (xx + \forall)(xx + \forall) (8 * \forall XX + \forall)
$\left[\left(\sqrt{x}\right)^{2}-\left(\sqrt{y}\right)^{2}\right](x+y)(x^{2}+y^{2})$
$\frac{(x - y)(x + y)(x^2 + y^2)}{(x - y)(x + y)(x^2 + y^2)}$
$\frac{(x^2 - y^2)(x^2 + y^2)}{(x^2)^2 - (y^2)^2 - x^2 - y^2}$
$(x^2)^2 + (y^2)^2 + y^2 + y^2$

Rationalization of Surds Definitions

- A surd which contains a single term is caved a monormal surd.
- (ii) A surd which contains sum of two monomial surds or sum of a monomial surd and a rational number is called a binomial surd.
- (bi) The conjugate of $x + \sqrt{y}$ is $x = \sqrt{y}$

Pilot Superone Mathematics 213 Class 91

Exercise 4.4

Q.1 Rutionalize the denominator of the following:

(ii)
$$\frac{3}{4\sqrt{3}}$$
 (ii) $\frac{14}{\sqrt{98}}$ (iii) $\frac{6}{\sqrt{8}\sqrt{27}}$ (iii) $\frac{6}{\sqrt{8}\sqrt{27}}$ (iv) $\frac{1}{3+2\sqrt{5}}$ (vi) $\frac{2}{\sqrt{5}-\sqrt{5}}$ (vii) $\frac{\sqrt{3}-1}{\sqrt{3}+1}$ (viii) $\frac{\sqrt{3}+\sqrt{3}}{\sqrt{5}-\sqrt{3}}$

$$I(0) = \frac{3}{4\sqrt{3}}$$

$$I(ii) = \frac{14}{\sqrt{9}i}$$

Solution:

$$\frac{14}{\sqrt{98}} \uparrow \left(\frac{\sqrt{98}}{\sqrt{98}} \right)$$

Pilot Supero	ne Mathematics 214	Class 9th	
Solution:	$ \frac{6}{\sqrt{8}}\sqrt{27} = \sqrt{8}\sqrt{27} $ $ 6 \times \sqrt{8} \times \sqrt{27} $		()
	$\frac{6 \times \sqrt{2^3} \times 2 \times \sqrt{3^2 \times 3}}{8 \times 27}$ $6 \times 2\sqrt{2} \times 3\sqrt{3}$	Q	
	8×77 $6 \times 2 \times 3 \times 2 + \sqrt{3}$ 8×27		
	$\frac{1}{6} \times \sqrt{2} \times 3 = \frac{1}{6} \times \sqrt{6} = \frac{\sqrt{6}}{6}$	•	
I(iv) 3+	$\frac{1}{2\sqrt{5}}$		
Solution:	$ \begin{array}{c} \frac{1}{2\sqrt{5}} \times \begin{pmatrix} 3 & 2\sqrt{5} \\ 3 & 2\sqrt{5} \end{pmatrix} \\ 3 & 2\sqrt{5} \end{array} $		
	$O^{\frac{3}{3} \cdot \frac{2\sqrt{5}}{3}} = \frac{2\sqrt{5}}{3 \cdot (2\sqrt{5})}$		
٦	$\frac{3}{9} \cdot \frac{2\sqrt{5}}{20}$		
	1 11 (3 - 2√5) 15		
1(v)	15 /31 - 4 15 (\J31 + 4)		
	1 5 5 11 1 1		

Pilot Superone Mathematics 215 Class 9th 15(√31+4) $= \frac{15(\sqrt{31}+4)}{31-16}$ $\frac{15(\sqrt{31}+4)}{14} = \sqrt{31}+4$ Solution: $\frac{2}{\sqrt{5}-\sqrt{3}}\times\left(\frac{\sqrt{5}+\sqrt{3}}{\sqrt{5}+\sqrt{5}}\right)$ $\frac{2(\sqrt{5}+\sqrt{3})}{(\sqrt{5})^2-(\sqrt{8})}$ $\frac{2(\sqrt{5}+\sqrt{3})}{5\cdot 3} \cdot \sqrt{5}+\sqrt{3}$ 1(vii) $\sqrt{3} - 1$ $\frac{\sqrt{3}}{\sqrt{3}+1} \times \frac{\left(\sqrt{3}-1\right)}{\left(\sqrt{3}-1\right)}$ Solution: $(\sqrt{3}-1)$

MATHEMATICS FOR 9" CI	LASS (UNIT # 4)
-14	Class 9
Pilot Superone Mathematics 216	
$(\sqrt{3})^2 + (1) - 2\sqrt{3}(1)$	ì
3 1	į
	}
3+ <u>1-2√3</u>	}
2	,
	i
$\frac{4-2\sqrt{3}}{2}$	\
_	<u>;</u>
$\frac{2(2-\sqrt{3})}{2} + 2 - \sqrt{3}$	
2	
E E	
$I(vili) = \frac{\sqrt{5}}{\sqrt{5}}, \frac{\sqrt{3}}{\sqrt{3}}$	
• • •	i
$(\sqrt{5}+\sqrt{3}) (\sqrt{5}+\sqrt{3})$	•
Solution: $(\sqrt{5}-\sqrt{3})^{\times}(\sqrt{5}+\sqrt{3})$	
(42-44) (42-43)	ı
1 Te 123*	:
$\frac{\left(\sqrt{5}+\sqrt{3}\right)^2}{\left(\sqrt{5}\right)^2-\left(\sqrt{3}\right)^2}$;
$(\sqrt{5})^2 - (\sqrt{3})^2$	<u> </u>
	•
$(\sqrt{5})^{2} + (\sqrt{3}) + 2\sqrt{5}\sqrt{3}$	•
5-3)
	•
$5 + \frac{3+2\sqrt{15}}{2} = \frac{8+2\sqrt{15}}{2}$	1
2 2	,
2(4+4)5)	*
$\frac{2(4+\sqrt{15})}{2}$ 4+ $\sqrt{15}$	ί,
Same of the Same	†
Q.2 Find the conjugate of $x + \sqrt{y}$	_ (
$(i) \qquad 3 + \sqrt{7} \qquad (ii)$	$4 - \sqrt{5}$ $2 + \sqrt{5}$
$\sin 2 + \sqrt{3} \qquad (iv)$	2 + √5
$\min 2 + \sqrt{3} \qquad \qquad \text{(iv)}$	-

Pilot Super	one Mathematics		Class 9 th
{vii) 7 – √6	(viii) 9 + √2	
2(i) 3 +	_y '7		
Solution:	Conjugate	3 √7	
2(ii) 4 –	√5		
Solution:	Conjugate	4 + √5	
<i>2(iu)</i> 2 +	√3		
Solution:	Conjugate	2 📢	
2(iv) 2+	v5		
Solution:	Conjugate	2 v š	
2(v) 5+	$\sqrt{7}$		
Solution:	Сопјидате	5 v?	
2(vi) 4 -	√15		
Solution:	Conjugate	4 - 15	
2(vii) 7 –	\6		
Solution:	Conjugate	7 - 56	
2(viii) 9+	√2		
Solution:	Conjugate	9 √ 2	
<i>Q.3</i> (i)	If $x = 2 = \sqrt{3}$, find	1	•
(ii)	$1 f x = 4 - \sqrt{17}$, fix	nd -	
(iit)	$1f x = \sqrt{3} + 2, \text{ find}$	x+ 1	
3(i) x =	2- _V 3	•	

Victorium de virgina de la contra de la fintes de la Devers Maria Teles III de la Contra dela contra de la contra del la contra del la contra del la contra de la contra del la contra de la contra de la contra del la contra

Class 9th Pilot Superone Mathematics 218 Solution: $\{2+\sqrt{3}\}$ (2-43)(2+43) $=\frac{2+\sqrt{3}}{(2)^3-(\sqrt{3})^3}$ $=\frac{2+\sqrt{3}}{1+\sqrt{3}}=2+\sqrt{3}$ 3(ii) $x = 4 - \sqrt{17}$ 1 <u>1</u> √ 1 √17 Solution: . . . (4+√17) 4-√17 (4+√17) $\frac{4+\sqrt{17}}{(4)-(\sqrt{17})}$ 4+ √17 16 -17 $4+\sqrt{17} = -4-\sqrt{17}$ 3(iii) $x = \sqrt{1+2}$ Solution: $1 - (\sqrt{3} + 2)$

Pilot Superone Mathematics Class 9th $=\frac{\sqrt{3}-2}{2}$ $= \frac{\sqrt{3}-2}{-1} = \sqrt{3}+2$ $x = \sqrt{3} + 2$ Now $\frac{1}{8} = \sqrt{3} + 2$ Δ nd $\sqrt{3} + 2 \cdot \sqrt{3} + 2$ Simplify: 0.4 $\frac{1+\sqrt{2}}{\sqrt{5}+\sqrt{3}} + \frac{1-\sqrt{2}}{\sqrt{5}-\sqrt{3}}$ (ii) $\frac{1}{2+\sqrt{3}} + \frac{2}{\sqrt{5}-\sqrt{3}} + \frac{1}{2+\sqrt{5}}$ (11i) $\frac{2}{\sqrt{5}+\sqrt{3}}+\frac{1}{\sqrt{3}+\sqrt{5}}+\frac{3}{\sqrt{5}+\sqrt{5}}$

 $\int_{0}^{2\pi} \frac{1+\sqrt{2}}{\sqrt{5}+\sqrt{3}} + \frac{1}{\sqrt{5}} - \frac{\sqrt{2}}{\sqrt{3}}$ Solution:

$$\frac{(1+\sqrt{2})}{(\sqrt{5}+\sqrt{3})} \times \frac{(\sqrt{5}-\sqrt{3})}{(\sqrt{5}-\sqrt{3})} + \frac{1-\sqrt{2}}{\sqrt{5}} \times \frac{(\sqrt{5}+\sqrt{3})}{(\sqrt{5}+\sqrt{3})}$$

Prior Superone Mathematics 220 Class 9th $\frac{(1+\sqrt{2})(\sqrt{5}-\sqrt{3})}{(1+\sqrt{2})(\sqrt{5}+\sqrt{3})}$ $(\sqrt{5})$ $-(\sqrt{3})$ $(\sqrt{5})$ $(\sqrt{3})$ $(1+\sqrt{2})(\sqrt{5}-\sqrt{3})+(1-\sqrt{2})(\sqrt{5}+\sqrt{3})$ $\sqrt{5} - \sqrt{3} + \sqrt{2} \times 5 = \sqrt{2} \times 3 + \sqrt{5} + \sqrt{3} + \sqrt{2} \times 3 = \sqrt{2} \times 3$ $\sqrt{5} - \sqrt{3} + \sqrt{10} - \sqrt{6} + \sqrt{5} + \sqrt{3} - \sqrt{10} = \sqrt{6}$ $2\sqrt{5} - 2\sqrt{6}$ $2(\sqrt{5}, \sqrt{6})$ $\sqrt{5}, \sqrt{6}$ $\sqrt{5} \cdot \sqrt[3]{7} + \sqrt{5} + \sqrt{2} = \sqrt{5} + \sqrt{2}$ Solution: ~ $\frac{1(24\sqrt{3})}{(2\sqrt{3})(2\sqrt{3})} \frac{2(\sqrt{5}+\sqrt{3})}{(\sqrt{5}-\sqrt{3})(\sqrt{5}+\sqrt{3})} \frac{1(2\sqrt{5})}{(2+\sqrt{5})(2-\sqrt{5})}$ $\frac{2}{(2)} \frac{\sqrt{3}}{(\sqrt{3})} + \frac{2}{(\sqrt{5})} \frac{\sqrt{5}}{(\sqrt{5})} + \frac{2}{(\sqrt{5})} \frac{\sqrt{5}}{(2)} + \frac{2}{(\sqrt{5})} \frac{\sqrt{5}}{(2)}$ $\frac{2}{4} \frac{\sqrt{3}}{3} \frac{2(\sqrt{5} + \sqrt{3})}{(\sqrt{5})} + \frac{2}{(27)} \frac{\sqrt{5}}{(\sqrt{5})}$ - (3 2(45+43) 2 ds

Pilot Superone Mathematics Class 9th $\frac{2}{1} + \frac{\sqrt{3}}{2} + \frac{2(\sqrt{5} + \sqrt{3})}{2} + \frac{2 - \sqrt{5}}{-1}$ 2 13 + 15 + 13 2 + 15 4(m) $\frac{2}{\sqrt{5}+\sqrt{5}}+\frac{1}{\sqrt{5}+\sqrt{5}}-\frac{3}{\sqrt{5}+\sqrt{5}}$ **Solution:** A $\frac{2}{\sqrt{5}+\sqrt{3}}$, B $\frac{1}{\sqrt{3}+\sqrt{2}}$, C $\frac{3}{\sqrt{5}+\sqrt{5}}$ $\Lambda = \frac{2(\sqrt{5}-\sqrt{3})}{(\sqrt{5}+\sqrt{3})(\sqrt{5}-\sqrt{3})}$ $3(\sqrt{5}-\sqrt{3})$ $[\sqrt{5}]$ $[\sqrt{3}]$ $3^{\frac{2(\sqrt{5}-\sqrt{3})}{\sqrt{5}-3}}$ $\frac{2(\sqrt{5} - \sqrt{3})}{2} - \sqrt{5} - \sqrt{3}$ $\frac{1}{\sqrt{3} + \sqrt{2}}$ $\frac{1(\sqrt{3}-\sqrt{2})}{(\sqrt{3}+\sqrt{2})(\sqrt{3}-\sqrt{2})}$ $\frac{1(\sqrt{3}-\sqrt{2})}{(\sqrt{3})^2-(\sqrt{2})^2}$

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MATHEMATICS FOR 9TH CLASS (UNIT # 4)

Class 9th Pilot Superone Mathematics 222 $=\frac{\sqrt{3}-\sqrt{2}}{2}=\sqrt{3}-\sqrt{2}$ $C = \frac{3(\sqrt{5} - \sqrt{2})}{(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2})}$ $\frac{3(\sqrt{5}-\sqrt{2})}{(\sqrt{5})^{3}-(\sqrt{2})^{2}}$ $=\frac{3(\sqrt{5}-\sqrt{2})}{5-2}$ $\frac{3\left(\sqrt{5}-\sqrt{2}\right)}{3}=\sqrt{5}-\sqrt{2}$ A+B C $(\sqrt{5}-\sqrt{3})+(\sqrt{3}-\sqrt{2})-(\sqrt{5}-\sqrt{2})$ $-\sqrt{5}$ $\sqrt{3}+\sqrt{3}-\sqrt{2}-\sqrt{5}+\sqrt{2}$ Q.5. (i) If $x = 2 + \sqrt{3}$, then find the value of x $\left(x-\frac{1}{x}\right)^{2}$ (ii) If $x = \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5} + \sqrt{2}}$, then find the value of $x + \frac{1}{x}$, $x + \frac{1}{x^2}$, and $x^2 + \frac{1}{x^2}$

Pilot Superone Mathematics 223 5(i) If $x = 2 + \sqrt{3}$, then find the value of $x = \frac{1}{2}$ and $\left(\begin{array}{c} \frac{1}{2} \end{array} \right)$ Solution: 1(2 √3) $(2+\sqrt{3})(2-\sqrt{3})$ $\frac{2-\sqrt{3}}{(2)^2-(\sqrt{3})^2}$ $-\frac{2\sqrt{3}}{4-3}=2\sqrt{3}$ Now Thus $\left(x - \frac{1}{x}\right)^2 = (2\sqrt{3})^2$ (Squaring) 4 + 3 - 12 If $x = \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5} + \sqrt{5}}$, then find the value of $x + \frac{1}{\sqrt{5}} = \frac{1}{\sqrt{5}}$ and $x' + \frac{1}{x}$ $x = \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5} + \sqrt{5}}$ Solution:

Class 9" Pilot Superone Mathematics 224 $\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}}$ $x = \frac{1}{\sqrt{5}} = \frac{\sqrt{5}}{\sqrt{5}} + \frac{\sqrt{5}}{\sqrt{5}} + \frac{\sqrt{5}}{\sqrt{5}} = \frac{\sqrt{5}}{\sqrt{5}}$ Now $(\sqrt{5} - \sqrt{2})^{2} + (\sqrt{5} + \sqrt{2})^{2}$ $(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2})$ $5+2-2\sqrt{5\times2}+5+2+2\sqrt{5\times2}$ (v5) -(J2) $\frac{7 - 2\sqrt{10} + 7 + 2\sqrt{10}}{5 - 2}$ $\frac{14}{5-2} - \frac{14}{3}$ $x^4 + \frac{1}{x^2} = 9$ $x + \frac{1}{x^2} = ?$ [x+1] - [14)

Pilot Superone Mathematics 225

$$x^{3} + \frac{1}{x^{3}} + 3x \times \frac{1}{x} \left(x + \frac{1}{x}\right) = \frac{2744}{27}$$
 $x^{3} + \frac{1}{x^{3}} + 3\left(\frac{14}{3}\right) = \frac{2744}{27}$
 $x^{3} + \frac{1}{x^{3}} + 14 = \frac{2744}{27}$
 $x^{3} + \frac{1}{x^{3}} = \frac{2744}{27} = \frac{2744}{27}$
 $x^{4} + \frac{1}{x^{3}} = \frac{2744}{27} = \frac{2744}{27}$

Q.6 Determine the rational number a and b if

$$\frac{\sqrt{3}-1}{\sqrt{3}+1} + \frac{\sqrt{3}+1}{\sqrt{3}-1} = a + b\sqrt{3}$$

$$\frac{\sqrt{3}-1}{\sqrt{3}+1} + \frac{\sqrt{3}+1}{\sqrt{3}-1} = a + b\sqrt{3}$$

$$\frac{(\sqrt{3}-1)(\sqrt{3}-1) + (\sqrt{3}+1)(\sqrt{3}+1)}{(\sqrt{3}+1)(\sqrt{3}-1)} = a + b\sqrt{3}$$

$$\frac{(\sqrt{3}-1)^2 + (\sqrt{3}+1)^2}{(\sqrt{3})^2 - (1)^2} = a + b\sqrt{3}$$

$$\frac{(3+1-2\sqrt{3})+3+1+2\sqrt{3}}{3+1} = a + b\sqrt{3}$$

$$\frac{8}{2} = a + b\sqrt{3}$$

$$\Rightarrow + + (0)\sqrt{3} = a + b\sqrt{3}$$

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Pilo. Superone Mathematics 237



Factorize:

ţ

 $l(v_i)$

I(vi)

FACTORIZATION

The process of writing a polynomial as a product of two or more than two polynomials is called factorization Every new polynomial is called a factor of the given polynomal

For example $\ln ab + bc + h(a + c) + b(a + c)$ is the factorization of ab + bc and bc (a + c) are its factors.

Exercise 5.1

```
Q.I.
        (i) 2obc - Juby + 2abd
        (it) 9xy - 12x^2y + 18y^2
                 3x^2y - 3x + 9xy^2
        (cis)
        (iv) 5ab<sup>2</sup>c<sup>3</sup> 10a<sup>2</sup>b<sup>3</sup>c 20a<sup>3</sup>bc<sup>2</sup>
                3x^{3}y(x - 3y) = 7x^{2}y^{2}(x - 3y)
        (v)
                2xy^2(r^2+3)+3xy^2(x^2+5)
        (vi)
Solutions -
            2abc Jahx 2abd
I(0)
          2ab(c - 2x + d)
            9xy - (2x^2y + 18y^2)
I(II)
        -3y(3x-1x^2+6y)
             3x^2y - 3x + 9xy^2
i(eu)
          -3x(xy+1-3y^2)
          3ab2c3 10a2b3c - 20u3bc2
Hir)
          Subothe 2ab 4a'e)
          3x'ver 3y, "ryin 3y)
```

x'yte 391 (3x 79)

2xy (x2 + 5)(1 + 4)

 $2xy^3(x^2+5)+8xy^2(x^2+5)$

Class 9th Pilot Superone Mathematics. 238 Factorize: 0.2. (i) 5ax 3ay 5bx + 3by(ii) $3xy + 2y + l^2x + 8$ (iii) $x^3 + 3xy^2 + 2x^2y + 6x^3$ (iv) $(x^2 - y^2)z + ty^2 - z^2/x$ Solution:-5au 3ay 3bx · 3hy 2(1) (5ax - 3ay) (5bx - 3by)4(3x - 3y) bisx 3x) (5x 3y)(a b) 3xy + 2y - 12x - 82(ii) (3xy + 2y, (12x - 8))

$$y(3x + 2) = 4(3x + 2)$$

$$(3x - 2)(1) = 4y$$

$$2(iii) = x^3 + 3xy^2 - 2x^2y - 6y^3$$

$$(x^3 + 3xy^2) - (2x^2y + 6y^3)$$

$$x(x^2 + 3y^2) - 2y(x^2 + 3y^2)$$

$$(x^3 + 3y^2)(x - 2y)$$

$$2(6v) \qquad (x^2 - y^2)z + (y^2 - z^2)x
= 2z^2 - y^2z + y^2x - z^2x
= x^2z + y^2 - z^2x + y^2z
= x(xz + y^2) - z(xz + y^2)
(xz - y^2) (x - z)$$

(i)
$$144a^2 + 24a + 1$$

 $a^2 - b^2$

(ii)
$$\frac{a^2}{b^2} = 2 + \frac{b^2}{a^2}$$

(iii)
$$(x + y)^2 - 14z(x + y) + 49z^2$$

 $Av(x^{2} - y^{2}) (x - 2y)$ $(x^{2} - y^{2})z + (y^{2} - z^{2})$ $(x^{2} - y^{2})z + y^{2}x - z^{2}x$ $(x^{2} + xy^{2} - z^{2}x - y^{2})z$ $(x^{2} + y^{2})z(x^{2} + y^{2})z(x^{2} + y^{2})$ $(x^{2} - y^{2})(x - z)$ $(x^{$

Filed Superone Mathematics 239

(144d + 12a, + (12a + 1)
12a(12a + 1) + 1(12a + 1)
(12a + 1) (12a + 1) - (12a + 1)^2

3(ii)
$$\frac{a}{b^2} = 2 \cdot \frac{b^2}{a^2}$$
 $\left(\frac{a}{b}\right)^2 - 2\left(\frac{a}{b}\right)\left(\frac{b}{a}\right) + \left(\frac{b}{a}\right)^2$
 $\left(\frac{a}{b}\right)^2 - 2 \cdot \frac{b^2}{a^2}$
 $\left(\frac{a}{b}\right)^2 - 2 \cdot \frac{b^2}{a^2}$
 $\left(\frac{a}{b}\right)^2 - \frac{b}{b} \times \frac{b}{a} + \frac{b}{a^2}$
 $\left(\frac{a^2}{b^2} - \frac{a}{b} \times \frac{b}{a}\right) - \left(\frac{a}{b} \times \frac{b}{a} + \frac{b^2}{a^2}\right)$
 $\left(\frac{a^2}{b^2} - \frac{a}{b} \times \frac{b}{a}\right) - \left(\frac{a}{b} \times \frac{b}{a} + \frac{b^2}{a^2}\right)$
 $\left(\frac{a}{b}\right)^2 - \frac{a}{b} \times \frac{b}{a} - \frac{b}{a}$
 $\left(\frac{a}{b}\right)^2 - \frac{b}{a} \times \frac{b}{a} + \frac{b}{a} \times \frac{b}{a}$
 $\left(\frac{a}{b}\right)^2 - \frac{b}{a} \times \frac{b$

MATHEMATICS FOR 9TH CLASS (UNIT # 5)

□ate ♥ʰ

Pilot Superone Mathematics 240 Gais Y

3(2x 3)²

Q.4. Factorine:
(i)
$$3x^2 - 75y^2$$
 (ii) $x(x + 1) - y(y + 1)$
(iii) $-128^{mn^2} - 242^{mn^2}$ (iv) $3x - 143x^3$

Solution:-

4(a) $3x^2 - 75y^2$
 $3(x)^2 - 25y^2$
 $3(x)^2 - 2$

www.dr.

Factorize:
(0
$$x^2 + y^2 + 6y + 9 = (40) + x^2 + x^2 + 2u + 1 = (40) + 4x^2 + y^2 + 2y + 1 = (4v) + x^2 + y^2 + 4x + 2v + 4x^2 = (4v) + x^2 + y^2 + 4x^2 + 4x^2 = (4v) + x^2 + y^2 + 4x^2 + 4x^2 = (4v) + ($$

Filot Superone Mathematics 241 Class 9th

Solutions:-

$$5(i) \qquad x^{2} - y^{2} - 6y + 9$$

$$= x^{2} - 6y^{2} + 6y + 9$$

$$= (x)^{2} - [y^{2} + 3y + 3y + 9]$$

$$= (x)^{2} - [y^{2} + 3y + 3(y + 3)]$$

$$= (x)^{2} - (y + 3) + 3(y + 3)$$

$$= (x)^{2} - (y + 3)^{2} + (x + 3)^{2}$$

$$= [x + (y + 3)] [x - (y + 3)]$$

$$5(ii) \qquad x^{2} - x^{2} + 2x - 1$$

$$= (x)^{2} - [x^{2} - 2x + 1]$$

$$= (x)^{2} - [x^{2} - 2x + 1]$$

$$= (x)^{2} - [x^{2} - 1 + (x - 1)]$$

$$= (x)^{2} - [x - 1]^{2}$$

$$(x + x - 1) - (x - x + 1)$$

$$5(iii) \qquad 4x^{2} - y^{2} - 2y - 1$$

$$(2x)^{2} - 6y^{2} + 2y + 1$$

$$= (2x)^{2} - [y^{2} + y + y + 1]$$

$$= (2x)^{2} - [y^{2} + y + y + 1]$$

$$= (2x)^{2} - (y + 1) - (y + 1)$$

$$= (2x)^{2} - (y + 1) - (y + 1)$$

$$= (2x)^{2} - (y + 1)^{2} - (2x + y + 1) - (2x + y + 1) - (2x + y + 1)$$

$$= (2x)^{2} - (y + 1)^{2} - (2x + y + 1) - ($$

MATHEMATICS FOR 9TH CLASS (UNIT # 5)

Pilot Superone Mathematics 242 $= (x - 2)^2 - (y - 1)^2$ = (x + y + 1)(x + 2 + y - 1)= (x + y - 1)(x + y - 3) $25x^2 - 10x + 1 - 36x^2$ 5(1) $(25x^2 - 10x + 1) - (36x^2)$ $= [25x^{2} 5x 5x + 1] - (6t)^{2}$ $-[5x(5x-1)-1(5x-1)]-(6x)^2$ $= (5x - 1)(5x - 1) \cdot (6z)^2$ $= (5x - I)^2 - (6z)^2$ = (5x - 1 + 6z) (5x - 1 - 6z) $x^2 - y^2 - 4xz^2 + 4z^2$ 5(vi) $= (x^2 - 4xz + 4z^2) - (y^2)$ $-[x^2 - 2xx - 2xx + 4x^2] - (y)^2$ $= [x(x-2z) - 2z(x-2z)] - y^2$ $= (x - 2z)(x - 2z) \cdot y^{t}$ $=(x-2z)^2 \times (y)^2$ = (x - 2z + y) (x - 2z - y)

with doi.

= (x + y - 2y) (x - y - 2z)

Pilot Superone Mathematics

Exercise 5.2

Q.1. Factorize:

(i)
$$x^4 + \frac{1}{x^7} - 3$$
 (ii) $3x^4 + 12y^4$
(iii) $a^3 + 3a^2b^3 + 4b^4$ (iv) $4x^4 + 81$
(v) $x^4 + x^2 + 25$ (vi) $x^4 + 4x^2 + 16$

$$(ii) \qquad 3x^4 + 12y^4$$

$$(h) = 4x^4 + 81$$

Solutions:

$$I(i) \qquad x^{i} + \frac{1}{x^{2}} - 2 - 1$$

$$= \left[(x^{2})^{2} - 2 + \left(\frac{1}{x^{2}} \right)^{2} \right] + \left[(x^{2} - \frac{1}{x^{2}} + 1) \left(x^{2} - \frac{1}{x^{2}} - 1 \right) \right]$$

$$= \left(x^{2} - \frac{1}{x^{2}} + 1 \right) \left(x^{2} - \frac{1}{x^{2}} - 1 \right)$$

$$= \left(x^{2} - \frac{1}{x^{2}} + 1 \right) \left(x^{2} - \frac{1}{x^{2}} - 1 \right)$$

$$= 3(x^{3} + 12)^{4}$$

$$= 3(x^{3} + 4y^{4})$$
Completing the square
$$= 3\{(x^{2})^{2} + (2y^{2})^{2} + 4x^{2}y^{2} - 4x^{2}y^{2}\}$$

$$= 3\{(x^{2})^{2} + (2x^{2})(2y^{2}) + (2y^{2})^{2}\} - (2xy)^{2}\}$$

$$= 3\{(x^{2})^{2} + 2(x^{2})(2y^{2}) + (2y^{2})^{2}\} - (2xy)^{2}\}$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

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$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

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$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

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$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} - 2xy)$$

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$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} + 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2y^{2} + 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2xy)$$

$$= 3(x^{2} + 2y^{2} + 2xy)(x^{2} + 2xy)(x^{2} + 2xy)$$

$$= 3(x^{2}$$

Website www.downloadclassmotes.com , E-mail raoshahzadlftikhar@omail.com

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(1(h))
$$4x^4 + 81$$

Completing the square

 $= (2x^2)^2 + (9)^2 + 2(2x^2)(9) - 36x^2$
 $= (2x^2 + 9 - 6x)(2x^2 + 9 - 6x)$
 $= (2x^2 + 9 - 6x)(2x^2 + 9 - 6x)$
 $= (2x^2 + 6x + 9)(2x^2 + 6x + 9)$

I(v) $x^4 + x^2 + 25$

Completing the square

 $(x^2)^2 + (5)^2 + 2(x^2)(5) - 9x^2$
 $= (x^2 + 5)^2 + (3x^2)$
 $= (x^2 + 5)^2 + (3x^2 + 5 - 3x)$
 $= (x^2 + 3x + 5)(x^2 + 3 - 3x + 5)$

I(vi) $x^4 + 4x^2 + 16$
 $= (x^2)^2 + (4)^2 + 2(x^2)(4) - 4x^2$

Completing the square

 $= (x^2)^2 + (4)^2 + 2(x^2)(4) - 4x^2$
 $= (x^2 + 4)^2 - (2x)^2$
 $= (x^2 + 4 + 2x, (x^2 + 4 - 2x))$
 $= (x^2 + 4 + 2x, (x^2 + 4 - 2x))$
 $= (x^2 + 2x + 4)(x^2 - 2x + 4)$

Q.2. Factorize:

(i) $x^2 + 14x + 48$

(iii) $x^2 - 21x + 108$
 $= x^2 + 8x + 6x + 48$
 $= x(x + 8) + 6(x + 8)$
 $= (x + 8)(x + 6)$

2(ii) $x^2 - 21x + 108$
 $= x(x + 8) + 6(x + 8)$
 $= (x + 8)(x + 6)$

2(iii) $x^2 - 21x + 108$
 $= x(x - 12)(x - 9)$

2(iii) $x^2 - 11x - 42$

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$$= x^2 - 1/x + 42$$
 $= x^3 - 1/4x + 3x - 42$
 $= x(x - 1/4) + 3(x - 1/4)$
 $= (x - 1/4) + 3(x - 1/4)$
 $= (x - 1/4) (x + 3)$
 $2(br) - x^2 + x - 1/32$
 $= x^2 + 1/2x - 1/3x - 1/32$
 $= x(x + 1/2) - 1/3(x - 1/2)$
 $= (x + 1/2) - 1/3(x - 1/2)$

Solutions:

 $= (x + 1/2) - 1/3(x + 1/2)$
 $= (x + 1/2) - 1/3(x + 1/2$

= (5x - 2l)(x + 1)

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$$3(v) = 4x^2 - 17xy + 4y^2$$
 $= 4x^2 - 16xy - xy + 4y^2$
 $= 4x(x - 4y) - (y(x - 4))$
 $= (x - 4y) - (x - y)$
 $3(vk) = 3x^2 - 38xy - 13y^2$
 $= 3x + xy - 3yy - 13y^2$
 $= (3x + y) - (x - 13y)$
 $3(vil) = 5x^2 - 35xy - 2xy - 14y^2$
 $= 5x^2 - y - (x - 2y) - (x - 2y)$
 $3(vili) = (5x - \frac{1}{x})^2 + 4(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + (5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + (5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 4$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 2(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 2(5x - \frac{1}{x}) + 3(5x - \frac{1}{x}) + 3$
 $= (5x - \frac{1}{x})^2 + 3(5x - \frac{1}{x}) + 3(5x$

4(1)
$$(x^2 - 5x + 4) (x^2 + 5x + 6) - 3$$

Let $-x^2 - 5x = y$
 $-(x^2 + 5x + 4) (x^2 + 5x + 6) - 3$

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= 0 + 4 0 + 6) 3		
$-y^2 + 10y + 24 - 3$		
$= y^2 - 10y + 21$		
$= y^2 + 7y + 3y + 21$		
= 10 + 7) + 3(5 + 7)		
= (y + 7) (y + 3)		
Putting $y = x^2 + 5$		
$= (x^2 + 5x + 7)(x^2 + 5x^2 $	8x + 3,	
$4(ii)$ $(x^2-4x)(x^2-4x)$	1) 20	
Let $x^1 + 4x = y$		
$(x^2 - 4x) (x^2 - 4x)$	1) - 20	(given expression)
- (1) (1) 20		
$= y^2 - y - 20$		
$= y^2 - 5y + 4y - 20$		
<i> y(y − 5) + 4(y − 5)</i> Putting y x ² 4x		
$= (x^2 + 4x - 5)(x^2 + 4x$		
$= (x^{2} + 5x + x + 5)/(x^{2})$		
x = (x(x - 5) + 1(x - 5))	2x - 2x + 4f	
(x - 5) (x + 1) (x - 2)	x(x - 2) 2(x	2)/
= (x 5) (x + 1) (x - 2)	, 2)	
4(iii) $(x + 2)(x + 3)(x + 3)$		•
Here $2+5=3+4$	マ) (ページ) 1.	,
(x + 2)(x + 5)(x + 5)	1) (x + 1) 1°	f
$= (x^2 + 7x + 10)(x^2 + 7)$	x + 121 - 15	,
Let $x^2 + 7x = y$		
$(x^2 + 7x + 10) (x^2 +$	7x + 121 - 13	· ·
= 0' + 10) (y + 12) 15		
$= y^2 + 22y + 120 - 15$		
-y' + 22y + 105		
$= y^2 + 15y + 7y + 105$		
$= y(y + 15) + 7(y + 15)^{4}$	•	
- (v + 15) (v + 7)		



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Puttung
$$y = x^2 + 7x$$

= $(x^2 + 7x + 15)(x^2 + 7x + 7)$

4(iv) $(x + 4)(x - 5, (x + 6)(x - 7) - 504$

Here $+4 - 5 = 6 - 7$
 $(x^2 - x - 20)(x^2 - x - 42) - 504$

Let $-x^2 - x = y$
 $(x^2 - x - 20)(x^2 - x - 42) - 504$ (given expression)

= $(y - 20)(y - 42) - 504$

= $y^2 - 62y + 336$

= $y^2 - 62y + 336$

= $y^2 - 56y - 6y + 316$

= $y(y - 56)(y - 6)$

Putting $y = x^2 - x$

= $(x^2 - x - 56)(x^2 - x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 + 6 + 5x)(3x + 3x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 8x + 2x - 6)$

= $(x^2 - 8x + 7x - 56)(x^2 - 8x$

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Q.5. Factorize:

(1)
$$x^3 + 48x - 12x^2 - 64$$

(4)
$$8x^3 + 60x^2 + 150x + 125$$

(iii)
$$x^3 18x^7 + 108x 216$$

(iv)
$$8x^3 - 125y^3 - 60x^3y + 150xy^2$$

Solutions:-

$$5(i) x^3 + 48x 12x^2 64$$

$$= x^3 - 64 - 12x^3 + 48x$$

$$+ (x)^3 - (4)^3 - 3(x^3)(4) + 3(x)(4^2)$$

$$= (x - 4)^3 [(a - b)^3 = a^3 - 3a^2b + 3ab^2 \cdot b^3] (Formula)$$

$$5(ii) = 8x^{3} + 60x^{2} + 150x + 125$$

$$= 8x^{3} + 125 + 60x^{2} + 150x$$

$$= (2x)^{3} + (5)^{3} + 3(2x)^{2}(5) + 3(2x)(5)^{2}$$

$$= (2x + 5)^{3}$$

$$5(iii) x3 18x2 + 108x 216$$

$$= x3 216 - 18x2 + 108x$$

$$= (x)3 - (6)3 3(x)2(6) + 3(x)(6)2$$

$$= (x - 6)3$$

$$5(1v) = 8x^{3} - 125y^{3} - 60x^{2}y + 150xy^{2}$$
$$= (2x)^{3} - (5y)^{3} - 3(2x)^{2}(5y) + 3(2x)(5y)^{2}$$
$$= (2x - 5y)^{3}$$

Factorize:

(i)
$$27 + 8x^3$$

(i)
$$27 + 8x^3$$
 (ii) $125x^2 - 216y^3$ (iii) $64x^3 + 27y^3$ (iv) $8x^3 + 125y^3$

(iii)
$$64x^3 + 27y^3$$

$$(iv) = 8x^3 + 125y^3$$

Solutions:-

$$6(i) 27 + 8x^3$$

$$= (3)^3 + (2x)^3$$

$$a^3 + b^3 = (a + b)(a^2 - ab + b^2) (Formula)$$

$$= (3 + 2x) ((3)^2 - (3)(2x) + (2x)^2)$$

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Pilot Superone Mathematics 250 $= (3 + 2x)(9 - 6x + 4x^2)$ $125x^2 - 216y^3$ 6(ii) $a^{3} = (a - b)(a^{2} + ab + b^{2})$ (Formula) $(5x)^3$ $(6y)^3$ $(5x - 6y) [(5x)^2 + (5x)(6y) + (6y)^2]$ $= (5x - 6y)(25x^2 + 30xy + 36y^2)$ $64x^3 + 27y^3$ 6(ill) $(4x)^3 + (3y)^3$ $a^{1} + b^{1} = (a + b)(a^{2} - ab + b^{2})$ $= (4x + 3y)[(4x)^2 - (4x)(3y) + (3y)^2]$ $(4x + 3y)(16x^2 + 12xy + 9y^2)$ $8x^3 + 125y^3$ 6liv) $= (2x)^3 + (5y)^4$ $a^3 + b^3 = (a + b)(a^2 + ab + b^2)$ (Formula) $-(2x + 5y)[(2x)^2 - (2x)(5y) + (5y)^2]$ $(2x + 5y)(4x^2 - 10xy + 25y^2)$

Remainder Theorem

If a polynomial p(x) is divided by a linear divisor $(x \mid a)$ then the remainder is p(a)

remander.

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Exercise 5.3

Use the remainder theorem to find the remainder 0.1. when

(4)
$$3x^{1} + 10x^{2} + 13x = 6$$

is divided by (x-2)

(ii)
$$4x^3 - 4x - 3$$

is divided by (2x + i)

(iii)
$$6x^4 + 2x^3 - x + 2$$

is divided by (x + 2)

(iv)
$$(2x - 1)^3 + 6(3 + 4x)^3 - 10$$
 is divided by $(2x+1)$

(v)
$$x^2 - 3x^2 + 4x - 14$$

is divided by (x+2)

Solutions:-

$$P(x_j = 3x^2 - 10x^2 + 13x - 6)$$
From $x = 2$, $x \cdot 2 = 0$

$$P(2) = 3(2)^3 - 10(2)^2 + 13(2) - 6$$

$$= 24 - 40 + 26 - 6$$

$$= 4(R)$$

$$I(ii)$$
 $p(x) = 4x^3 - 4x + 3$

From
$$2x - 3 = 0$$
 $x = \frac{1}{2}$

$$p(\frac{1}{2}) = 4(\frac{1}{2})^3 \cdot 4(\frac{1}{2}) + 3$$

$$4 \times \frac{1}{8} = 2 + 3$$

$$= \frac{1}{2} - 2 + 3 = \frac{1}{2} + 1 = \frac{3}{2}$$

$$p(x) = 64x^4 + 2x^3 - x + 2$$

From
$$x + 2 = 0$$
 x 2

$$p(-2) = 6(-2)^{4} + 2(-2)^{3} - (-2) + 2$$

$$6(16) + 2(-8) + 2 + 2$$

$$= 96 - 16 + 2 + 2$$

$$p(x) = (2x-1)^3 + 6(3+4x)^2 - 10$$

From
$$2x + 1 = 0$$
, $x = -\frac{1}{2}$

 $p(-\frac{1}{2}) - \left[2(-\frac{1}{2}) - 1\right]^3 + 6\left[3 + 4(-\frac{1}{2})\right]^2 - 10$ 1 Pilot Superone Mathematics 253 $-[-1-1]^3+6[3-2]^2-10$ # (-213 + 6(112 - 10 = 8+6-10 - 12 (R) I(y) $p(x) = x^3 - 3x^3 + 4x - 14$ From x + 2 = 0, x = -2 $p(-2)=(-2)^3-3(-2)^2+4(-2)-14$ --8-12 8-14 = -42(R)Q.2. (1) If (x + 2) is a factor of $3x^2 - 4kx - 4k^2$ then find the value (s) of k (iii) If (x-1) is a factor of $x^2 - kx^2 + 1/x - 6$, then find

Solutions:-

the value of &

$$p(x) = 3x^{2} - 4kx - 4k^{2}$$
From $x + 2 = 0, x = -2$

$$p(-2) = 3(-2)^{2} - 4k(-2) - 4k^{2}$$

$$+ 3(4) + 8k - 4k^{2}$$

$$+ 12 + 8k - 4k^{2}(R)$$

From
$$x + 2 = 0, x = -2$$

 $p(-2) = 3(-2)^2 + 4k(-2) + 4k$
 $+ 3(4) + 8k + 4k^2$
 $+ 12 + 8k + 4k^2 = 0$ divided by 4^+
 $- 12 + 8k + 4k^2 = 0$ divided by 4^+
 $- 3 + 2k + k^2 = 0$
 $- 3 + 3k - k - k^2 = 0$
 $- 3(1 + k) - k(1 + k) = 0$
 $- (1 + k)(3 - k) = 0$
From $- 1 + k = 0$
 $- k = -1$
and $- 3 + k = 0$
give $- k = 3$
 $- k = 3, -1$

From
$$j+k=0$$

$$k = -1$$
and
$$3 \quad k = 0$$

$$k = 3$$

k = 3, -1

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                  p(x) = x^3 \cdot kx^2 + 11x - 6
                    From x - 1 = 0 x = 1
                   p(1) = (1)^3 - k(1)^2 + 11(1) = 6
                        -1 k+11-6
                        =6-k (R)
                If x - 1 is factor, then R = 0
                From
                 \delta \cdot k = 0
                     k = 6
                Without actual long division determine whether
        Q.3.
        (i)
               (x - 2) and (x - 3) are factors of p(x) = x^3 - 12x^2 + 44 - 48
               (x-2), (x+3) and (x-4) are factors of q(x) = x^3 + 2x^2 - 5x - 6
1
        100
                         p(x) = x^2 - 12x^2 + 44x \cdot 48
        3(1)
                       x = 2 = 0, x = 2
                         p(2) = (2)^3 - 12(2)^2 + 44(2) - 48
                               = 8 - 48 + 88 48
                              = 96 \cdot 96 = 0 (R)
               R = 0 therefore, x - 2 is a factor of the polynomial
                         p(x) = x^3 - 12x^2 + 44x - 48
               From (x-3), x=3, x=3=0
                         p(3) = (3)^3 - 12(3)^2 + 44(3) 48
                              = 27 - 108 + 132 48
                           R = 159 \cdot 156 = 3 \neq 0
               R = 0, therefore, x = 3 is NOT factor
                         p(x) = x^{2} + 2x^{3} - 5x = 6
       \mathbf{v}
               From
                       x = 0, x = 2
                        p(2) = (2)^3 + 2(2)^2 - 5(2) - 6
                              = 8 + 8 - 10 - 6
                              = 16 - 16 = 0 (R)
                           R = 0, therefore, x = 2 is factor
                        p(x) = x^3 + 2x^2 - 5x - 6
                       x + 3 = 0, x = -3
               from
```

Pilot Superone Mathematics 254 $p(-3) = (-3)^3 + 2(-3)^2 - 5(-3) - 6$ = -27 + 18 + 15 - 6= 33 - 33 = 0 (R) R = 0.x + 3 is factor $p(x) = x^3 + 2x^2 - 5x - 6$ From (x + 4) = 0: x + 4 $p(4) = (4)^3 + 2(4)^2 - 5(4) - 6$ = 64 + 32 20 6 $= 96 + 26 \neq 0$ (R)

 $R \neq \theta$, therefore, x 4 is not factor

Q.4. For what value of m is the polynomial $p(x) = 4x^3 - 7x^2 + 6x - 3m$ exactly divisible by x + 2?

Solution:-

$$p(x) = 4x^{3} - 7x^{2} + 6x - 3m$$
From $x + 2 = 0$, $x = -2$

$$p(-2) = 4(-2)^{3} - 7(-2)^{2} + 6(-2) - 3m$$

$$= -32 - 28 - 12 - 3m$$

$$= -72 - 3m - (R)$$

If x + 2 is factor then R = 0

$$. -72 -3m = 0$$

or $24 + m = 0$
thus $m = -24$

Q.5. Determine the value of k if $p(x) = kx^3 + 4x^2 + 3x - 4$ and $q(x) = x^3 - 4x + k$ leaves the same remainder when divided by (x-3).

$$p(x) = kx^{3} + 4x^{2} + 3x - 4$$
From $x - 3 = 0$, $x = 3$

$$p(3) = k(3)^{3} + 4(3)^{2} + 3(3) - 4$$

$$27k + 36 + 9 - 4$$

$$= 27k + 41 - (R)$$
Now $q(x) = x^{3} - 4x + k$
and $q(3) = (3)^{3} - 4(3) + k$

	Files Superone Mathematics	255 Class 9*
•	= 27 - 12	
i	= 15 + k	(Ry
	Now $R_I = R_2$	
'	2/k + 4l = 15 + k	
	$27k \cdot k = 15 \cdot 41$	
	$ \begin{array}{ccc} 26k & - & 26 \\ \text{thus} & k & = -I \end{array} $	
	, -, -, -, -, -, -, -, -, -, -, -, -,	
	Q.6. The remainder after $n(x) = \frac{1}{2} \cdot n(x^2 - x^2)$	f dividing the polynomial
1	value of a and but	(x + 1) is 2b. Calculate the
i	ranginder of the st	this expression leaves a
i	Solution:	being divided by (x 2).
•	$p(\mathbf{x}) = \mathbf{x}^1 + \alpha \mathbf{x}^2$	
	From $x+1=0$; $x=$	'
[$p(-1) = (-1)^3 + 1$	
1	= -J + n +	•
1	= a + 6	, ,
i	a+6 -2b	(1 st Condition)
	Now $p(x) = x^3 + \alpha x^2$	+ 7
	From $(\pi-2) = 0$, $x = 2$	•
ı	and $p(2) \sim (2)^3 + a(2)^3$	2) ² + 7
	= 8 + 4a +	7
į	4a + 15	
'	4a + 15 = b + 5	(2°4 Condition)
	4a-b $3-13$	
1	4a b = -10	(B)
	a - 2b = 6	(i) From A B
i	8a - 2b × 20	(ii) mult.plying B by 2
-	7a = -14	subtracting (i) from (ii)
	$a = \frac{14}{7}$	
1	a = 2	
	a-2b = -6	From A
ì		

Pilot Superope Mathematics 256 (lass 9**)
$$-2-2b = -6 (Putting $a = -6$)
$$-2b = -6 + 2$$

$$2b = -4$$

$$b = 2$$
Thus $a = -2, b = 2$$$

Q.7. The polynomial $x^3+ix^2+mx+24$ has a factor (x+4)and it leaves a remainder of 36 when divided by (x-2). Find the values of l and m.

Solution:-

From
$$x + 4 = 0$$
, $x = -4$
 $p(-4) = (-4)^3 + 1(-4)^2 + m(-4) + 24$
 $= -6i + 16l - 4m + 24$
 $= +16l - 4m + 40$
161 $4m - 40 = 0$ (1" Condition)
or $4l - m = 10$ (A)
Now $p(x) = x^3 + 1x^3 + mx + 24$
From $x = 2 = 0$, $x = 2$
 $p(2) = (2)^3 + 1(2)^2 + m(2) + 24$
 $= 8 + 4l + 2m + 24$
 $= 4l + 2m + 32$
or $4l + 2m = 36 - 32$
or $4l + 2m = 36$
or $4l + 2m = 4$
or $2l + m = 2$ (B)
 $4l - m = 10$
 $6l = 12$ From $A + B$
 $l = 2$
Putting $l = 2$ in A
 $4l - m = 10$
 $4(2) = m = 10$
 $8 + m = 10$

-------Pilot Superope Mathematics 257 -m = 10 - 8m = 2 m = 2 thus 1 2. m = 2Q.8. The expression $1x^3 + mx^2 + 4$ leaves remainder of - 3 and 12 when divided by (x - 1) and (x + 2)respectively. Calculate the values of I and m. Solution. $p(x) = ix^{2} + mx^{2} - 4$ From $x = \theta + x = 1$ $p(1) = t(1)^3 + m(1)^2 - 4$ -1+m 1 1+m-4 = 3 (1st Condition) l+m=3+J1 + m - 1 $p(x) = bx^3 + inx^3 + 4$ From $x + B = \theta + x = -2$ $p(-2) = l(-2)^{1} + m(-2)^{2}$ = 8t · Jm 4 81 + 4m 4 - 12 (2nd Condition) -81 + 4m = 12 + 4-81 + 4m = 1621 m - 1 (B) $l \cdot m = l$ From A31 --3 From A + BI = -I1 · m = 1 (From A)Putting m = l + lThus I = 1, m = 2

CARACTER CONTROL OF THE CONTROL OF T

MATHEMATICS FOR 9TH CLASS (UNIT # 5)

Pilot Superone Mathematics 258 Class 9^{th} Q.9. The expression $ax^3 - 9x^2 + bx + 3a$ is exactly divisible by $x^2 - 5x + 6$. Find the values of a and b.

Solution:-

Factoriting:
$$x^2 - 5x + 6$$

 $x^2 - 2x - 3x + 6$
 $= x(x-2) - 3(x-2)$
 $= (x-2)(x-3)$

If x' = 5x + 6 divides the expression $ax^3 = 9x^2 + bx + 3a$ then x + 2 and x - 3 will also divide it.

$$p(x) = ax^{3} - 9x^{2} + bx + 3a$$

$$x - 2 = 0; x = 2$$

$$p(2) = a(2)^{3} - 9(2)^{2} + b(2) + 3a$$

$$= 8a - 36 + 2b + 3a$$

$$= 11a + 2b - 36$$

$$\begin{array}{rcl}
\cdot t_{c\bar{t}} + 2b & -36 = 0 & (1^{st} \text{ Condition}) \\
(1a + 2b & = 36 & (A) \\
p(x) & = ax^3 - 9x^2 + bx + 3a \\
p(3) & = a(3)^3 - 9(3)^3 + b(3) + 3a \\
& = 27a - 8I + 3b + 3a \\
& = 30a + 3b - 81
\end{array}$$

$$\Re(a + 3b - 8) = 0$$
 (2nd Condition)
 $30a + 3b = 8$!

$$10a + b = 27$$
 (B) Dividing by 3
 $11a + 2b = 36$ A

$$10a + b = 27$$
 B
 $29a + 2b = 54$ (i) Multiplying B by 3

$$a < 11a + 2b = 36$$
 (ii) Subtracting it from .

$$9a = 18$$

 $a = 2$
 $10a + b = 27$ From B
 $10(2) + b = 27$ Putting a 2

$$20 + b = 27$$

 $b = 27 = 20$

Thus a = 2, b = 7

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Pilot Superone Mathematics 259 Exercise 5,4 Factorize each of the following cubic polynomials by factor theorem. $x^3 - 2x^2 - x + 2$ 2. $x^3 - x^2 - 22x + 40$ L $x^3 - 6x^2 + 3x + 10$ 4. $x^3 + x^2 - 10x + 8$ 3. $x^{1} - 2x^{2} - 5x + 6 = 6$, $x^{1} + 5x^{2} - 2x - 24$ $3x^{1} - x^{2} - 12x + 4 = 8$, $2x^{3} + x^{2} - 2x - 1$ 7. Solutions:- $P(x) = x^3 - 2x^2 - x + 2$ p = 2 and possible factors of 2 are $\pm 1 \pm 2$ q = 1 and possible factor of 1 are 1 possible factors of P(x) will be from P = ± 1.±2 $P(x) = x^3 - 2x^2 + x + 2$ $P(1) = (1)^3 - 2(1)^2 - (1) + 2$ = 1 - 2 - 1 + 2 = 0 Remainder) x - I is one factor. $P(1) = (-1)^3 - 2(-1)^2 - (-1) + 2$ $= -1 \cdot 2 + 1 + 2 = 0$ (Remainder) x | d is another factor $P(2) = (2)^3 - 2(2)^2 - (2) + 2$

=882+2=0 (R)

x 2 is third factor.

Thus

2.

 $x^3 - 2x^2 - x+2 = (x - 1)(x + 1)(x - 2)$ $P(x) = x^3 - x^3 - 22x + 40$

p = 40, possible factors of 40 are ± 1 , ± 2 , ± 4 , ± 5 , ± 8 , ± 10, ± 20

q = I, possible factor of I are $\pm I$, P(x) = 0: possible factors of P(x) will be from

MATHEMATICS FOR 9TH CLASS (UNIT # 5)

Pilot Superone Mathematics 260 Class 9* $\frac{P}{q} = \pm 1, \pm 2, \pm 4, \pm 5, \pm 8, \pm 10, \pm 20$ $P(x) = x^{3} - x^{2} - 22x + 40$ Put = x - 2 $P(2) = (2)^{3} - (2)^{2} - 22(2) + 40$ $= 3 - 4 + 4 + 40 = 0 \qquad (R)$ = 64 - 16 - 88 + 40 $= 104 - 104 = 0 \qquad (R)$ = x + 4 is also factor of Y(x)

Put
$$x = 5$$

 $P(5) = (5)^3 = (5)^2 = 22(5) + 40$
 $1.25 = 25 - 110 + 40$
 $165 = 135 \neq 0$ (R)

(x - 5) is not factor of P(x)

Put
$$x = 5$$

 $P(-5) = (-5)^3 \cdot (-5)^3 \cdot 22(-5) + 40$
 $= -125 \cdot 25 + 110 + 40$
 $= -150 + 150 + 0$ (R)

x + Sis also factor of P(x)

Thus $x^2 + x^2 + 22x + 4(1 - 4x - 2)(x - 4)(x + 5)$ $P(x) = x^2 - 6x^2 + 3x + 40$

P = 10, possible factor of 10 are 11, \pm 2, \pm 5, \pm 10 q = 1 factor of 1 are \pm 1 possible factors of P(x) can be

 $q \rightarrow I$ factor of I are $\pm I$ possible factors of I(x) found from P = 4 + 1 + 2 + 5 + 10

Put
$$x = 1, \pm 2, \pm 5, \pm 10$$

$$P(x) = x^3 - 6x^2 + 3x + 10$$
Put $x = 1$

$$P(x) = (1)^2 - (1)^2 - 6(1)^2 + 10$$

wind de

Prior Superorg Mathematics 261 $\frac{1}{1} \cdot 6 \cdot 3 + 10$ $= 11 \cdot 6 \cdot 8 \neq 0$ (81

 $\tau = I$ is not factor.

Put
$$x = -1$$

 $P(x) = (-1)^3 - 6(-1)^2 + 3(-1) + 10$
 $1 - 6 - 3 + 10 = 0$ (R9)

(x + /) is factor

$$P(x) = x^{2} - 6x^{2} + 3x + 10$$
Put $x = 2$

$$P(2) - (2)^{3} - 6(2)^{2} + 3(2) + 10$$

$$= 8 - 24 + 6 + 10$$

$$= 24 - 24 = 0$$
(R)

x = 2 factor

Put
$$x = 5$$

 $P(5) = (5)^3 - 6(5)^2 + 3(5) + 10$
 $-125 - 150 + 15 + 10$
 $-150 - 150 = 0$ (R)

x - 5 p also factor

Thus

$$x^{3} \cdot 6x^{2} \cdot 3x + (0 = (x + 1)(x - 2)(x - 5))$$
$$P(x) = x^{3} + x^{2} \cdot 10x + 8$$

P 8, factor of 8 are ± 1 , ± 2 , ± 4 , ± 8

q = I factor of I are f I possible factors can be found from

$$\frac{p}{1} = \pm 1. \pm 2, \pm 4, \pm 8$$

$$P(x) = x^3 + x^3 - 10x + 8$$
Put $x = 1$

winh di

Filot Superone Mathematics 262 Class 9^{th} $P(l) = (1)^{3} + (1)^{2} - 10(1) + 8$ $= 1 + 1 - 10 + 8 = 0 \qquad (R)$ x - l is factor of P(x)

$$P(x) = x^{3} + x^{2} - 10x + 8$$
Put $x = 2$

$$P(2) = (2j^{3} + (2)^{2} - 10(2) + 8$$

$$= 8 + 4 - 20 + 8$$

$$= 20 - 20 - 0$$
(R)

x 2 is also factor

$$P(x) = x^{3} + x^{2} - 10x + 8$$
Put $x = -4$

$$P(-4) = (-4)^{3} + (-4)^{2} - 10(-4) + 8$$

$$= -64 + 16 - 40 + 8$$

$$= -44 + 64 = 0$$
(R)

x + 4 is factor

Thus

5.

$$x^3 + x^2 = 10 + 8 = (x - 1)(x - 2)(x + 4)$$

 $P(x) = x^3 - 2x^2 + 5x + 6$

P 6, factor of 6 are ±1, ±2 ±3 ±6

q = I, factor of I are f I members of factors of P(x) can be found from

$$\frac{p}{q} = \pm 1, \pm 2, \pm 3, \pm 6$$

$$P(x) = x^{3} - 2x^{2} - 5x + 6$$
Put $x = 1$

$$P(1) = (1)^{3} - 2(1)^{2} - 5(1)$$

$$= 1 - 2 - 5 + 6$$

$$= 7 - 7 = 0$$

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Pilot Superone Mathematics 263 Class 9*

x I is factor of P(x)

$$P(z) = x^{3} - x^{2} - 5x + 6$$
Put $x = 2$

$$P(2) = (+2)^{3} - 2(+2)^{2} - 5(+2) + 6$$

$$= + 8 - 8 - 10 + 6$$

$$= 14 - 18 = -4 \neq 0$$
(R)

x = 2 is not factor of P(x)

$$P(x) = x^{2} \cdot 2x^{2} - 5x + 6$$
Put $x = 3$

$$P(3) = (3)^{3} - 2(3)^{2} - 5(3) + 6$$

$$= 27 - 18 - 15 + 6$$

$$= 33 - 33 = 0$$
(R)

x = 3 is also factor of P(x)

Thus

$$P(x) = x^{2} - 2x^{2} - 5x + 6$$
Put $x = -2$

$$P(-2) = (-2)^{2} - 2(-2)^{2} - 5(-2) + 6$$

$$= -8 - 8 + 10 + 6$$

$$= -16 + 16 = 0$$
(R.

+ 2 is one factor of P(x)

Thus

$$x^{3}-2x^{2}-5x+6=(x-1)(x-3)(x+2)$$

$$P(x)=x^{3}+5x^{2}-2x-24$$

P = -24. factor of 6 are ± 1 , ± 2 , ± 3 , ± 4 , ± 6 , ± 8 , ± 12 , ± 24 , q = 1, factor of q are $= \pm 1$ possible factors of P(x) will be found from

print.

P. or Superone Mathematics 264	<u>Class 9**</u>
$\frac{P}{q} = \pm 1, \pm 2, \pm 3, \pm 4, \pm 4$	6 ± 8, ± 12, +24
$P(x) = x^3 + 3x^2 - 2x - 24$,
Pu\	(
$P(2) = (2)^3 + 5(2)^2 - 2(2)$	- 24
= 8 + 20 4 - 24	
28 28 0	(A)
(x-2) is factor of $P(x)$	
$P(x) = x^3 + 5x^2 - 2x - 24$	
Put x - 3	
$P(-3) = (-3)^3 + 5(+3)^3 - 3$	
- 27 + 45 · 6 2:	
-51-5I=0	(R)
x + 3 is factor of $P(x)$	
$P(x) = x^3 + 3x^2 - 2x - 24$	•
Put # 4	
$P(4) = (4)^3 + 5(4)^2 \cdot 2(4)$	- 24
64 + 80 8 - 24	d) .
= 144 32 ≠0	(R)
x = 4 is not factor of $P(x)$	
Put x = -4	24 44 24
$P(-x^2 - (-4)^3 + 5(-4)^2$	
64 + 80 + 8 = 2 R8 - 88 = 0	(R)
An Super of Mari	111/
$x + 4$ is factor of $P(x) = x^3 + 5x^2 - 2x - 24 - (x - 7)^{-1}$. di
7. $P(x) = 3x^2 - 125 + 125$	•

Pilot Superone Mathematics 265 Class 91

P = 4 factor of 4 are $+1, \pm 2, \pm 4$

q = 3 factor of 3 are $- + 1 \pm 3$ possible factors of P(x)

can be found from $\frac{p}{a}$

x 2 is factor of P(x)

Put
$$x = -2$$
 in $P(x)$

$$P(-2) = 3t - 2t^{3} - (-2t^{2} - 12t - 2) + 4$$

$$-2t - 4 + 2t + 4$$

$$= -2t + 2t - 4$$

$$= -2t - 4$$

$$= -2t$$

x + 2 is factor of P(x)

Put
$$x = \frac{1}{2}$$

 $P(\frac{I}{2}, -3i\frac{I}{2})^3 - (\frac{I}{2})^2 - 12(\frac{I}{2}) + 4$
 $= \frac{3}{8} - \frac{I}{4} - 6 + 4 \neq 0$ (R)

2x - I is not factor of P(x)

Put
$$x = \frac{1}{3}$$

 $P(\frac{1}{3}) = 3(\frac{1}{3})^3 - (\frac{1}{3})^2 - 12(\frac{1}{3}) + 4$
 $3 \times \frac{1}{27} = \frac{1}{9} - 4 + 4 = 0$ (R)

 $x = \frac{1}{3} g_1 v cs 3x - 1 = 0$

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Pilot Superone Mathematics 266 Class 9th

 $\exists x \mid I$ is factor of P(x)

Thus

$$3x^3 - x^2 + 12x + 1 = (x - 2)(x + 2)(3x - 1)$$
$$P(x) = 2x^3 + x^2 - 2x - 1$$

P = I, factor of $\cdot I$ are $\pm I$

q = 2, factor of 2 are $= \pm 1$, ± 2 possible factors of P(x)

will be found from $\frac{p}{q}$

$$P(x) = \pm 1, \pm \frac{1}{2}$$

$$P(x) = 2x^{3} + x^{2} - 2x - 1$$

$$x = 1$$

$$P(x) = 2x^{3} + x^{2} - 2x - 1$$

Put x = 1 $P(1) = 2(1)^3 + (1)^2 - 2(1) - 1$ = 2 + 1 = 2 + 1 = 0 (R)

x + I is factor of F(x)

Put
$$x = -1$$

 $P(-1) = 2(-1)^3 + (-1)^2 - 2(-1) - 1$
 $= -2 + 1 + 2 - 1$ (R)

x + 1 is factor of P(x)

Put
$$x = -\frac{1}{2}$$

 $P(-\frac{1}{2}) = 2(-\frac{1}{2})^3 + (-\frac{1}{2})^2 - 2(-\frac{1}{2}) - 1$
 $= -2 \times \frac{1}{8} + \frac{1}{4} + 1 - 1$
 $= -\frac{1}{4} + \frac{1}{4} + 1 - 1 = 0$ (R)

From $x = -\frac{1}{2}$, $2x + \ln x$ factor of P(x)

Thus $f(x) = \frac{1}{2x} - 1 = (x - 1)(x + i)(2x + 1)$

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Pilot Superone Mathematics 271 Class 9th



ALGEBRAIC MANIPULATION

Highest Common Factor (H.C.F) and Least Common Multiple (L.C.M) of Algebraic Expressions Highest Common Factor (H.C.F):

If two or more algebraic expressions are given then their common factor of highest power is called the H.C.F. of the expressions.

Least Common Multiple (L.C.M.)

If an algebraic expression p(x) is exactly divisible by two or more expressions, then p(x) is called the Common Multiple of the given expressions.

The Least Common Multiple (L.C M) is the product of common factor of the given expressions.

Square Root:

Square root of an algebraic expression p(x) will be another algebraic expression q(x) if $[q(x)] \times [q(x)] = p(x)$

Exercise 6.1

```
Q.1 Find the H.C.F. of the following expressions.

(i) 39x^{3}y^{3}z, 91x^{5}y^{6}z^{7}

(ii) 102xy^{2}z, 85x^{2}yz, 187xyz^{2}

1(i) 39x^{3}y^{3}z, 91x^{5}y^{6}z^{7}

Solution: 39x^{7}y^{3}z = 3 \times 13 x^{5} x^{2}.y^{3}.z

91x^{5}y^{6}z^{7} = 7 \times 13 x^{5}.y^{3}.y^{3}.z.z^{6}

H.C.F. = 13x^{5}y^{3}z

1(ii) 102xy^{2}z, 85x^{2}yz, 187xyz^{2}

Solution: 102xy^{2}z = 2 \times 3 \times 17 xyyz

85x^{2}yz = 5 \times 17xxyz
```

Pilot Superone Mathematics 272 Class 9th 187xvz² - 11 × 17xyzz H C F. = 17xyz

Q.2 Find the H.C.F. of the following expressions by factorization.

(i)
$$x^2 + 5x + 6$$
, $x^2 - 4x + 12$
(ii) $x^3 - 27$, $x^2 + 6x + 27$, $2x^2 - 18$
(iii) $x^3 - 2x^2 + x$, $x^3 + 2x - 3$, $x^1 + 3x - 4$
(iv) $18(x^3 - 9x^2 + 8x)$, $24(x^2 - 3x + 2)$
(iv) $36(3x^4 + 5x^3 - 2x^2)$, $54(27x^4 - x)$

2(i) $x^2 + 5x + 6$, $x^2 + 4x - 12$

$$x^2 + 5x + 6$$
, $x^2 + 2x + 3x + 6$

$$= x(x + 2) + 3(x + 2)$$
and $x^2 - 4x - 12$

$$x^2 - 4x - 12$$

$$x^2 - 4x - 12$$

$$x^2 - 4x - 12$$

$$x^2 + 5x + 6 = (x + 2)(x + 3)$$

$$x^2 - 4x - 12 = (x - 6)(x + 2)$$
H.C. F. = $x + 2$

$$x^2 + 6x - 27$$
, $2x^2 - 18$

$$x^3 - 27 = (x)^3 - (3)^3$$

$$(x - 3)[(x)^2 + (x)(3) + (3)^2]$$

$$= (x - 3)(x^2 + 3x + 9)$$

$$x^2 + 6x - 27 = x^2 + 9x - 3x - 27$$

$$-x(x + 9) - 3(x + 9)$$

$$= (x - 3)(x + 3)$$

Pilot Superone Mathematics 273 Class 9th Now
$$x^3$$
 27 = (x 3)(x² + 3x + 9) x^2 + 6x 27 = (x - 3)(x + 9) $2x^2$ + 18 = 2(x 3)(x + 3) H.C.F. = (x - 3)

2(iii) x^3 - 2x² + x, x^2 + 2x 3, x^2 + 3x - 4

Solution. x^3 - 2x³ + x = x(x² - 2x + 1) = x(x² - x - x + 1) = x(x - 1)(x - 1)] = x(x - 1)(x - 1) = x(x - 1)(x + 3) = (x - 1)(x + 3) = (x - 1)(x + 3) = (x - 1)(x + 4)

Now x^3 - 2x² + x = x(x - 1)(x - 1) = (x - 1)(x + 4) = (

MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone Mathematics 274 Class 9th 2(v)
$$36(3x^4 + 5x^3 - 2x^2)$$
, $54(27x^4 - x)$
Solution $36(3x4 + 5x3 - 2x^2)$, $54(27x^4 - x)$
 $= 4 \times 9x2[3x2 + 6x - x - 2]$
 $= 4 \times 9x2[3x(x + 2) - 1(x + 2)]$
 $= 2 \times 2 \times 3 \times 3x2(x + 2)(3x - 1)$
 $= 6 \times 9x[(3x)3 - (1)3]$
 $= 2 \times 3 \times 3x3(3x - 1)(9x2 + 3x + 1)$
Now $36(3x4 + 5x3 - 2x2) = 2 \times 2 \times 3 \times 3x2(x + 2)(3x - 1)$
 $= 54(27x4 - x) = 2 \times 3 \times 3x(3x - 1)(9x2 + 3x + 1)$
H.C.F. $= 2 \times 3 \times 3x(3x - 1)$
 $= 18x(3x - 1)$
Q: Find the H.C.F. of the following by division method.
(i) $= x^3 + 3x^2 - 16x + 12$, $= x^3 + x^2 - 10x + 8$
(ii) $= x^3 + 3x^2 - 16x + 12$, $= x^3 + x^3 - 3x^3 - 3x^2 - 3x^3 - 3x^2 - 3x^3 - 3x^3$

H.C.F =
$$x^2 - 3x + 2$$

Pilot Superone Mathematics 275 Class 9th 3(ii)
$$x^4 + x^5 - 2x^2 + x - 3$$
, $5x^3 + 3x^2 - 17x + 6$

Solution.
$$5x^3 + 3x^2 - 17x + 6 = x^4 + x^3 - 2x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^4 + x^3 - 2x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^4 + x^3 - 2x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^2 + x - 3$$

$$x + 2 = x^3 + 3x^2 - 17x + 6 = x^2 + x - 3$$

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$$x + 3 + x^2 - 3x - 3$$

$$x + 4 - 3x^3 - 3x^2 - 3x - 3$$

$$x + 4 - 3x^3 - 3x^2 - 3x - 3$$

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$$x + 4 - 3x^3 - 3x^2 - 3x - 3$$

$$x + 4 - 3x^3 - 3x^2 - 3x - 3$$

$$x + 4 - 3x$$

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Pilot Superone Mathematics 276 HCF of x and x2 .s x HC.F = x(x + 1)Q.4 Find the L.C.M. of the following expression by factorization. (i) $39x^2y^3z$, $91x^5y^6z^7$ (ii) 102xy²z, 85x²yz, 187xyz² 39x'y'z, 91x5y6z7 4(i) Solution: $39x^{7}y^{3}z = 3 \times 13x^{7}y^{3}z = 3 \times 13x^{5}x^{2}y^{3}z$ $91x^5y^6z^7 = 7 \times 13x^5y^6z^7 = 7 \times 13x^5y^3y^2zz^6$ L.C.M. = (Common factor)×(non-common factor) $=(13x^5y^3z)(3\times7x^2y^3z^6)$ $= 13 \times 3 \times 7 \chi^{5+2} v^{3+3} z^{1+6}$ $= 273x^{1}y^{6}z^{7}$ 4(11) 102xy²z, 85x²yz, 187xyz² Solution: $102xy^2z = 2x3 \times 17xyyz$ $85x^2yz = 5 \times 17 \times x y.2$ $[87xyz^2 = 11 \times 17xyzz]$ L C M = (Common factor)×(non-common factor) $= (17xyz)(2 \times 5 \times 11xyz)$ $= 17 \times 2 \times 3 \times 5 \times 11 x^2 v^2 z^2$ $= 5610x^2y^2z^2$ Find the L.C.M. of the following expression by 0.5

factorization.

(i)
$$x^2 - 25x + 100, x^2 - x - 20$$

(i)
$$x^2 + 4x + 4, x^2 - 4, 2x^2 + x - 6$$

$$\frac{(ii)}{(iii)} = 2(x^4 - y^4), 3(x^3 + 2x^2 - xy^2 - 2y^3)$$

(iii)
$$2(x^2-y), 6(x^3-x^2-x+1)$$

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Pilot Superone Mathematics 277 Class 9th 5(i) $x^{2}-25x+100, x^{2}-x-20$ $x^2 - 25x + 100 = x^2 - 5x - 20x + 100$ Solution: = x(x-5) - 20(x-5)= (K 5)(X 20) $x^2 - x \cdot 20 = x^2 - 5x + 4x - 20$ = x(x-5) + 4(x-5)= (x - 5)(x + 4) $x^2 - 25x + 100 = (x - 5)(x - 20)$ Now $x^2 - x - 20 - (x - 5)(x + 4)$ and L.C.M. = (x-5)(x-20)(x+4)5(ii) $x^2 + 4x + 4$, $x^2 - 4$, $2x^2 + x - 6$ $x^2 + 4x + 4 = x^2 + 2x + 2x + 4$ Solution: x(x + 2) + 2(x + 2) \Rightarrow (x + 2)(x + 2) $x^2 - 4 = (x)^2 - (2)^2$ =(x - 2)(x + 2) $2x^2 + x - 6 = 2x^2 + 4x - 3x - 6$ =2x(x+2)-3(x+2)=(x+2)(2x-3) $x^2 + 4x + 4 = (x + 2)(x + 2)$ Now $x^2 - 4 = (x - 2)(x + 2)$

$$2x^{2} + x - 6 = (x + 2)(2x - 3)$$

$$L C.M. = (x + 2)(x + 2)(x - 2)(2x - 3)$$

$$= (x + 2)^{2}(x - 2)(2x - 3)$$

$$5(iti) \quad 2(x^{4} - y^{4}), 3(x^{3} + 2x^{2} - xy^{2} - 2y^{3})$$
Solution:
$$2(x^{4} - y^{4}) = 2[(x^{2})^{2} - (y^{2})^{2}]$$

$$= 2(x^{2} + y^{2})(x^{2} - y^{2})$$

$$= 2(x^{2} + y^{2})(x + y)(x - y)$$

$$3(x^{3} + 2x^{2} - xy^{2} - 2y^{3}) = 3[(x^{3} + 2x^{2}y) = (xy^{2} - 2y^{3})]$$

$$= 3[x^{2}(x + 2y) - y^{2}(x + 2y)]$$

Pilot Superone Mathematics
$$\frac{278}{3(x+2y)(x^2-y^2)}$$
 $= 3(x+2y)(x+y)(x-y)$
 $2(x^4-y^4) = 2(x^2+y^2)(x+y)(x-y)$
 $3(x^3+2x^2-xy^2-2y^2) = 3(x+2y)(x+y)(x-y)$
 $1 \le 2 \le 3(x+y)(x-y)(x+2y)(x^2+y^2)$
 $1 \le 6(x+y)(x-y)(x+2y)(x^2+y^2)$
 $1 \le 6(x^2-y^2)(x^2+y^2)(x+2y)$
 $1 \le 2 \le 2(x^2+1)(x^2-1)$
 $1 \le 2 \le 2(x^2+1)(x^2-1)$
 $1 \le 2 \le 2(x^2+1)(x+1)(x-1)$
 $1 \le 2 \le 3(x-1)(x^2-1)$
 $1 \le 2 \le 3(x-1)(x^2-1)$
 $1 \le 2 \le 3(x-1)(x+1)(x-1)(x^2+1)$
 $1 \ge 2 \le 3(x-1)(x+1)(x-1)(x-1)(x^2+1)$
 $1 \ge 2 \le 3(x-1)(x+1)(x-1)(x-1)(x^2+1)$
 $1 \ge 2 \le 3(x-1)(x+1)(x-1)(x-1)(x-1)(x-1)(x-1)$
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 $1 \le 3(x-1)(x+1)(x-1)$
 $1 \le 3(x-1)(x$

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Pilot Superone Mathematics 279 Class 9th

16 4 2k - 2

10 2k = R

R must be zero

$$10 2k = 0$$

$$2k = 10$$

$$k = 5$$

$$q(x) 2x^{2} + kx - 12$$

$$x = -4$$

$$q(-4) = 2(-4)^{2} 4k - 12$$

$$= 32 - 4k - 12$$

$$= 20 4k = R$$

R must be zero

$$20 - 4k = 0$$
$$-4k = 20$$
$$k = 5$$

Q.7 If
$$(x + 3)(x - 2)$$
 is the H.C.F. of $p(x) = (x + 3)(2x^2 - 3x + k)$ and $q(x) = (x - 2)(3x^2 + 7x + 1)$, find k and l.

Solution: (x-2)(x+3) will divide $p(x) = (x+3)(2x^2 - 3x + k)$ We put x - 2 in it.

$$p(2) = (2+3)[2 \times 2^2 - 3(2) + k]$$

$$= 5(8 + 6 + k)$$

$$= 5(2 + k) = R$$

R must be zero

$$5(2 + k) = 0$$

$$2 + k = 0$$

$$k = 2$$

$$q(x) = (x-2)(3x^{2} + 7x + 1)$$

$$(x-2)(x+3) \text{ will divide } q(x) = (x-2)(3x^{2} + 7x + 1)$$
Completely We put $x = -3$ in it

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MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone Mathematics 280 Class 9th $q(-3) = (-3-2)[3(-3)^2 + 7(-3) - I]$ = (-5)(27-21+I)= (-5)(6-I) = R

R must be zero

$$(5)(6-i) = 0$$

 $6-i = 0$
 $i = 6$

Q.8 The L.C.M. and H.C F of two polynomials p(x) and $2(x^4-1)$ and $(x+1)(x^2+1)$ respectively.

If $p(x) = x^{1} + x^{1} + x + 1$, find q(x) are

Solution: Formula
$$p(x) \times q(x) = L.C.M. \times H.C.F$$

 $p(x) \times q(x) = 2(x^4 + 1)(x + 1)(x^2 + 1)$
 $(x^3 + x^2 + x + 1) \times q(x) = 2(x^4 + 1)(x + 1)(x^2 + 1)$
 $q(x) = \frac{2(x^4 + 1)(x + 1)(x^2 + 1)}{x^3 + x^2 + x + 1}$
 $= \frac{2(x^4 + 1)(x + 1)(x^2 + 1)}{x^2(x + 1) + 1(x + 1)}$
 $= \frac{2(x^4 + 1)(x + 1)(x^2 + 1)}{(x + 1)(x^2 + 1)}$
 $= \frac{2(x^4 + 1)(x + 1)(x^2 + 1)}{(x + 1)(x^2 + 1)}$
 $= \frac{2(x^4 + 1)(x + 1)(x^2 + 1)}{(x + 1)(x^2 + 1)}$

Q.9 Let $p(x) = 10(x^2 - 9)(x^2 - 3x + 2)$ and $q(x) = 10x(x + 3)(x - 1)^2$. If the H.C F. of p(x), q(x) is 10(x + 3)(x - 1), find their L.C.M.

Solution: Formula $p(x) \times q(x) = L.C.M. \times H.C.F.$ Putting values in it.

$$10(x+3)(x-1)\times q(x) = 10(x^2-9)(x^2-3x+2)(10)(x)(x+3)(x-1)^2$$

$$q(x) = \frac{10(x^2-9)(x^2-3x+2)(10)(x)(x+3)(x-1)^2}{10(x+3)(x-1)}$$

Prior Superope Mathematics 281 Class 9th
=
$$(x^2 - 9)(x^2 - 3x + 2)(10)(x)(x - 1)$$

= $10x(x^2 - 9)(x - 1)(x^2 - 3x + 2)$
= $10x(x^2 - 9)(x - 1)[(x^2 - 2x - x + 2)]$
= $10x(x^2 - 9)(x - 1)[x(x - 2) - 1(x - 2)]$
= $10x(x^2 - 9)(x - 1)(x - 1)(x - 2)$
= $10x(x^2 - 9)(x - 1)^2(x - 2)$

Q.10 Let the product of L.C.M. and H.C.F. of two polynomials be $(x + 3)^2(x - 2)(x + 5)$. If one polynomial is (x + 3)(x - 2) and the second polynomial is $x^2 + kx + 15$, find the value of k.

Solution. (L.C.M.) × (H.C.F.) =
$$(x + 3)^2(x-2)(x + 5)$$

$$p(x) = (x + 3)(x - 2)$$

$$q(x) = x^2 + kx + 15$$

$$p(x) × q(x) = H.C.F. × L.C.M$$

Putting value in it

٠.

$$(x^{2} + kx + i5)(x + 3)(x - 2) = (x + 3)^{2}(x - 2)(x + 5)$$

$$x^{2} + kx + 15 = \frac{(x + 3)^{2}(x - 2)(x + 5)}{(x + 3)(x - 2)}$$

$$x^{2} + kx + 15 = (x + 3)(x + 5)$$

$$x^{2} + kx + 15 = x^{2} + 8x + 15$$

$$kx = x^{2} + 8x + 15 - x^{2} - 5$$

$$kx = 8x$$

$$k = 8$$

MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone I tax rematics 282 Class 9th Q. 11 Waqas with hes to distribute 128 bananas and also 176 apples among a certain number of children. Find the nighest rember of children who can get the fruit in

Solution: Number of children will be H.C.P of 176 and 128

this way.

Number of children * 16

Pilot Superone Mathematics 284

Q.2 $\left[\frac{x+1}{x-1} - \frac{x-1}{x+1} - \frac{4x}{x^2+1}\right] + \frac{4x}{x^4-1}$ **Solution:** $= \begin{pmatrix} x+1 & x & 1 \\ x-1 & x+1 \end{pmatrix} - \frac{4x}{x^2+1} + \frac{4x}{x^4-1}$ $=\frac{(x+1)^2-(x-1)^2}{(x-1)(x+1)}-\frac{4x}{x^2+1}+\frac{4x}{x^4-1}$ $= \frac{x^2 + 2x + 1 - x^2 + 2x - 1}{x^2 - 1} - \frac{4x}{x^2 + 1} + \frac{4x}{x^4 - 1}$ $=\left[\frac{4x}{x^2-1}-\frac{4x}{x^2+1}\right]+\frac{4x}{x^4-1}$ $= (4x) \left[\frac{1}{x^2 - 1} - \frac{1}{x^2 + 1} \right] + \frac{4x}{x^4 - 1}$ $(4x) \left[\frac{x^2 + 1 - x^2 + 1}{(x^2 - 1)(x^2 + 1)} \right] + \frac{4x}{x^4 - 1}$ $= (4x) \left[\frac{2}{x^4 - 1} \right] + \frac{4x}{x^4 - 1}$ $\left(4x\right)\left[\frac{2}{x^4-1}+\frac{1}{x^4-1}\right]$ $(4x)\left[\frac{2+1}{(x^4-1)}\right]$ $=\frac{12x}{x^{4}}$ $Q.3 = \frac{1}{x^2 - 8x + 15} + \frac{1}{x^2 + 4x + 3} - \frac{2}{x^2 - 6x + 5}$ Solution: = $\frac{1}{x^2 - 3x - 5x + 15} + \frac{1}{x^2 - x - 3x + 3} + \frac{2}{x^2 - x - 5x + 5}$

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$$= \frac{1}{x(x-3)-5(x-3)} + \frac{1}{x(x-1)-3(x-1)} + \frac{2}{x(x-1)-5(x-1)}$$

$$= \frac{1}{(x-3)(x-5)} + \frac{1}{(x-1)(x-3)} + \frac{2}{x(x-1)(x-5)}$$

$$= \frac{1}{(x-1)+(x-5)} + \frac{1}{(x-1)(x-3)} + \frac{2}{(x-1)(x-5)}$$

$$= \frac{(x-1)+(x-5)}{(x-3)(x-5)(x-1)}$$

$$= \frac{x-1+x-5-2x+6}{(x-3)(x-5)(x-1)}$$

$$= \frac{2x-2x+6-6}{(x-3)(x-5)(x-1)}$$

$$= 0$$
2.4 $\frac{(x+2)(x+3)}{x^2-9} + \frac{(x+2)(2x^2-32)}{(x-4)(x^2-x-6)}$

$$= \frac{(x+2)(x+3)}{(x)^2-(3)^2} + \frac{(x+2)(2)(x^2-16)}{(x-4)(x^2-3x+2x-6)}$$

$$= \frac{(x+2)(x+3)}{(x-3)(x+2)} + \frac{2(x+2)(x^2-4^2)}{(x-4)(x(x-3)+2(x-3))}$$

$$= \frac{(x+2)}{(x-3)} + \frac{2(x+2)(x-4)(x+4)}{(x-4)(x-3)(x+2)}$$

$$= \frac{x+2}{x-3} + \frac{2(x+4)}{x-3}$$

$$= \frac{x+2+2x+8}{x-3}$$

$$= \frac{3x+10}{x-3}$$

MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone Mathematics	286	Class 9th
$Q.5 = \frac{x+3}{2x^2+9x+9} + \frac{1}{2(2x-3)}$	$\frac{4x}{4x^2-9}$	
Solution = $\frac{x+3}{2x^2+6x+3x+9}$	$+\frac{1}{2(2\pi-3)}$	$\frac{4x}{2x)^2-(3)^2}$
$=\frac{x+3}{2x(x+3)+3(x+3)}$	$\frac{1}{30} + \frac{1}{2(2x-3)}$	$\frac{4x}{(2x+3)(2x-3)}$
$= \frac{x+3}{(2x+3)(x+3)} +$	$\frac{1}{2(2x-3)}$ $\frac{1}{(2x-3)}$	$\frac{4x}{(+3)(2x-3)}$
$= \frac{1}{(2x+3)} + \frac{1}{2(2x+3)}$	$\frac{4x}{(2x+3)(2x+3)}$	(x-3)
$=\frac{2(2x-3)+(2x+3)}{2(2x+3)(2x+3)}$	+3)- (4x)(2)	
$= \frac{4 \times 6 + 2 \times + 3 - 2}{2(2 \times + 3)(2 \times - 3)}$		
$=\frac{2x-3}{2(2x+3)(2x-3)}$	_	
$=\frac{-(2x+3)}{2(2x+3)(2x-3)}$	3)	
$=\frac{-1}{2(2x-3)}$		
Q.6 A - $\frac{1}{A}$ if A = $\frac{a+1}{a-1}$		
Solution: $A \cdot \frac{1}{A} =$	$\frac{a+1}{a-1} - \frac{1}{a+1}$	
_	$\frac{a+1}{a-1} - \frac{a-1}{a+1}$	

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$$\frac{(a+1)^2 - (a-1)^2}{(a-1)(a+1)}$$

$$\frac{(a^2+2a+1) - (a^2-2a+1)}{(a-1)(a+1)}$$

$$-\frac{a^2+2a+1 - a^2+2a-1}{(a-1)(a+1)}$$

$$4a$$

$$a^2-1$$

Solution:
$$= \left[\frac{x-1}{x-2} + \frac{2}{x-2}\right] - \left[\frac{x+1}{x+2} + \frac{4}{4-x^2}\right] \times TS$$

$$= \left[\frac{x-1}{x-2} - \frac{2}{x-2}\right] - \left[\frac{x+1}{x+2} - \frac{4}{x^2-4}\right] \times TS$$

$$= \left[\frac{x-1}{x-2} - \frac{2}{x-2}\right] - \left[\frac{x+1}{x+2} - \frac{4}{x^2-4}\right] \times TS$$

$$= \left[\frac{x-3}{x-2}\right] - \left[\frac{(x+1)(x-2)(4)}{(x+2)(x-2)}\right]$$

$$= \frac{x-3}{x-2} - \frac{x^2 - x - 6}{(x+2)(x-2)}$$

$$= \frac{x-3}{x-2} - \frac{x^2 - x - 6}{(x+2)(x-2)}$$

$$= \frac{x-3}{x-2} - \frac{x(x-3) + 2(x-3)}{(x+2)(x-2)}$$

$$= \frac{x-3}{x-2} - \frac{(x-3)(x+2)}{(x+2)(x-2)}$$

Pilot Superone Mathematics 288 Class 9th

$$= \frac{x-3}{x-2} \cdot \frac{x-3}{x-2}$$

$$= 0$$

Q.8 What rational expression should be subtracted from

$$\frac{2x^{2}+2x-7}{x^{2}+x-6} \text{ to get } \frac{x-1}{x-2} ?$$

Let A be the required expression.

Solution: Thus
$$A = \frac{x-1}{x^2 + x - 6}$$

$$= \frac{2x^2 + 2x - 7}{x^2 + x - 6} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{x^2 + 3x - 2x - 6} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{x(x + 3) - 2(x + 3)} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{(x + 3)(x - 2)} - \frac{x - 1}{x - 2}$$

$$= \frac{2x^2 + 2x - 7}{(x + 3)(x - 2)} - \frac{x - 1}{(x + 3)(x - 2)}$$

$$= \frac{2x^2 + 2x - 7 - (x - 1)(x + 3)}{(x + 3)(x - 2)}$$

$$= \frac{2x^2 + 2x - 7 - (x^2 + 2x - 3)}{(x + 3)(x - 2)}$$

$$= \frac{2x^2 + 2x - 7 - (x^2 + 2x - 3)}{(x + 3)(x - 2)}$$

$$= \frac{x^2 - 4}{(x + 3)(x - 2)}$$

Pilot Superone Mathematics 289
$$= \frac{(x+2)(x-2)}{(x+3)(x-2)}$$

$$= \frac{x+2}{x+3}$$

Perform the indicated operations and simplify to the lowest

forms.
$$\frac{x^2 + x - 6}{x^2 - x - 6} \times \frac{x^2 - 4}{x^2 - 9}$$

Q.9 Simplify to the lonest form

$$\frac{x^2 + x - 6}{x^2 - x - 6} \times \frac{x^3 - 2^2}{x^2 - 3^2}$$

Solution.
$$= \frac{x^2 + 3x - 2x - 6}{x^2 - 3x + 2x - 6} \times \frac{x^2 - 2^2}{x^2 - 3^2}$$

$$= \frac{x(x+3) - 2(x+3)}{x(x-3) + 2(x-3)} \times \frac{(x+2)(x-2)}{(x+3)(x-3)}$$

$$= \frac{(x+3)(x-2)}{(x-3)(x+2)} \times \frac{(x+2)(x-2)}{(x+3)(x-3)}$$

$$= \frac{(x-2)(x-2)}{(x-3)(x-3)}$$

$$= \frac{(x-2)^2}{(x-3)^2}$$

Q:10
$$\frac{x^3 - 8}{x^2 - 4} + \frac{x^2 + 6x + 8}{x^2 - 2x + 1}$$
$$\frac{x^3 - 2^3}{x^2 - 2^2} \times \frac{x^2 + 4x + 2x + 8}{x^2 - x - x + 1}$$

Solution:
$$= \frac{x^{2}-2^{3}}{x^{2}-2^{2}} + \frac{x(x+4+2(x+4))}{x(x-1)-1(x-1)}$$

$$= \frac{(x-2)(x^{2}+2x+4)}{(x-2)(x+2)} + \frac{x(x+4)+2(x+4)}{x(x-1)-1(x-1)}$$

Pilot Superone Mathematics 290 Class 9th

$$= \frac{x^2 + 2x + 4}{x + 2} + \frac{(x + 4)(x + 2)}{(x - 1)(x - 1)}$$

$$= \frac{(x^2 + 2x + 4)(x + 4)}{(x - 1)(x - 1)}$$

$$= \frac{(x + 4)(x^2 + 2x + 4)}{(x - 1)^2}$$
211.
$$\frac{x^4 - 8x}{2x^2 + 5x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x^2 - 2x}$$
Solution:
$$- \frac{x(x^3 - 8)}{2x^2 + 6x - x - 3} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= \frac{x(x^3 - 2^3)}{2x(x + 3) - 1(x + 3)} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$= \frac{x(x - 2)(x^2 + 2x + 4)}{(x + 3)(2x - 1)} \times \frac{2x - 1}{x^2 + 2x + 4} \times \frac{x + 3}{x(x - 2)}$$

$$- \frac{x(x - 2)(x^2 + 2x + 4)(2x - 1)(x + 3)}{x(x - 2)(x^2 + 2x + 4)(2x - 1)(x + 3)}$$

$$= 1$$
2.12
$$\frac{2y^2 + 7y - 4}{3y^3 - 13y + 4} + \frac{2y^2 - 1}{6y^2 + y - 1}$$

$$= \frac{2y^2 + 8y - y - 4}{3y^3 - 12y - y + 4} + \frac{(2y)^2 - (1)^2}{6y^2 + 3y - 2y - 1}$$

$$= \frac{2y(y + 4) - 1(y + 4)}{3y(y - 4) - 1(y - 4)} \div \frac{(2y - 1)(2y + 1)}{3y(2y + 1) - 1(2y + 1)}$$

$$= \frac{(y + 4)(2y - 1)}{(y - 4)(3y - 1)} + \frac{(2y - 1)(2y + 1)}{(2y + 1)(3y - 1)}$$

Pilot Superone Mathematics 291 Class 9th

$$= \frac{(y+4)(2y-1)}{(y-4)(3y-1)} \times \frac{2y-1}{3y-1}$$

$$= \frac{(y+4)(2y-1)}{(y-4)(3y-1)} \times \frac{3y-1}{2y-1}$$

$$= \frac{y+4}{y-4}$$
Q.13
$$\left[\frac{x^2+y^2}{x^2-y^2} - \frac{x^2-y^2}{x^2+y^2}\right] \div \left[\frac{x+y}{x-y} - \frac{x-y}{x+y}\right]$$
Solution.
$$= \left[\frac{(x^2+y^2)^2 - (x^2-y^2)^2}{(x^2-y^2)(x^2+y^2)}\right] \div \left[\frac{(x+y)^2 - (x-y)^2}{(x-y)(x+y)}\right]$$

$$= \frac{(x^4+y^4+2x^2y^2) - (x^4+y^4-2x^2y^3)}{(x^2-y^2)(x^2+y^2)} \div \frac{x^2+y^2+2xy-(x^2+y^2-2xy)}{(x-y)(x+y)}$$

$$= \frac{(x^4+y^4+2x^2y^2-x^4-y^4+2x^2y^3)}{(x^2-y^2)(x^2+y^2)} \div \frac{x^2+y^2+2xy-x^2-y^2+2xy}{x^2-y^2}$$

$$= \frac{4x^2y^2}{(x^2-y^2)(x^2+y^2)} \div \frac{4xy}{x^2-y^2}$$

$$= \frac{4x^2y^2}{(x^2-y^2)(x^2+y^2)} \times \frac{x^2-y^2}{4xy}$$

$$= \frac{xy}{x^2+y^2}$$

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Exercise 6.3

Use factorization to find the square root of the 0.1 following expressions.

(i)
$$4x^2 + 12xy + 9y^2$$

(ii)
$$x^2 - 1 + \frac{1}{4x^2}$$
, $(x \neq 0)$

(111)
$$\frac{1}{16}x^2 - \frac{1}{12}xy + \frac{1}{36}y^2$$

(iv)
$$4(a+b)^2 - 12(a^2-b^2) + 9(a-b)^2$$

(v)
$$\frac{4x^6 - (2x^3y^3 + 9y^6)}{9x^4 + 24x^2y^2 + 16y^4}, (x \neq 0)$$

(vi)
$$\left(x+\frac{1}{x}\right)^{2}-4\left(x-\frac{1}{x}\right), (x \neq 0)$$

(vii)
$$\left(x^{1} + \frac{1}{x^{1}}\right)^{2} - 4\left(x + \frac{1}{x}\right)^{2} + 12 (x \neq 0)$$

(viii)
$$(x^2+3x+2)(x^2+4x+3)(x^2+5x+6)$$

$$\frac{(y_1)}{(1x)} = \frac{(x^2 + 8x + 7)(2x^2 + x - 3)(2x^2 + 11x - 21)}{4x^2 - 12xy + 9y^2}$$

$$I(i) = 4x^2 - 12xy + 9y^2$$

Solution:
$$4x^2 + 9y^2 = 4x^2 - 6xy - 6xy + 9y^2$$

= $2x(2x - 3y) - 3y(2x - 3y)$
= $(2x - 3y)(2x - 3y)$
= $(2x - 3y)^2$

$$\sqrt{4x^2 - 12xy + 9y^2} = \pm (2x - 3y)$$

$$I(ii)$$
 $x^2-1+\frac{1}{4x^2}$, $(x \neq 0)$

Solution:
$$x^2 - 1 + \frac{1}{4x^2} = (x)^2 - 1 + \left(\frac{1}{2x}\right)^2$$

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MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone Mathematics $= (x)^2 - 2(x) \left(\frac{1}{2x}\right) + \left(\frac{1}{2x}\right)^2$ $=\left(x-\frac{1}{2x}\right)^2$ $\sqrt{x^2 - 1 + \frac{1}{4x^2}} = \pm \left(x - \frac{1}{2x}\right)$ $I(iii) = \frac{1}{16}x^2 - \frac{1}{12}xy + \frac{1}{36x^2}$ **Solution:** $\frac{1}{16}x^2 - \frac{1}{12}xy + \frac{1}{36v^2} = \left(\frac{1}{4}x\right)^2 + \frac{1}{12}xy + \left(\frac{1}{6v}\right)^2$ $-\left(\frac{1}{4}x\right)^2-2\left(\frac{1}{4}x\right)\left(\frac{1}{6y}\right)+\left(\frac{1}{6y}\right)^2$ $=\left(\frac{1}{4}x - \frac{1}{6y}\right)^2$ $\sqrt{\frac{1}{16}}x^{2} - \frac{1}{12}xy + \frac{1}{36y^{2}} = \pm \left(\frac{x}{4} - \frac{1}{6y}\right)$ $I(iv) = 4(a+b)^2 - 12(a^2 - b^2) + 9(a-b)^2$ = $[2(a+b)]^2$ $i2(a+b)(a+b) + [3(a+b)]^2$ Solution: = $[2(a + b)]^2$ -(2)(2)(a + b)(3)(a-b) + [3(a-b)]ЫŽ $= [2(a+b) - 3(a-b)]^2$ $= (2a + 22b + 3a + 3b)^2$ = [5b - a]2 $\sqrt{4(a+b)^2-12(a^2-b^2)+9(a-b)^2} = \pm (5b-a)$ $I(v) = \frac{4x^4 - 12x^3y^3 + 9y^6}{9x^4 + 24x^2y^2 + 16y^4}, (x = 0)$

Pilot Superone Mathematics $=\frac{(2x^3)^3-2(2x^3)(3y^3)+(3y^3)^2}{(3x^2)^2+2(3x^2)(4y^3)+(4y^2)^2}$ $=\frac{(2x^{1}+3y^{2})^{2}}{(3x^{2}+4y^{2})^{2}}$ $\frac{4x^6 - 12x^3y^3 + 9y^6}{9x^4 + 24x^2y^2 + 16y^4} = \left(\frac{2x^3 - 3y^3}{3x^2 + 4y^2}\right)^2$ $\sqrt{\frac{4x^6 - 12x^3y^3 + 9y^6}{9x^4 + 24x^3y^2 + 16y^4}} = \pm \frac{2x^3 + 3y^3}{3x^3 + 4y^2}$ $I(vi) = \left(x + \frac{1}{v}\right)^2 - 4\left(x - \frac{1}{v}\right), (x \neq 0)$ **Solution:** Let $x + \frac{1}{x} = R$ Now $\left(x + \frac{1}{x}\right)^2 = \left(x - \frac{1}{x}\right)^2 + 4$ $= (a^2 + 4) - 4a$ (Given expression) = m² 4a + 4 #(a 2)² $= \left[\left(\begin{array}{cc} x & 1 \\ x & 1 \end{array} \right) - 2 \right]$ $\left(x+\frac{1}{x}\right)^2 = 4\left(x-\frac{1}{x}\right) = -\left[\left(x-\frac{1}{x}\right)-2\right]^2$ $\sqrt{\left(x+\frac{1}{x}\right)^2-4\left(x-\frac{1}{x}\right)}=\pm\left[\left(x-\frac{1}{x}\right)-2\right]$

Plot Superone Mathematics 295 (lass 9th I(vii)
$$\left(x^2 + \frac{1}{x^2}\right)^2 - 4\left(x + \frac{1}{x}\right)^2 + 12$$

Solution: Let $x + \frac{1}{x} = a$ (A)
$$\left(x + \frac{1}{x}\right)^2 = a^2$$
 (Squaring)
$$x^2 + \frac{1}{x^2} + 2 = a^3$$

$$x^2 + \frac{1}{x^2} = a^3 - 2$$
 (B)
$$\left(x^3 + \frac{1}{x^2}\right)^2 - 4\left(x + \frac{1}{x}\right)^2 + 12 = (a^2 - 2)^2 - 4a^2 + 12 \text{ (From A.B)}$$

$$\frac{1}{x^2} = a^4 - 4a^2 + 4 - 4a^2 + 12$$

$$\frac{1}{x^2} = a^4 - 8a^2 + 16$$

$$\frac{1}{x^2} = a^3 - 2a^2 + 16$$

$$\frac{1}{x^2} = a^3 - 2a^3 + 12 = a^3 + 12 =$$

Pilot Superone Mathematics 296 Class 9th

$$= (x + 2)(x + 1)(x + 1)(x + 3)(x + 2)(x + 3)$$

$$= (x + 1)^{2} (x + 2)^{2} (x + 3)^{2}$$
Taking square root
$$\sqrt{(x + 1)^{2}(x + 2)^{2}(x + 3)^{2}} = (x + 1)(x + 2)(x + 3)$$

$$1(ix) \quad (x^{2} + 8x + 7)(2x^{2} - x - 3)(2x^{2} + 11x - 21)$$
Solution:
$$= (x^{2} + x + 7x + 7)[2x^{2} - 3x + 2x - 3)[2x^{2} + 14x - 3x - 21]$$

$$= (x(x + 1) + 7(x + 1))[x(2x - 3) + 1(2x - 3)][2x(x + 7) - (x + 7)]$$

$$= (x + 1)(x + 7)(2x - 3)(x + 1)(x + 7)(2x - 3)$$

$$= (x + 1)^{2} (x + 7)^{2} (2x - 3)^{2}$$
Taking square root
$$\sqrt{(x + 1)^{2}(x + 7)^{2}(2x - 3)^{2}} = (x + 1)(x + 7)(2x - 3)$$
Q.2 Use division method to find the square root of the following expression.
(i)
$$4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$
(ii)
$$x^{4} - 10x^{3} + 37x^{2} - 60x + 36$$
(iii)
$$9x^{4} - 6x^{3} + 7x^{2} - 2x + 1$$
(iv)
$$4 + 25x^{3} - 12x - 24x^{3} + 16x^{4}$$
(v)
$$\frac{x^{2}}{y^{2}} - 10 \frac{x}{y} + 27 - \frac{10y}{x} + \frac{y^{2}}{x^{2}}, (x \neq 0, y \neq 0)$$

$$2(i) 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$
Solution.
$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 4x^{2} + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 12xy + 9y^{2} + 16x + 24y + 16$$

$$2x + 3y + 4 + 12xy + 3y + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y + 4x + 16x + 24y + 16$$

$$2x + 3y +$$

Square root = 2x + 3y + 4

Pilot Superono	Mathematics 297	Class 9 th
	$x^3 + 37x^2 - 60x + 36$	_
Solution.	$ \begin{array}{r} x^2 - 5x + 6 \\ x^4 - 0x^3 + 37x^2 - 60x + 36 \\ \pm 4x^4 \\ \hline 10x^3 + 37x^2 \\ - 10x^3 \pm 25x^2 \\ \hline 12x^2 - 60x + 36 \\ \pm 12x^2 - 60x \pm 36 \end{array} $	
x ²	$x^4 = 0x^3 + 37x^2 = 60x + 36$	
- 1 -	±4x4	
2x" 5x	$10x^3 + 37x^2$	_
$2x^2 = 10x + 6$	$\frac{-10x^2 \pm 25x^2}{12x^2 + 12x^2}$	
rux r u	12x 00x + 36 + 12x2 60x + 36	
	1 = 123 - 50X ± 36	_
Square	$root = x^2 - 5x + 6$	
2000 aut c.	3 , 7, 2 , 4 , 4	
Solution:	$3x^2 - x + 1$	
3x²	$9x^{4} - 6x^{3} + 7x^{2} - 2x + 1$	_
6x² x	$ \begin{array}{r} 3x^{2} - x + 1 \\ 9x^{3} - 6x^{3} + 7x^{2} - 2x + 1 \\ \pm 9x^{4} \\ \hline 6x^{3} + 7x^{2} \\ - 6x^{3} \pm x^{2} \\ \hline 6x^{2} - 2x \pm 1 \\ \pm 6x^{2} - 2x \pm 1 \end{array} $	_
$6x^2 - 2x + 1$	- 0x' ± x'	
	$\begin{array}{c} 0x - 2x + 1 \\ \pm 6x^2 - 2x + 1 \end{array}$	
	×	_
Square r	$3x^2 - x + 1$	
$2(iv) = 4 + 25x^2$	$-1/2x - 24x^3 + 16x^4$	
Solution.	$-4x^2 - 3x + 2$	
4x ²	$ \begin{array}{r} 4x^2 - 3x + 2 \\ 16x^4 - 24x^3 + 25x^2 - 12x + 4 \\ \pm 16x^4 \\ \hline 24x^3 + 25x^2 \\ -24x^3 \pm 9x^2 \end{array} $	_
	± 16x4	_
8X 3x	$24x^3 + 25x^2$	
$8x^2 - 6x + 2$		_
VII. 7	$ \begin{array}{r} $	
'	×	_
Square ro	$xot = 4x^2 - 3x + 2$	
$2(v) = \frac{x^2}{y^2} - 10\frac{x}{y}$	$+27-\frac{10y}{x}+\frac{y^2}{x^2}$, $(x \neq 0, y \neq 0)$	

Solution: Writing in descending order

Pilot Superone	Mathematics 298	Class 9th
	$\frac{2}{y}$ - 5 + $\frac{y}{x}$	
<u>*</u>	$\frac{x^{j}}{y^{j}} - \frac{10x}{j} + 27 \cdot \frac{10y}{x} + \frac{y^{j}}{x^{j}}$	
	- *'	
2x -5	+ 10x + 27	
,	. <u>10x</u> + 25	
İ	+ 7	
$\frac{2x}{y} \cdot 10 + \frac{y}{x}$	$2 - \frac{10y}{x} + \frac{y^2}{x^2}$	•
	$2 \cdot \frac{10y}{x} + \frac{y^2}{x^2}$	
	<u> </u>	

Square root $\frac{\lambda}{v}$ 5 + $\frac{y}{x}$

Q3 Find the value of k for which the following expressions will become a perfect square.

(i)
$$4x^4 - 12x^3 + 37x^2 - 42x + k$$

(ii) $x^4 - 4x^3 + 10x^3 - kx + 9$

(ii)
$$x^4 - 4x^3 + 10x^3 + kx + 9$$

$$3(i) = 4x^4 - 12x^3 + 37x^2 - 42x + k$$

Solut on: Taking square root

In case of perfect square, remainder is zero

Therefore 1 49 = 0

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Pilor Superone Mathematics and k = 49 $3(ii) = x^4 - 4x^3 + 10x^2 - kx + 9$ Solution Taking square root ± 6x² 7 12x ± 9 in case of perfect square -kx + 12 = 0x(k-12) = 0k 12 = 0k = 12Q.4 Find the value of I and m for which the following expressions will become perfect square. (i) $x^4 + 4x^3 + 16x^2 + 2x + m$ $49x^4 - 70x^3 + 109x^2 - I_X - m$ (ii) $x^4 + 4x^3 + 16x^2 - Ix + m$ 4(1) Solution: Taking square root

In case of perfect square, remainder is zero

MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone	Mathematics	300	Class 9th
Ix 2	24x = 0		
	24) = 0		
	24 = 0	$\mathbf{x} = 0$	
	/ = 24		
and m -	36 = 0		
-	m = 36		
4(ii) 49x ⁴ - 1	70x³ + 109x² -	y u	
	T 1	ma mil	
	$x^2 + 2x +$	6	<u> </u>
7x ²	$49x^4 - 70x^2$	$^{3} + 109x^{2} - hx$	m
14.2 E	± 49x*	3 + 109x2	
14X - 3X	70x	$^{3} \pm 25x^{2}$	
14x ² -10x+6		$ \frac{6}{3 + 109x^2 - lx} = \frac{3 + 109x^2 - lx}{3 + 25x^2} = \frac{84x^2 + lx}{40x^3 + (x^2 - 60x)} $	m
	\	$\pm 84x^2 - 60x$	<u>± 36</u>
	A:)	יור)י (אטט -	,
		are, remainder is	2010
	60x = 0		
•	► 60) = 0	- 0	
,		x = 0	
	! - 60		
and –m≀	-36 = 0		
	m =36		
	m = 36	. 6.4 13.3.	22-2 13-412
~		ion 9X - 12X +	$22x^2 - 13x + 12$
	ect square What should	be added to it?	
<i>(i)</i>		be subtracted fr	om it?
(II)		be the value of:	
(iii) Solution:	Texing squar		
Solution:	3x ² - 2x		

Written/Composed by SHAHZAD IFTIKHAR Contact # 03.3.3-5665666 Website www.downloadclassnotes.com , F-mail raoshahzadiftikhar@gmail.com

MATHEMATICS FOR 9TH CLASS (UNIT # 6)

Pilot Superone	Mathematics 301	Class 9th
3x²	$9x^4 - 12x^3 + 22x^2 - 13x + 12$ $\pm 9x^4$	
14x2 - 5x	$ \begin{array}{r} 12x^3 + 22x^2 \\ \pm 12x^3 \pm 4x^2 \end{array} $	-
14x ² 10x+6		•
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	

- (i) What should be subtracted, remainder should be subtracted i.e. x + 3
- (ii) What should be added. Negative of remainder should be added i.e. x 3
- (iii) To find x, put remainder equal to zero. x - 3 = 0x = 3

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Pilot Superone Mathematics 310 Class 9"



LINEAR EQUATIONS AND INEQUALITIES

Linear Equations

A linear equation is one unknown variable x is an equation of the form ax + b = 0, where $a, b \in \mathbb{R}$ and $a \neq 0$

Radical Equations

When the variable in an equation occurs under a radical the equation is called a radical equation.

Exercise 7.1

Q.1 Solve the following equations.

(i)
$$-\frac{2}{3}x + \frac{1}{2}x + x + \frac{1}{6}$$
 (ii) $-\frac{x-3}{3} + \frac{x-2}{2} = I$

(iii)
$$\frac{1}{2} \left(x - \frac{1}{6} \right) + \frac{2}{3} = \frac{5}{6} + \frac{1}{3} \left(\frac{1}{2} - 3x \right)$$

(iv)
$$x + \frac{1}{3} = 2\left(x - \frac{2}{3}\right) - 6x$$

(v)
$$\frac{5(x-3)}{6}$$
 $x=1-\frac{x}{9}$

(vi)
$$\frac{x}{3x-6} = 2 + \frac{2x}{x-2}, x \neq 2$$

(vii)
$$\frac{2x}{2x+5}$$
 $\frac{2}{3}$ $\frac{5}{4x+10}$ $x \neq \frac{5}{2}$

(viii)
$$\frac{2x}{x+1} + \frac{1}{3} = \frac{5}{6} + \frac{2}{x-1}, x \ne 1$$

(ix)
$$\frac{2}{x^2-1} = \frac{1}{x+1}, x \neq \pm 1$$

Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>raoshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 7)

Pilot Superone Mathematics 311 Class 9th

(x)
$$\frac{1}{3}x + 6 = 6 = 2x + 4$$

I(i) $\frac{2}{3}x + \frac{1}{2}x + \frac{1}{6}$

1. C. M. of 2. 3. 6 is 6 multiplying by 6

Solution: (6) $\frac{2}{3}x + \frac{1}{6}x + \frac{1}$

Pilot Superone Mathematics 312 Class 9th 12
$$\left(\frac{x}{7}\right)$$
 - 12 $\left(\frac{1}{12}\right)$ + 12 $\left(\frac{2}{3}\right)$ - 12 $\left(\frac{5}{6}\right)$ + 12 $\left(\frac{1}{6}\right)$ - 12(x)

6x 1 + 8 10 + 2 - 12x
6x + 12x = 10 + 2 + 1 8
18x = 5
$$x = \frac{5}{18}$$
Solve
$$x = \left\{\frac{5}{18}\right\}$$
I(iv) $x + \frac{1}{3} = 2\left(x - \frac{2}{3}\right)$ - 6x

Solve
$$x + \frac{1}{3} = 2x - \frac{4}{3} - 6x$$
Multiplying by 3
$$3x + 3\left(\frac{1}{3}\right) = 3(2x) - 3\left(\frac{4}{3}\right) - 3(6x)$$

$$3x + 1 = 6x - 4 - 18x$$

$$3x - 6x + 18x = -4 - 1$$

$$15x = 5$$

$$x = -\frac{5}{15}$$

$$x = -\frac{1}{3}$$
Solve set
$$x = \left\{-\frac{1}{3}\right\}$$

 $I(x) = \frac{5(x-3)}{6} - x = 1 - \frac{x}{9}$

Selection: L.C.M. of 6, 9, is 18 multiplying by 18

Pilox Superone Mathematics 313
$$\frac{18(5)(x-3)}{6} - 18x = 18 - 18\left(\frac{x}{9}\right)$$

$$15(x-3) - 18x = 18 - 2x$$

$$15x - 45 - 18x = 18 - 2x$$

$$15x - 18x + 2x = 18 + 45$$

$$-x = 63$$

$$x = -63$$
Solve set
$$x = \frac{1}{6} = \frac{1}{3}$$

$$I(vi) = \frac{x}{3x-6} = 2 - \frac{2x}{x-2}, x \neq 2$$
Solution:
$$\frac{x}{3x-6} + \frac{2x}{x-2} = 2$$

$$\frac{x+3(2x)}{3(x-2)} = 2$$
Multiplying by $2(x-2)$

$$7x = 2(3)(x-2)$$

$$7x = 6(x-2)$$

$$7x = 6x - 12$$

$$7x - 6x = -12$$

$$x = 12$$
Solve Set
$$x = \frac{1}{2}$$

$$x = 12$$
Solve Set
$$x = \frac{1}{2}$$

$$x = -12$$

$$x = 12$$
Solve Set
$$x = \frac{1}{2}$$

$$x = \frac{1}{2}$$
Solution:
$$\frac{2x}{2x+5} = \frac{2}{3} - \frac{5}{4x+10}, x \neq -\frac{5}{2}$$
Solution:
$$\frac{2x}{2x+5} + \frac{5}{4x+10} = \frac{2}{3}$$

$$\frac{2x}{2x+5} + \frac{5}{2(2x+5)} = \frac{2}{3}$$

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MATHEMATICS FOR 9TH CLASS (UNIT # 7)

Pilot Superone Mathematics 314 Class 9th

$$\frac{2(2x)+5}{2(2x+5)} = \frac{2}{3}$$

$$4x+10 = 2(2x+5)$$
Multiplying by $2 \times 3(2x+5)$

$$2 \times 3(2x+5) \left(\frac{4x+10}{2(2x+5)}\right) = \frac{2}{3} \times 2 \times 3 \times (2x+5)$$

$$3(4x+5) - 4(2x+5)$$

$$12x+15 = 8x+20$$

$$12x-8x = 20 - 15$$

$$4x = 5$$

$$x = \frac{5}{4}$$
Solve Set
$$x = \left\{\frac{5}{4}\right\}$$
I(viti) $\frac{2x}{x-1} + \frac{1}{3} = \frac{5}{6} + \frac{2}{x-1}, x \neq 1$
Solution: $\frac{2x}{x-1} = \frac{5}{6} - \frac{1}{3}$

$$\frac{2x-2}{x-1} = \frac{5-2}{6}$$

$$\frac{2(x-1)}{x-1} = \frac{3}{6}$$

$$2 = \frac{3}{6}$$

Solution is not possible

Pilot Superone Mathematics 315	Class 9th
$f(ix) = \frac{2}{x^2 - 1} - \frac{1}{x + 1} = \frac{1}{x + 1}, x \neq \pm 1$	
Solution: $\frac{2}{(x+1)(x-1)} - \frac{1}{x+1} = \frac{1}{x+1}$	
Multiplying by $(x + 1)(x - 1)$	
$\frac{2(x+1)(x-1)}{(x+1)(x-1)} - (x+1)(x-1)x \frac{1}{x+1} = (x+1)(x-1)x$	<u> </u>
2(x-1) = x-1	
2 - x + 1 = x [
$x \cdot x = 1 \cdot 2 \cdot 1$	
2x = -4	
$x = \frac{-4}{2}$	
x = 2	
Solve Set x = {2}	
$I(x) = \frac{2}{3x+6} = \frac{1}{6} - \frac{1}{2x+4}, x \neq -2$	
Solution: $\frac{2}{3(x+2)} = \frac{1}{6} - \frac{1}{2(x+2)}$	
$\frac{2}{3(x+2)} + \frac{1}{2(x+2)} = \frac{1}{6}$	
$\frac{2 \times 2 + 1 \times 3}{6(x+2)} = \frac{1}{6}$	
$\frac{4+3}{6(x+2)} = \frac{1}{6}$	
Multiplying by 6(x + 2)	
7 + x + 2	
x -7 2	
x = 5	

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MATHEMATICS FOR 9TH CLASS (UNIT # 7)

Pilot Superone Mathematics 316 Soire each equation and check for extraneous solution, if any: (ii) $\sqrt[4]{2x-4} - 2 = 0$ $\sqrt{3x+4} = 2$ (iii) $\sqrt{x-3}-7=0$ (iv) $2\sqrt{t+4}=5$ (v) $\sqrt[3]{2x+3} = \sqrt[3]{x-2}$ (vi) $\sqrt[3]{2-1} = \sqrt[3]{21-28}$ (vii) $\sqrt{2t+6} - \sqrt{2t-5} = \theta$ (viii) $\sqrt{\frac{x+1}{2x+5}} = 2x + \frac{5}{2}$ $\sqrt{3x+4}=2$ 2(1) $\left(\sqrt{3x+4}\right)^2 = (2)^2 \qquad \text{(Squaring)}$ Solution: 3x + 4 = 43x = 4 43x = 0 $\mathbf{x} = \mathbf{0}$ $\sqrt[4]{2x-4} - 2 = 0$ $\sqrt[3]{2x} = 2$ Solution: $(2x-4)^{1/3}=2$ $\{(2x-4)^{1/3}\}^3 = (2)^3$ (Cubing) $(2x-4)^{1/3+3} = 8$ 2x - 4 = 82x = 8 + 42x = 12 $x = \frac{12}{2}$ x ~6

Pilot Superone Mathematics 317 Class 9th 2(iii)
$$\sqrt{x-3} - 7 = 0$$

Solution: $\sqrt{x} = 7$ ($(x-3)^{\frac{y_1}{2}} = 7$) (Squaring) ($(x-3)^{\frac{y_2}{2}} = 49$ $(x-3)^{\frac{y_3}{2}} = 5$ $(x-3)^{\frac{y_3}{2}} = 5$ (Squaring) ($(x-4)^{\frac{y_3}{2}} = 5$ (Squaring) 4($(x-4)^{\frac{y_3}{2}} = (5)^2$ (Squaring) 4($(x-4)^{\frac{y_3}{2}} = (5)^2$ (Squaring) 4($(x-4)^{\frac{y_3}{2}} = (5)^2$ (Squaring) 1 = $\frac{9}{4}$ (Cubing) ($(2x+3)^{\frac{y_3}{2}} = (x-2)^{\frac{y_3}{2}}$ (Cubing) ($(2x+3)^{\frac{y_3}{2}} = (x-2)^{\frac{y_3}{2}}$ (Cubing) ($(2x+3)^{\frac{y_3}{2}} = (x-2)^{\frac{y_3}{2}}$ ($(2x+3)^{\frac{y_3}{2}} = ($

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Pilot Superone Mathematics 318 Class 9th 2(vii)
$$\sqrt{2}-1-\sqrt[3]{21-28}$$

Solution: $\sqrt[3]{2-1} = \sqrt[3]{21-28}$

or $(2-1)^{1/3} = (21-28)^{1/3}$
 $[(2-t)^{1/3}]^3 = [(21-28)^{1/3}]^3$
 $[(2-t)^{1/3}]^3 = (21-28)^{1/3-3}$
 $[(2-t)^{1/3}]^3 = (21-28)^{1/3}$
 $[(2-t)^{1/$

Pilot Superone Mathematics 319 Class
$$9^{th}$$

$$\left[\left(\frac{x+1}{2x+5} \right)^{\frac{1}{2}} \right]^{2} = (2)^{2} \qquad \text{(Squaring)}$$

$$\left(\frac{x+1}{2x+5} \right) = 4$$
Multiplying $2x+5$

$$\left(\frac{x+1}{2x+5} \times 2x+5\right) = 4 \times (2x+5)$$

$$x+1 = 4(2x+5)$$

$$x+1 = 8x+20$$

$$x = 8x = 20-1$$

$$7x = 19$$

$$x = -\frac{19}{7}$$

Equation Involving Absolute Value

Another type of linear equation is the one that contains absolute value. To solve equations involving absolute value we first give the following definition.

Definition

The absolute of a real number 'a' denoted by [a], is defined as

|a| = a, if
$$a \ge 0$$

= -a, if $a < 0$
e.g., $|6| = 6$, $|0| = 0$ and $|-6| = 6$

Some properties of absolute value

If a, b ∈ R, then

(i)
$$|a| \ge 0$$
 (ii) $|-a| = |a|$

(iii)
$$|ab| = |a| \cdot |b|$$
 (iv) $\left| \frac{a}{b} \right| - \frac{|a|}{|b|}, b \neq 0$

Pilot Superone Mathematics 320

Class 9th

Exercise 7.2

- Identify the following statements as True of False. 0.1
 - $|\mathbf{x}| = 0$ has only one solution. (i)
 - All absolute value equations have two solution. (ii)
 - The equation |x| = 2 is equivalent to x = 2 or x = -2. (iii)
 - The equation |x 4| = -4 has no solution. (iv)
 - The equation |2x 3| = 5 is equivalent to 2x 3(v) = 5 or 2x + 3 = 5.

Answers:

1	(A)	Tr -	(an)	Ł.	(iii)	т	(iv)	Ţ	(v)	F	
	(4)	1.1	(ii)	P	(HH)	 	(tv)	1	117	<u>'</u>	J

Solve for x: 0.2

(i)
$$|3x - 5| = 4$$

(ii)
$$\frac{1}{2}|3x+2|-4=$$

П

(iii)
$$|2x+5|=11$$

(iv)
$$|3+2x|=|6x-7|$$

$$|x+2|-3=5-|x+2|$$
 (vi) $\frac{1}{2}|x+3|+21=9$

(vii)
$$\left| \frac{3}{4} \right| - \frac{1}{3} = \frac{2}{3}$$
 (viii) $\left| \frac{x+5}{2-x} \right| = 2$

(viii)
$$\left| \frac{x+5}{2-x} \right| = 2$$

$$2(i)$$
 $|3x-5|=4$

$$|3x - 5| = 4$$

$$3x = 4 + 5$$

$$x = \frac{9}{3}$$

$$x = 3$$

$$-(3x-5) = 4$$

$$3x-5 = -4$$

$$3x = -4 + 5$$

$$3x = 1$$

$$x - \frac{1}{3}$$

$$=\left\{3,\frac{1}{3}\right\}$$

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Pilot Super	one Mathematics 321	Class 9th
2(ii) 1 p	3x + 2 -4 = EE	
Solution:	$\frac{1}{2} 3x+2 = 11+4$	-
	$\frac{1}{2} 3x+2 =15$	
Now	3x + 2 = 30	(Multiplying by 2)
	3x + 2 = 30	-(3x + 2) = 30
	3x 30 2	3x + 2 - 30
	3x = 28	3x = 30 2
	$x = \frac{28}{3}$	3x = -32
	. 3	$x - \frac{-32}{3}$
	Sol. Set $=$ $\left\{ \frac{28}{3}, \frac{-32}{3} \right\}$	}
2(iii) 2x	· 5 = 11	
Solution:	2x + 5 = 11	(2x+5) = 11
	2x = 11 S	2x + 5 = 11
	2x = 6	$2x = -11 \cdot 5$
	$x = \frac{6}{2}$	2x = -16
	-	$x = \frac{-16}{2}$
	x = 3	_
	Cat Cara to the	x = 8
2/ha 13 4 1	Sol. Set = {3, 8}	
2(iv) 3 + ? Solution:	2x(= xx-7 3+2x=6x,7	1.5
	3+7 = 6x - 7 3+7 = 6x - 2x	3 + 2x = -(6x 7) 3 + 2x = 6x + 7
		2x + 6x = 7 3

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Pilot Superone Mathematics 322	Class 9 th
Hot super-	8x 4
$\mathbf{x} = \frac{10}{4}$	4
	$x - \frac{4}{8}$
$x = \frac{5}{2}$	1
2	x - 2
Sol Set $\left\{\frac{5}{2}, \frac{1}{2}\right\}$	
2(v) = (x+2)-3=5 - (x+2)	
Solution: $ x + 2 + x + 2 - 5 + 3$	
2 x+2 =8	
Dividing by 2	
x + 2 4	(x+2)=4
$\begin{array}{cccc} x+2&-4\\ x&4&2 \end{array}$	x+2 = 4
x = 2	x = 4 2
	x 6
Sol. Set = {2, -6}	
$2(vi) = \frac{1}{2} x+3 +21 = 9$	
Solution: $\frac{1}{2} x+3 = 9 - 21$	
$\frac{1}{2} x+3 = 12$	
x+3 = 24	(Multiplying by 2)
Sol. Set * \$	
(Absolute value is never negative)	
$2(vii) \frac{3}{4} \frac{5x}{3} = \frac{2}{3}$	
Solution: $\frac{\left \frac{3-5x}{4}\right -\frac{1}{3}}{4}=\frac{2}{3}$	
$\frac{ 3-5x }{4} - \frac{2}{3} + \frac{1}{3}$	

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MATHEMATICS FOR 9TH CLASS (UNIT # 7)

Pilot Superone Mathematics 3	23(.lass 9 th
$\left \frac{3-5x}{4}\right = 1$	
Now $\frac{3-5x}{4}$	3 52 1
and	3 - 5x
3 5x 4 -5x 4 3 5x 1	4
$x = -\frac{1}{5}$	3 5x 4 5x 4 3 5x 7 x 7 x 5
Sol Ser * 1	5 5
$2(viii) \left \frac{x+5}{2-x} \right = 6$	
Solution: $\frac{x+5}{2-x} = 6$ $\frac{x+5}{x+5} = 6(2-x)$ $\frac{x+5}{x+5} = 12-6x$	$\left(\frac{\frac{5+5}{2+3}}{2+3}\right) = 6$
x + 6x 12 5 7x 7 x 1	2 x × 1.5 6(2 x) × 1.5 12 6x
	x 6x 12 5 5x 17 x 17
Sol Set = $\begin{cases} L \frac{1}{2} \end{cases}$	7 }

Defining Inequalities

Let a, b be real numbers. Then a is greater than b if the difference a, b is positive and we denote this order relation by the inequality a > b. An equivalent statement is that b is less

Pilot Superone Mathematics 324 Class 9^{th} than a symbolized by b a Similarly, if a b is negative, then a is less than b and expressed in symbols as a < b.

Properties of Inequalities

1. Law of Trichotomy

For any $a,b\in\mathbb{R}$, one and only one of the following statements is true

a √ b or a b, or a > b

An important special case of this property is the case for b = 0, namely

a · o or a O ora > O foranya ∈ R.

2. Transitive Property

Let a, b, c ∈ R

- (i) If a + b and b ≥ c, then a > c
- (ii) If a s b and b s c, then a s c

3. Additive Closure Property

For a, b, c ∈ R.

- (i) If a + b, then a + c > b + c If a < b, then a + c < b + c
- (ii) If a > 0 and b > 0, then a + b > 0(If a < 0 and b < 0, then a + b < 0

4. Muttiplicative Property

leta, b, c, d e R

- (i) If $a \ge 0$ and $b \ge 0$, then $ab \ge 0$. whereas $a \le 0$ and $b \le 0 \Rightarrow ab \ge 0$
- (11) If a > b and c > 0, then ac > bc or if a < b and c > 0, then ac < bc
- (iii) If a > b and c < 0, then ac < bcor if a < b and c < 0, then ac > bc

The above property (iii) states that the sign of inequality is reversed if each side is multiplied by a negative real number

(iv) If a > b and e > d, then ac > bd

Pilot Superone Mathematics 325 lass 9th

Exercise 7.3

Solve the following inequalities. 0.1

(i)
$$3x + 1 < 5x - 4$$

(i)
$$3x + 1 < 5x - 4$$
 (ii) $4x + 10.3 \le 21x + 1.8$

3 2

(v)
$$\frac{3x+2}{9} \cdot \frac{2x+1}{3} > -1$$

(vi)
$$3(2x+1) - 2(2x+5) < 5(3x-2)$$

(vii)
$$3(x-1) - (x-2) > -2(x+4)$$

(viii)
$$2\frac{2}{3}x + \frac{2}{3}(5x + 4) > -\frac{1}{3}(8x + 7)$$

$$I(i) = 3x + 1 > 5x - 4$$

Solution ·

$$3x + 1 - 5x + 5x + 4 - 5x$$

 $-2x + 1 < 4$

$$3x \cdot 1 < 4$$

$$2x+1 < 4$$

$$-2x+1 + 1 + 4 + 1$$

$$|x| \ge \frac{5}{2} - NAS$$
 change of sign

Sol. Set =
$$\{x|x > \frac{5}{2}\}$$

$$I(n) = 4x - 10.3 \le 21x - 1.8$$

Solution:

(Subtracting 21x)

$$17x - 10.3 + 10.3 \le 1.8 + 10.3$$
 (Adding 10.3)
 $17x \le 8.5$

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Pilot Superone Mat	hematics	326	Class 9 th
	NIS	Dividing by	17 (change of sign)
	x	$> \frac{8.5}{-17}$	
		, ,	
		≥ ⋅ 5	
	Sol. Set	{x x ≥.	5}
$I(iii) 4 - \frac{1}{2} x \ge -$	-7 + ¹ x		•
Solution:	$4 - \frac{1}{2}x$	· 7 + 1 x	1
Multiplying	g by 4		
	16 2x	> 28 + m	
Subtracting	g by N		
16	6 2x x	> 28 + x	x
	16 3x	> 28	
Subtracting	g by 16		
16	3x 16	≥ 28 10	\$
		≥ 44	
Subtracting	g by 3		•
	X	≤ -44	N T.S (change of
sign)			
	,	$\frac{44}{3}$	
	Sol Se	ı = {x x <	⁴⁴ ₃ }
!(iv) x 2(5 -	2x) > 6x 3	$3\frac{1}{2}$	
Solution: x	2(5 - 2x) ≥ 6x - 3	-

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Pilot Superone Mathematics 327 Class 9th					
$x = 10 + 4x \ge 6x = \frac{7}{2}$					
Multiplying by 2					
2x - 20 + 8x > 12x - 7					
10x - 20 > 12x - 7					
Sobracting 12x					
10x - 20 - 12x > 12x - 7 - 12x					
2x 20 ≥ 7					
Adding 20					
$-2x - 20 + 20 \ge 7 + 20$					
-2x ≥ f3					
Dividing by -2					
$x \le -\frac{13}{2}$ (change of sign)					
X 🐒 -6.5					
Sol Set $= \{x x \le 6.5\}$					
$I(v) = \frac{3x+2}{9} = \frac{2x+1}{3} > -1$					
Solution: Multiplying by 9					
$\frac{9(3x+2)}{9} - \frac{9(2x+1)}{3} > 1(9)$					
3x + 2 3(2x + 1) > 9					
$3x+2\cdot 6x 3 \ > \ 9$					
-3x 1 > -9					
-3x 1+1 > 9+1 (Adding 1)					
-3x > -R					
Dividing by -3 (change of sign)					
8					
$x < \frac{-8}{-3}$					
•					

Phot Superone Mathematics 328 Class
$$\frac{8}{3}$$
 $x < \frac{8}{3}$

I(vi) $3(2x + 1) - 2(2x + 5) < 5(3x - 2)$

Solution: $6x + 3 - 4x + 10 < 15x + 10$
 $2x - 7 < 15x + 10$

Subtracting 15x

 $2x - 7 + 15x < 15x + 10$

13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10$
13x $- 7 < 10 < 10$
13x $- 7 < 10$
14x $- 7 < 10$
2x $- 7 < 10$

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Pilot Superone Mathematics 330
Solution: 24 \times 2 \le 24 (Multiplying by 4) 24 + 2 \le x + 2 \le 24 + 2 (Adding 2)
2(iv) \quad 3 \ge \frac{7}{3} \times 2 1
Solution: 6 \ge 7 + x \ge 2 (Multiplying by 21 6 = 7 \ge 7 + x = 7 \ge 2 = 7 (Subtracting 7)
                Multiplying by -1 (change of sign)
                1 < x < 5
2(14) 3x 10 < 5 < x + 3
Solution: Here
    3x 10 < 5
                           3x = 10 + 10 < 5 + 10
3x < 15
    x < 5
        From (i) and (ii)
       2 \le x \le 15
2(vi) -3 \le \frac{x-4}{5} < 1
Solution: Multiplying by 5 (Change of sign)
               15 > x + 4 > -20
               15 + 4 > x 4 + 4 > 20 + 4 (Adding + 4)
               19 \ge x > 16
              -16 \le x \le 19
Οſ
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Pilot Superone Mathematics	331	Class 9th
$-2(vii) - 1 - 2x < 5 - x \le 25 - 6$	x	
Solution ·		
$1-2x \le 5-x$	5 - x < 25 6x	
1 - 2x + x < 5 - x + x	5 x + 6x < 25	6x + 6x
1 x < 5	5 + 5x < 25	
x < 5	5 + 5x - 5 < 25	5
-x < 4	5x ≤ 20	
or x > 4 ()	$\frac{5x}{5} < \frac{20}{5}$	
	x < 4	(11)
From (i) and (ii)		
4 < x < 4		
2(viii) 3x $2 < 2x + 1 < 4x +$	17	
Solution: Here		
3x 2 < 2x + t	2x+1<4x+1	,
3x + 2 + 1 < 2x + 1 + 1	2x+1 /<4x	+ 17 1
3x 3 < 2x	2x < 4x + 16	
3x 2x 3 < 2x 2x	2x + 4x < 4x + 1	6 4x
x 3 < 0	2x < 16	
x 3 + 3 < 0 + 3	Dividing by 2 (Chang	te of sign)
x ≤ 3 (i)	$x > \frac{16}{-2}$	
	x > 8	(ii)
From (1) and (1i)		• •
-8 < x < 3		

Pilot S	uperon	ie Mathematic	33	2 Class 9 th		
		Reviev	e Exer	cise 7		
Q.I	Multi	ple choice que	stion, ch	oose the correct answers.		
(4)	The second secon					
3 4x - 112						
	(a)	8	(b)	2		
	(c)	14 4	d)	None of these		
(ii)	A state		ng any of	f the symbols *** *§≤ or ≥ is		
	(a)	equation	(b)	identity		
	(c)	inequality	(d))mean equation		
(10)	`	18 a 80	dution of	the inequality $ 2 \le \frac{3}{2}$.		
	(a)	5	(b)	3		
	(c)	U	(d)	; ;		
(iv)	Hist	s no larger tha	n it), ther	1		
	(a)	× × 8	(b)	$\Delta = 10$		
	(c)	x+ 10	(0)	s 10		
(v) If the capacity c of an elevator is at most 1600 pounds, then						
	(a)	c < 1600	(b)	e · 1600		
	(c)	$\epsilon \le 1600$	(b)	c > 1600		
(33)	A 1	Ers a solution o	of the ime	quality		
	(8)	× 0	(b)	3x 5 = 0		
	101	$x \cdot 2 \le 0$	(d)	x 2 · 0		
inse	rc/S?					
(i)	b	(ii) (C	(iii)	(iv) b		
0)	ď	<i>. mip</i> d	•	in b		
				==		

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MATHEMATICS FOR 9TH CLASS (UNIT # 7)

Pilot Superone Mathematics 333 Class 9th

- Q.2 Identify the following statements as True or False.
 - the equation 3x 5 7 x is a linear equation.
 - (ii) The equation x 0.3x 0.7x is an identity
 - (iii) The equation 2x + 3 8 is equivalent to 2x 11,
 - (iv) To elin mate fractions, we multiply each side of an equation by the LCM or denominators
 - (v) 4(x+3) x+3 is a conditional equation
 - (vi) The equation 2(3x + 5) = 6x + 12 is an inconsistent equation
 - (vii) To solve $\frac{2}{3}x = 12$, we should multiply each side by $\frac{2}{3}$
 - (viii) Equations having exactly the same solution are called equivalent equations
- (ix) A solution that does not satisfy the original equation is called extrareous solution.

Ansı	vers:							
(1)	True	[av]	frue	(iii)	False	(lv)	True	1
(v)	True	(vi)	True	(vii)	False	(viii)	True	1
(ix)	True]				<u> </u>	1

- Q.3 Answer the following short question.
- Define a linear inequality in one variable.
- (ii) State the trichotomy and transitive properties of inequalities.
- (iii) The formula relating degrees Fahrenheit to degrees Celsius is $F = \frac{1}{4}C + 32$. For what value of C is F < 0?
- (iv) Seven times the sum of an integer and 12 is at least 50 and at most 60. Write and solve the inequality that expresses this relationship.

Pilot Superone Mathematics 334 Class 9th

- (i) A linear nequality in one variable x is ax + b < 0, a \neq 0
- (ii) Trichotomy Property.

 $\forall a, b \in \mathbb{R}$, one and only one of the following statement is true

asbora bora>b

if b 0 then a < 0 or a 0 or a > 0 for any $a \in \mathbb{R}$.

Transitive Property:

 $\forall a, b, c \in R$

- (i) 16a > b and b > c then a > c
- (ii) If a < b, and b < c then a < c

(iii)
$$+ \frac{9}{5}C + 32 < 0$$

$$C < 32 \times \frac{5}{\parallel}$$

$$C < \frac{160}{9}$$

(iv) Let the integer - x

According to the conditions

$$50 \le 7(x + 12) \le 60$$

Solution: $50 < 7x + 84 \le 60$

$$-\frac{34}{7} \le \frac{7x}{7} \le \frac{-24}{7}$$

Q.4 Solve each of the following and check for extraneous solution if any

(i)
$$\sqrt{21+4} = \sqrt{1-1}$$

(ii)
$$\sqrt{3x-1}-2\sqrt{8-2x}=0$$

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Pilot Superone Mathematics 335 Glass 9th

4(i)
$$\sqrt{2t+4} = \sqrt{t-1}$$

Solution:

 $2t+4=1$ (Squaring)

 $2t+4=-1$ (Squaring)

 $2t+4=-1$ (Squaring)

 $2t+4=-1$ (Squaring)

 $2t+4=-1$ (Squaring)

 $2t+4=-1$ (Squaring)

 $3t+4=-5$

Check Put $t=5$
 $3t+4=-5$

Check Put $t=5$
 $3t+4=-5$

Solution in integers in mill set (4)

4(ii) $\sqrt{3x-1}$ $2\sqrt{8-2x} = 0$

Solution.

 $3x-1$ $2\sqrt{8-2x} = 0$

Squaring

 $3x+1 - 4(8-2x)$
 $3x+8x-32+1$
 $11x-33$
 $x=33$
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Pilot Superone Mathematics	336 Class 9 th
$2\sqrt{2}-2\sqrt{2} = 6$	0 = R.H.S.
Q.5 Solve for x	
(i) $3x + 14 - 2 = 5$	$ x \qquad (ii) \qquad \frac{1}{3} x-3 = \frac{1}{2} x+1 $
35	
5(i) = 3x + 14 - 2 - 5x	_
Solution: $ 3x + 14 - 2 =$	5x
3x + 14	١
3x + 14 - 5x + 2	-(3x + 4) = 5x + 2
3x 5x 2 14	$-3x \cdot 14 = 5x + 2$
2x - 12	-3x - 5x = 2 + 14
$x = \frac{-12}{2}$	-8x = 16
x <u>-2</u>	$x = \frac{16}{-8}$
x 6	L .
	x = 2
Check: L.H.S.	R.H.S.
[3x + 14] - 2	x – 6
3(6) + 14 2	5(x)
· 118 + 14 -2	= 5 × 6
- [32] 2	= 30
32 2	
30	True
Now check	x = -2
3x + 14 2 - 5x + 2	2
LHS	R.H.S
[3(2) + 14] -2	5x + 2
J-6 + 14 ₁	= 5(-2) + 2
18)	= -10 + 2
• •	=8

Pilot Superone Mathematics 337 Class 9th [8] = -8 False

Sol. Set = {6}

5(ii)
$$\frac{1}{3}|x-3| = \frac{1}{2}|x+2|$$
 $\frac{1}{3}(x-3) = \frac{1}{2}(x+2)$
Divide on 6

 $2(x-3) = 3(x+2)$
 $2x-6 = 3x+6$
 $2x-3x=6+6$
 $-x=12$
 $x=-12$
Set $\{-12,0\}$
Q.6 Solve the following inequality.

(i) $-\frac{1}{3}x+5 \le 1$ (ii) $-3 < \frac{1-2x}{5} < 1$

Salution: $-\frac{1}{3}x+5-5 \le 1-5$
 $-\frac{1}{3}x+5-5 \le 1-5$
 $-\frac{1}{3}x < -4$

Multiplying by 3 (Change of sign)

$$(-3)$$
 $\left(-\frac{1}{3}x\right) \ge (-3)(-4)$
 $x \ge 12$

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Pilot Superone Mathematics	338 Class 9**
6(ii) $-3 < \frac{1}{5} + \frac{25}{5} < 1$	
Solution: -15 < 1 -2x < 5	Multiplying by 5
15 1 × 1 25	- < 5 1 Subtracting I
16 < 2x < 4	
Dividing by 2	change of sign)
$\frac{-16}{-2} > \frac{-2x^2}{-2} > 0$	1 Ž
2 > x > 2	

Unit LINEAR GRAPHS & THEIR APPLICATION



An Ordered Poir of Real Numbers

An ordered pair of real numbers x and y is a pair (x, y) in which elements are written in specific order i.e.,

- (a) (a, y) is an ordered pair in which first element is x and second is y such that (x,y) ≠ (y, x) where.
- (ii) (2-3) and (3-3) are two different ordered pairs.
- (iii) (x2y) (m, n) only if x m and x n

Cartesian Plane

The Cartesian plans establishes one-to-one correspondence between the set of ordered pairs $R+R=\{0, 0\}$ $x,y \in R$; and the points of the Cartesian plane

In plane two mutually perpendicular straight lines are drawn. The lines are called the coordinate axes. The point O, where the two lines meet is called origin. This plane is called the coordinate plane or the Cartesian plane.



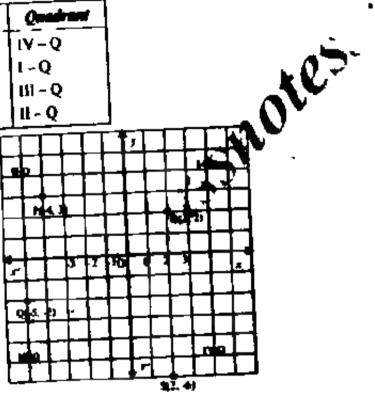
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Class 9° Prior Superone Mathematics 340 **EXERCISE 8.1**

Determine the quadrant of the coordinate plane in 0.1 which the following points lie: P(-4, 3), Q(-5, -2), R(2, 2) and S(2, -6).

Ordered Pair	Quadrant
S(2, -6)	ıV−Q
R(2, 2)	I-Q
Q(-5, -2)	[អ] − Q
P(-4, 3)	II-Q



Q.2 Draw the graph of each of the following.

(vi)
$$x = 0$$

(vii)
$$y = 3x$$
 (viii) $-y = 2x$

$$(\mathbf{x}) = \frac{1}{2} = \mathbf{x}$$

$$3y-5z$$
 (xi) $2x-y=0$ (xii) $2x-y=2$

(xi)
$$x - 3y + 1 = 0$$
 (xii) $3x - 2y + 1 = 0$

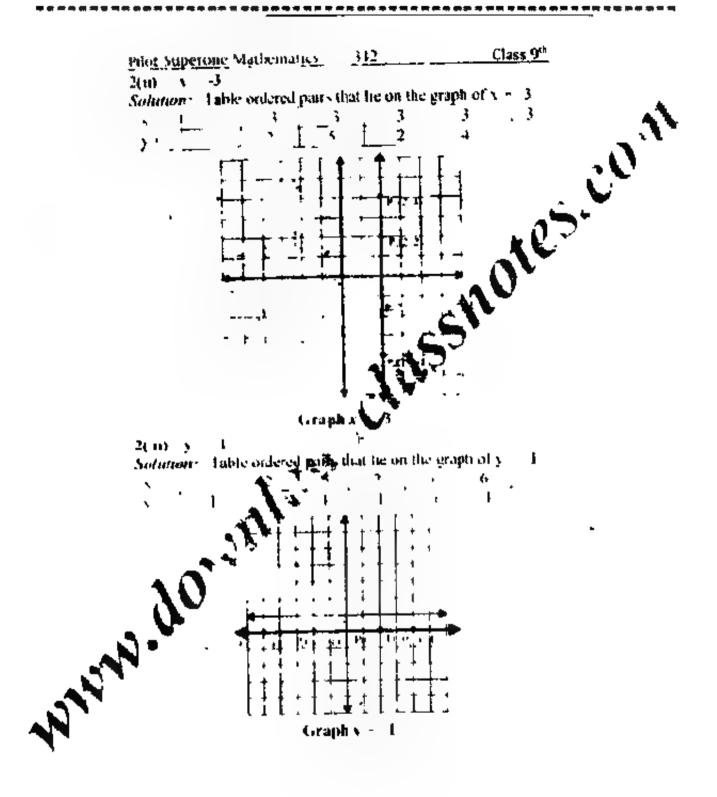


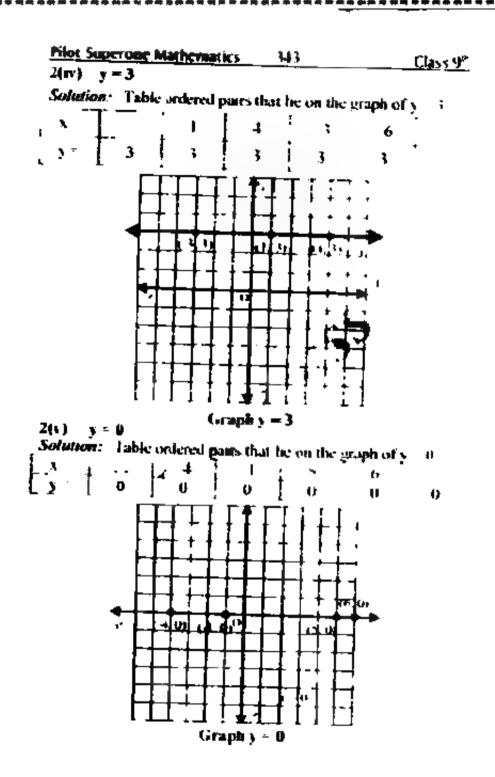
		natios 341	<u> </u>	Class 9 th	
i(i) x = Solution:		ed pairs that is	e on the graph	n of x = 2.	
х=	2	2	2	2	
y =	2	4	2	-4	
ГГ	$\overline{}$		• •		ţ
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\vdash		+	P ₂ (2, 4)		
		-	1,514,41		
	 	\bot			
			P ₁ 2, 2		
\[\frac{\pi^2}{2}\]				x	
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	 		T	, 	

Graph x = 2

Selet	es: Table	ardend	pairs that	he on the	graph of a	x = 3.
¥ *		3	3	-3	3	3
_ورّان		2	5	-2	4	

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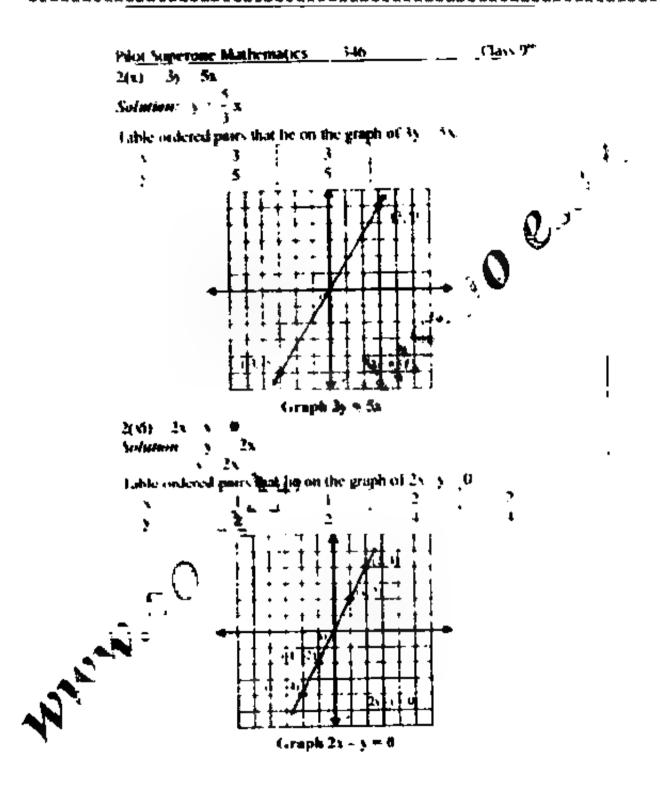


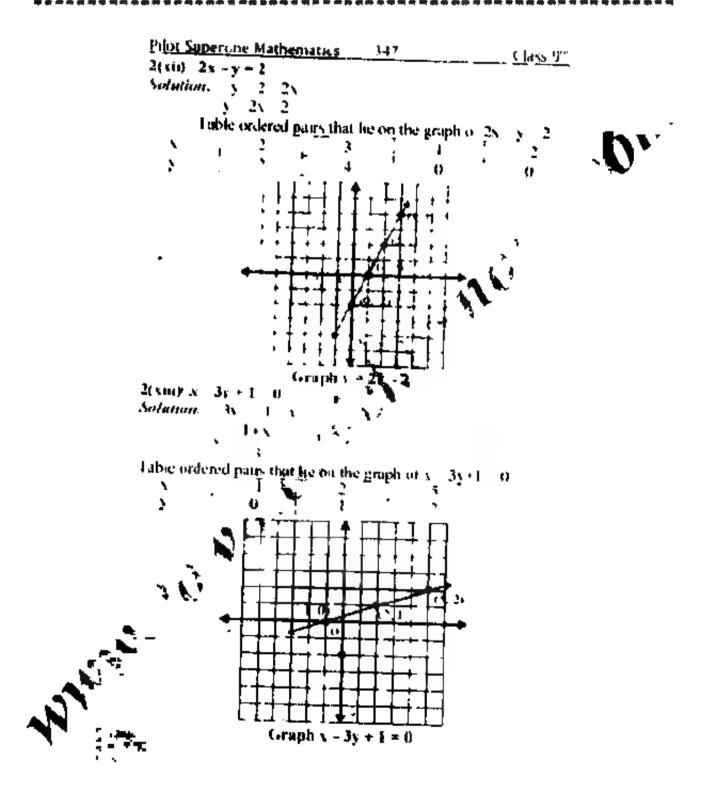


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	2(v) :	6	1110 15 2	MAIN.		
	A(VI) : Salutini	t ~ v ⊶ Table ord¢	red pairs tha	the on the g	$\frac{\text{raph of } x = 0}{1 + 0}$	- A.
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<u>†</u>	 -		3 5	2	-6	.
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		_	- 4	. k		
	Graph	x = 0	This is y-=	À		
	27-35	w = 3×				
	Solutio	w. Table ord	lered pairs th	at he on the	graph of $y = 3x$	
	x =		- 2	1 1 3		
	<u></u>		he points on	tke oranh na		
		Pionaig C	re points on		7	
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, G ,			√y =34			
ware.			Graph o	f y = 3x		

Pilot Superone Mathematics 345 Class 9* 2(vidi) - y = 2xSolution: Table ordered pairs that he on the graph of y = 2xGraph -y = 2x $2(ix) = \frac{1}{2} - x$ Solution: Table ordered pairs that lie on the graph of x =Graph $x = \frac{1}{2}$

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Class 9th Pilot Superone Mathematics 348

2(xiv) 3x - 2y + 1 = 0

Solution: -2y = -1 - 3x

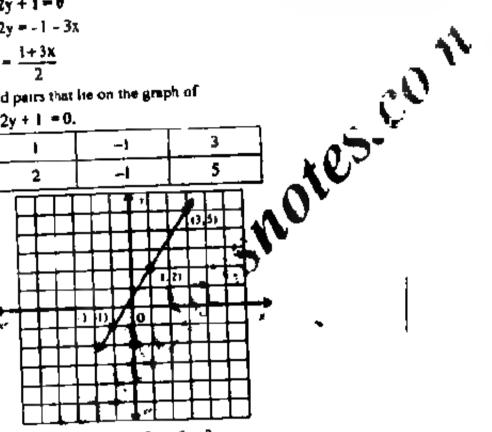
OT

$$y = \frac{1+3x}{2}$$

Table ordered pairs that he on the graph of

3x 2v + 1 = 0.

			 _
x =	ı	(<u>-</u> 1	3
	2	-1	5
		<u> </u>	



Graph 3x - 2y + 1 = 0

Q.3 Are the following lines (i) parallel to x-axis (ii) parallel to y-axis

(1)
$$2x-1=3$$

(ii)
$$x + 2 = 1$$

(iii)
$$2y + 3 = 2$$

$$(v) \qquad 2x - 2y = 0$$

$$3(t) x - 1 = 3$$

Solution.

$$2x - 1 = 3$$

$$2x = 3 + 1$$

MATHEMATICS FOR 9TH CLASS (UNIT # 8) Pilot Superone Mathematics Class 9 Parallel to y-axis x + 2 = -1 3(4) Solution: x + 2 = -1x =-1~2 x = -3 Parallel to y-axis 3(iii) 2y + 3 = 2 Solution. 2y + 3 = 22y = 2 - 3Parallel to x-axis $3f(y) \quad x + y = 0$ Solution: x + y = 0y =



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KIY 0

350 Class 9 Pilot Superone Mathematics h is neither parallel to x-axis, not to y-axis 2x - 2s = 03637 2x - 2y = 0Solution:

It is neither parallel to x-axis, not to y-axis

Find the value of m and c of the following lines by expressing them in the form $\gamma = mx + c$



$$2x + 3y - 1 = 0$$

$$(0) \qquad x-2y=-2$$

(iii)
$$3x + y - 1 = 0$$

(b)
$$2x-y=7$$

(v)
$$3-2x+y=0$$

(vi)
$$2x = y + 3$$



$$2x + 3y - 1 = 0$$

Solution.
$$2x+3y-1=0$$

$$3$$
 - $-2x + 1$

Prior Se	operone Mathematics 351 Clas
or .	$y = -\frac{2}{3}x + \frac{1}{3}$ (i) (Dividing by 3)
	 ms c (n) Comparing Grand
	m <u>2</u>
4(ii) ,	x 2y = 2
Solution	7 x 25 2
	2y + x 2
	$\frac{2}{-2}y = \frac{-x}{2} - \frac{2}{2}$ (Dividing by (2))
	_
	$y = \frac{1}{2}x = 1$ (Comparing it with)
	y = mx + c
	$m = \frac{1}{2}$, $e = 1$
	x+y 1=0
	2. 3x+y F _k ≠6
or	y = 3x + 1 (i)
	3 $\text{fix} * c$ (ii) Comparing (ii) and (iii) 3, $c = 1$
4(h) 21	
Salution:	-
WT .	y = -2x + 7
OF	$y = 2x - 7 \qquad (i)$
) * mx + c (it) Comparing (i) and (i
万 .	m=2, c=-7

Pilot Superone Mathematics 352 4(v) 3 - 2x + y = 0 Solution: 3 2x + y = 0y = 2x - 3 (i) σť y = mx + e (ii) Comparing (i) and (ii) m = 2, c = -3 $4(v!) \quad 2x = y + 3$ 2x = y + 3Solution. y+3 = 2xŒ y = 2x - 3(i) OF. y = mx + c (ii) Comparing (i) and (ii) m = 2, c = -3 Verify whether the following points ile on the line Q.5 1x - y + 1 = 0 or not. (ii) (0,0) (iii) (-1,1) (i) (2, 3) (v) (5, 3) (iv) (2.5) (2,3)5(1) 2x-y+1 = 0Solution: -y •--2x+1 (i)(2,3) $\frac{1}{2} = 2x + 1$ Putting x = 2 ey $\Rightarrow 3$ in the equation 3 = 2(2) + 13 = 4 + 1(impossible) 3 = 5 The point (2, 3) does not lie on the line.

5(4) (0,0)

Solution:

$$y = 2x + 1$$

Putting x = 0, y = 0 in the equation

$$0 = 2(0) + 1$$

$$0 = 0 + 1$$
 (Impossible)



Pilot Superone Mathematics 353 Class 9th The point (0, 0) does not lie on the line. 5(IU) (-1, 1) Solution: 2x - y + 1 = 0y = 2x + 1Putting x = -1, y = 1 in the equation 1 = 2(-i) + 1I = -2 + 11 = -1(impossible) The point (-1, 1) does not lie on the line. 5(h) (2,5) Solution: 2x - y + | = 0y = 2x + 1Putting x = 2, y = 5 in the equation 5 = 2(2) + 15 = 4 + F5 = 5 (True) The point (2, 5) he on the late. 5(0) (5, 3)2x - x + 1 = 0 y = 2x + 1Solution: Putting z=5, y=3 in the equation 3 = 2(5) + 13 = 10 + 13 = 11 (Impossible)

Class 9th Pilot Superone Mathematics 354

EXERCISE 8.2

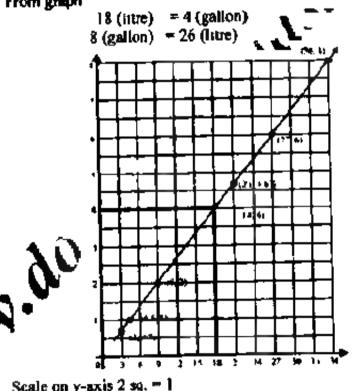
- Draw the conversion graph between litres and gallons 0.1 using the relation 9 litres = 2 gallons (approximately), and taking litres along horizontal axis and gallans along vertical axis. Form the graph, read
 - The number of gallons in 18 fitres.
 - The number of litres in 8 gallons. (ii)

Solution:

(Litre)
$$9 = 2$$
 (gallon)

	Value table fe	or (x, <u>y)</u>		14
x =	3	45	21	27
y =	67	i	4 67	6

From graph



Scale on y-axis 2 sq. = 1

Pilot Superone Mathematics 355 Class 9th
Scale on x-axis 1 sq = 3

Q.2 On 15.03 2008 the exchange rate of Pakistani currency and Saudi Riyal was as under:

I.S. Riyal = 16,70 Rupees

If Pakiston: currency y is an expression of S. Riyal x, expressed under the rule y = 16.70x, then draw the conversion graph between these two currencies by taking S. Riyal along x-axis.

Solution:-

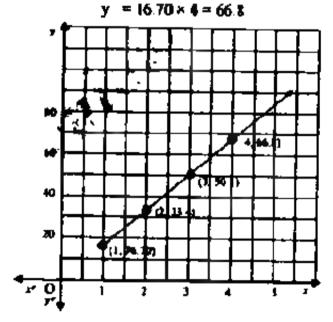
y = 16.70x where y is Pak. Rupee and x is S. Riyel
Table value for x and v

x- i	2	3	4
y= 16.70	33 40	50.10	66.8

From graph

$$y = 16.70 \times 2 = 33.40$$

 $y = 16.70 \times 3 = 50.10$



Pilot Superone Mathematics 356 Class 9th Graph. y 16.70

Q.3 . Sketch the graph of each of the following lines.

- (e)
- x-3y+2=0 (b) 3x-2y-1=0
- (c) 2y x + 2 = 0
- (d) y 2x = 0
- (e) 3y-1=0
- (f) y+31=0
- (g) 2x + 6 = 0

$$3(a) = x - 3y + 2 = 0$$

Solution:

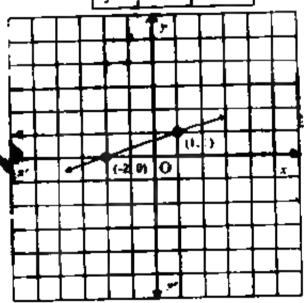
$$-3y = -x - 2$$

$$y = \frac{-x-2}{-3}$$

$$y = \frac{x+2}{3}$$

Table value for x and y

x =	l	* 2
y =	1	0



Graph: x - 3y + 2 = 0

Written/Composed by - SHAHZAD IFTIKHAR Contact # 0313-5665666 Website www.downloadclassnotes.com , E mail ragshahzadiftikhar@gmail.com

MATHEMATICS FOR 9TH CLASS (UNIT # 8)

Pilot Superone Mathematics 357

3(b) 3x-2y-1=0

Solution.

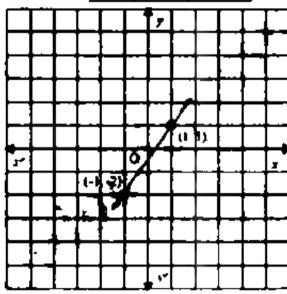
$$-2y = -3x + 1$$

$$y = \frac{-3x + 1}{-2}$$

$$y = \frac{3x - 1}{2}$$

Table of ordered pairs for (x, y)

x =	1	-l
y =	1	7



Graph: 3x - 2y - 1 = 0

$$3(c)$$
 $2y-x+2=0$

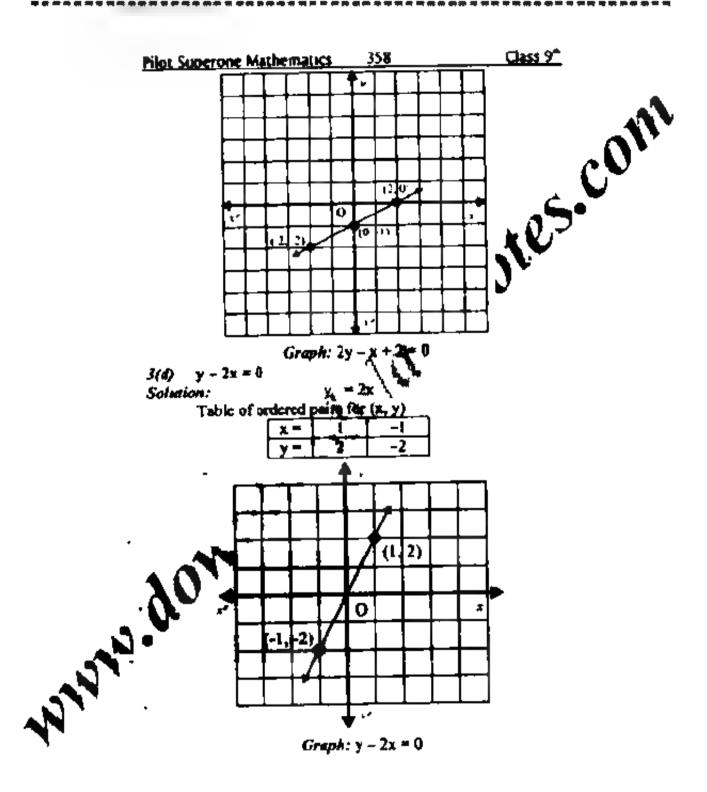
$$2y = x - 2$$

$$y = \frac{x-2}{2}$$

Table of ordered pairs for (x, y)

x-	2	-2	0
y=	0	-2	-1





NATHEMATICS FOR 9TH CLASS (UNIT # 8)

Pilot Superone Mathematics 359 Class 9th					
3(c) y-1=					
Solution.	3y - 1 y = $\frac{1}{3}$				
	of ordered pairs for (x, y)				
X	1 2 3 -2				
, , , ,	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
3(f) y + 3x : Solution Table o	Graph: $3y - 1 = 0$ $y = 3x$ of ordered pairs for (x, y) $x = -1$ $y = 3$				
	(1,2)				
•					
	11 31				

Graph: y + 3x = 0

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MATHEMATICS FOR 9TH CLASS (UNIT # 8)

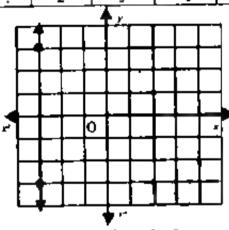
Pilot Suberone Mathematics 360 Class 9^{\pm} 3(g) - 2x + 6 = 0

Solution:

~

$$x = -3$$

Table of ordered pairs for (x, y)					
X =	-3	3	-3	-3	-3
y =		2	3	_3_	



Graph: 2x +6=0

Q.4 Draw the graph for following relations.

- (i) One mile = 1.6 km
- (ii) One Acre- 0.4 Hectare

(iii)
$$F = \frac{9}{5}C + 32$$

(iv) One Rupec =
$$\frac{1}{86}$$
\$

4(i) One mile = 1.6 km

Solution:

one mile = 1.6 km

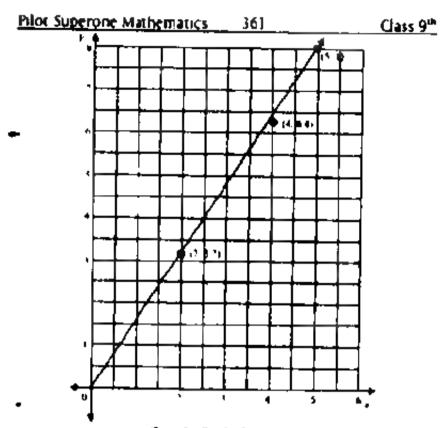
Let us show it by an equation

$$y = 16x$$

We prepare a table in form of ordered pairs in x, y

ſ	x =	0	2	5	* _ ^
T	y =	0	3 2	80	6.4





Graph: Scale 2 sq. = 1

6(ii) One Acre- 0.4 Hectare

Solution:

One Acre = 0.4 Hextor

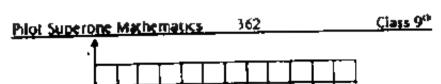
Let us show it by an equation

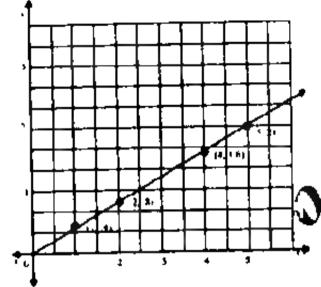
$$y = 0.4x$$

Table of ordered pairs in (x, y)

The state of the s						
X €	0	1	2	4	5.	
y-	0	0.4	.8	1.6	2.0	

Putting the ordered pair on the graph and joining them, we get a straight line





Graph: Scale $3 \text{ sq.} = 1_a \text{ Scale} + 2 \text{ sq.} = 1$

4(iii)
$$F = \frac{9}{5}C + 32$$

Solution:

Table value for F and C in form of (x, y)						
[x	(0	10	20	50	100
- ~	- ï-	32	50	68	122	212

$$F = \frac{9}{5}C + 32$$

$$F = \frac{9}{5}(0) + 32 - 32$$

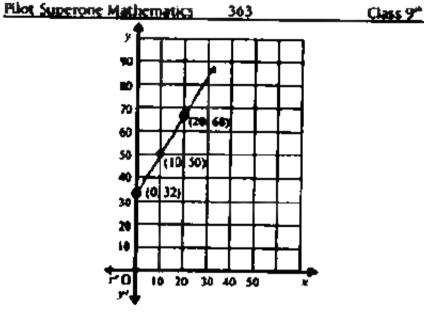
$$F = \frac{9}{5}(10) + 32 - 50$$

$$F = \frac{9}{5}(20) + 32 - 68$$

$$F = \frac{9}{5}(100) + 32 - 212$$

$$F = \frac{9}{5}(100) + 32 = 212$$

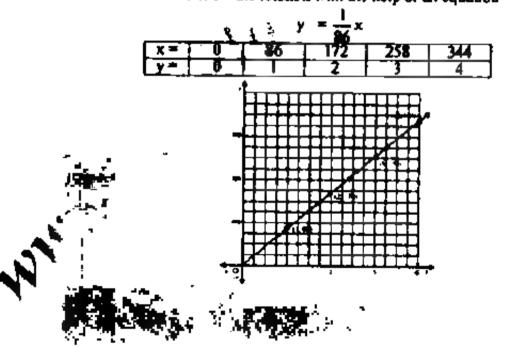




4(lv) One Rupee =
$$\frac{1}{86}$$
\$

Solution: One rapes $= \frac{1}{26}$

We show the relation with the help of an equation



Pilot Superone Mathematics 364

EXERCISE 8.3

otes, com Solve the following pair of equations in x and y graphically.

- 1+y = 0, 2x y + 3 = 0
- x-y+1=0, x-2y=-1
- 2x + y = 0, x + 2y = 2
- x+y-1-0,x-y+1=0
- 2x + y 1 = 0, y = -y

x+y=0.2x-y+3=0

Solution:

-y **≠-2**x-3 y = 2x + 3

Table for x and y values

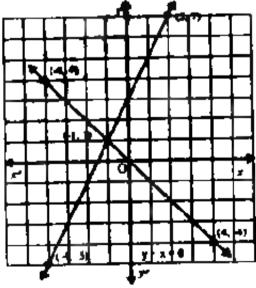
	1	
X =	4	4
y=	1	4

Table for a and y value

X =	2	4
у.=	7	-5

Ł

Plotting points on the graph paper



Point of intersection (-1, 1)

Set. Set = $\{(-1, 1)\}$

Pilot Superone Mathematics 365

Class 9th

2. x-y+1=0, x-2y=-1

Th/amag/

$$x-y+1=0$$

$$-y=-x-1$$

$$y=x+1$$

-2y = -1 - x $y = \frac{-1 - x}{2}$

Table for x and y values

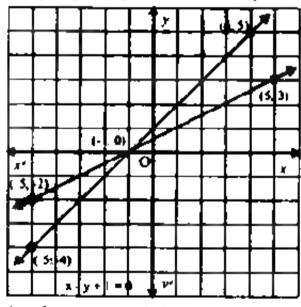
χ=	4	5
y=	5	-4

 $y = \frac{1+x}{2}$

Table for x and y value

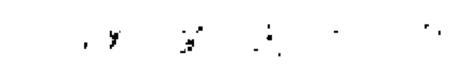
	~	
χ =	5	-5
y =	3	-2

Plotting the pair of points of both the equations.



Point of intersection (-1, 0)

Sol. Set = $\{(-1, 0)\}$



Pilot Superone Mathematics 366 Class 9^{40} 3. 2x + y = 0, x + 2y = 2

Solution:

$$2x + y = 0$$
$$y = -2x$$

Table value for x, y

X =	2	3
y =	1	6

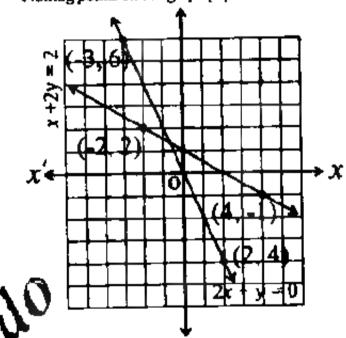
(+	2y	= ;	2
	2у	= 2	2 – x
		_	2-x
	,	_	

Table value for x, y

	<u> </u>				
X =	4	-2			
у 🛨	-l	3			
		_			

-co.

Plotting points on the graph paper



Point of intersection $\left(-\frac{2}{3}, \frac{4}{3}\right)$

Sol. Set =
$$\left\{ \left(-\frac{2}{3}, \frac{4}{3} \right) \right\}$$

Pilot Superone Mathematics 367 x+y-1=0,x-y+1=0

Solution:

Table value of x, v

		<u> </u>
x =	7	6
y -	5	_5

Table value of x, y							
X **	4	- 5					
y =	5	-4					

Plotting points on the graph paper

		14	5)		Ľ	F		Γ		F	Г
	L`			\Box					\mathbb{Z}	Н,	7
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Point of intersection (0, 1)

Sol. Set =
$$\{(0, 1)\}$$

$$2x + y - 1 = 0, x = -y$$

Solution:

x	≖ -y
V	⇒ –x

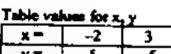
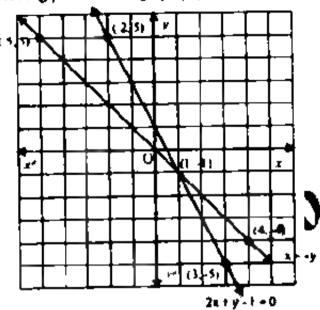


Table value for x, y						
χ-	4	-5				
y =	4	5				

Pilot Superone Mathematics 368 Class 9th

Plotting points on the graph paper



Point of intersection $(1, -\frac{1}{2})^{4}$ Sol. Set = $\{(1, -1)\}$

Review Exercise 8

Q.1 Choose the correct answers.

- (i) If (x 1, y + 1) = (0, 0), then (x, y) is
 - (a) (1,-1)
- (b) (-1, 1)
- (c) (f. 1)
- (d) (-1,-1)
- (ii) ||f(x,0)|| = (0, y), then (x, y) is



- **(0, 1)**
- (b) (1,0)
- (c) (0,0)
- (d) (1, 1)

r: 41

Point (2, -3) lies in quadrant

- (a) 1
- (b) II
- (c) [1]
- (d) IV

(iv)

- Point (-3, -3) lies in quadrant
 - (a) 1
- (b) II

Written/Composed by - SHAHZAD IFTIKHAR Contact # 0313-5665666 Website www.downloadclassnotes.com , E mail ragshahzadiftikhar@gmail.com

MATHEMATICS FOR 9TH CLASS (UNIT # 8)

Pilot Superone Mathematics Class 9th (c) 111 (d)

- If $y = 2x + 1 \times 2$ then y is (v)
 - (a) Ż **(b)**
 - (c) **(d)** 5
- $\{v_1\}$ Which ordered pair satisfy the equation y = 2x
 - (1, 2)
- (b) (2, 1)

3

- (2, 2)(C)
- (d) (0, 1)

Answers:

0	Я	(II)	С	(iii)	đ	(iv) = 6
(4)	d	(vi)	A			
					_	

Identify the following statements as True or False. 0.2

- (i) The point O(0, 0) is a vertical line.
- (i) The point P(2, 0) lies on x-axis.
- (iii) The graph of x = 2 is a vertical line.
- (iv) 3 y 0 is a horizontal line
- (v) The point Q(1,2) is in quadrant III
- (vi) The point R(1, -2) is in quadrant IV
- (vii) y = x is a line on which origin lies.
- (viii) The point P(1, 1) lies on the line x + y = 0.
- (iz) The point S(1, 3) ies in quadrant III
- (x) The point R(0, 1) lies on the x-axis

A	*
t	113
(0)	1LF

	(4)	F	(ii)	T	(lii)	Т	(tv)	T
q	(1)	F	(vi)	F	(vii)	Ť	(vill)	ŀ
7	(ix)	[F]	(x)	F				

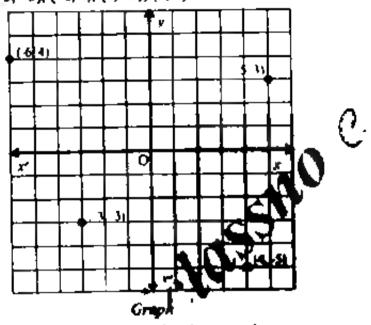




Pilot Superone Mathematics 370

Draw the following points on the graph paper.

(-3, -3), (-6, 4), (4, -5), (5, 3)



Q.4 Draw the graph of the following equations.

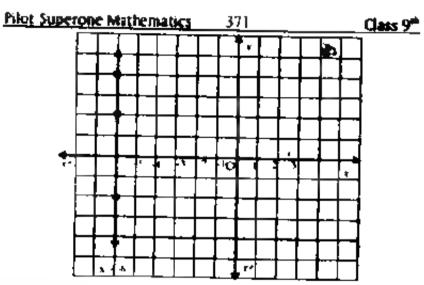
(iii)
$$x = \frac{3}{2}$$

(iv)
$$y = \frac{5}{2}$$
 (v) $y = 4x$ (vi) $y = -2x + 1$

(vi)
$$y = -2x + 1$$

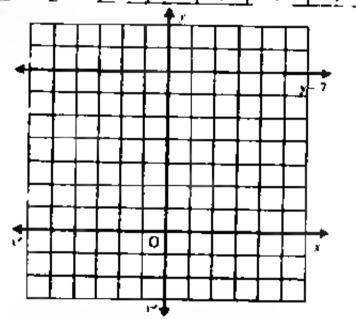
Salution: Table value for x, y

	Contraction									
ſ	χ =	6	-6	-6	-6	6	-6			
ľ	y ±		2	4	5	1	2			



Graph of x = -6 to parallel to y-axis and at the left side of it.

4(ii) Soluti	y = 7		value for	rx, y			
_ <u>x</u> =		2	3	4	-1	-3	
y = j	7	7	_ 7	7	7	7	1



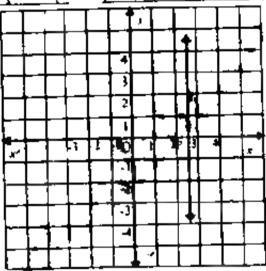
Pilot Superone Mathematics 372 Class 9"

Graph of y = 7 is parallel to x-axis and it is box it at a distance of 7 units

Solution: x = 2.5

Table value for x. Y

		LADIC	YARK	: IU	٠.,	<u>, , , , , , , , , , , , , , , , , , , </u>							
	x =	2.5	2.5		2.5	<u> </u>	2	5	2	5	1	2 :	
1	y -		3		4		2		-1_		┸		
١		٦	T										
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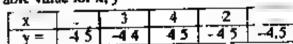


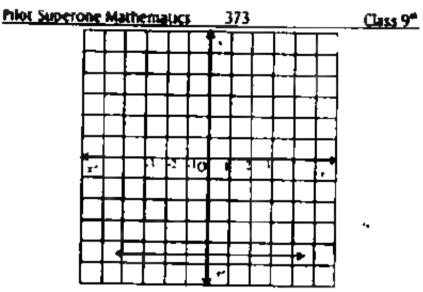
Graph of $R = \frac{5}{2}$ is parallel to y-axis and is on the right of it at a distance of $\frac{5}{2}$ units.

4(iv)
$$y = -\frac{9}{2}$$

Solution: $y = -4.5$

Table value for x, y

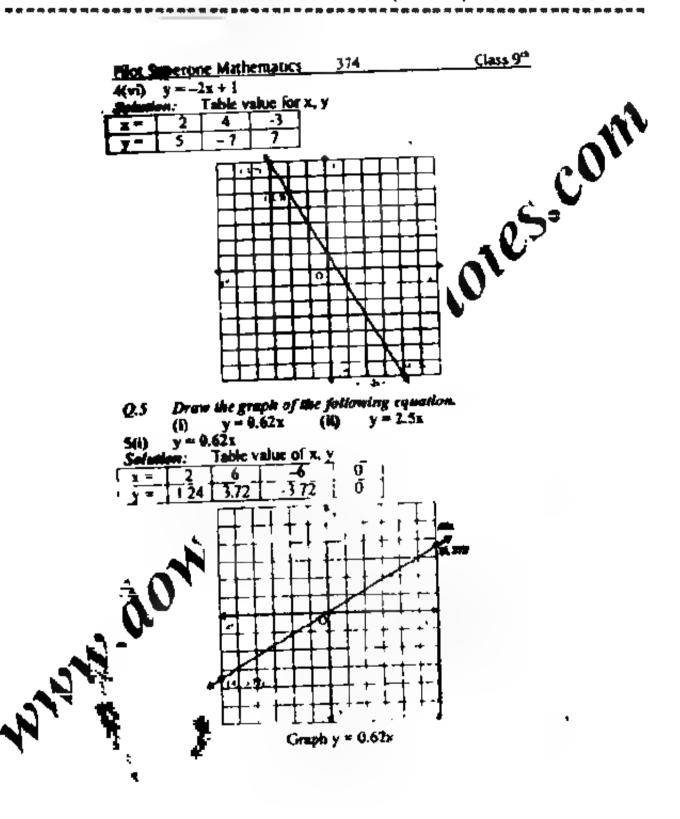




Graph of $y = -\frac{9}{2}$ is parallel to x-axis and it is below at a distance of $-\frac{9}{2}$ units. $\frac{1}{4}$

4(v) y = 4xSolution: Table value

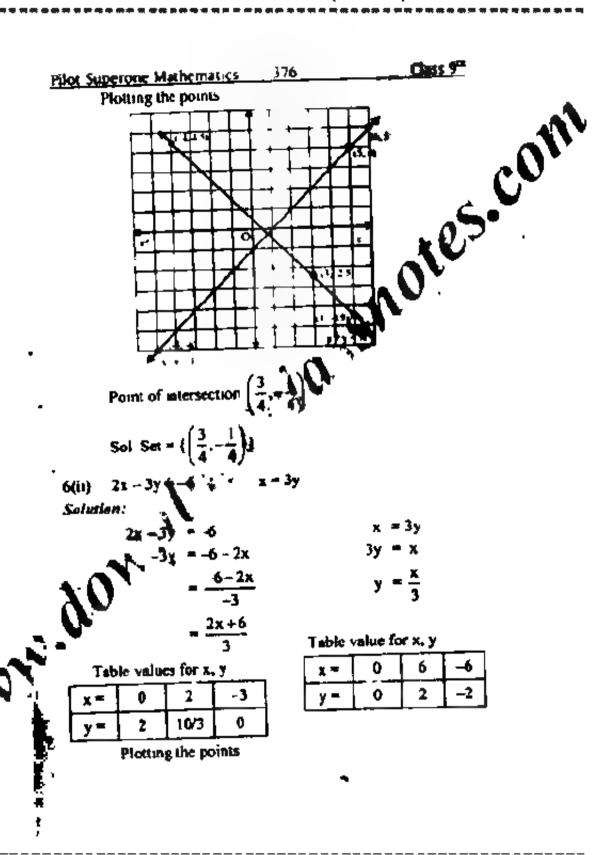
Solution:	Table value for x, y								
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		\Box	-)		4	_	4
	[;]	Ţ	1	T	١.		ΤĒ	$\overline{}$	亓
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•				y =	٠X				

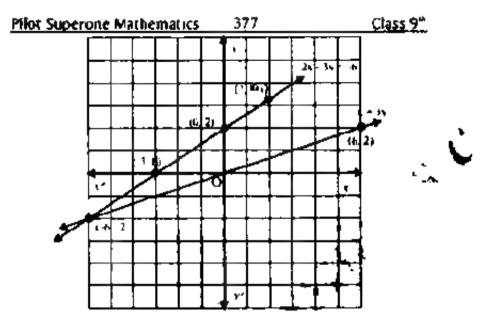


Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>ranshahzadiftikhar@qmail.com</u>

NATHEMATICS FOR 9TH CLASS (UNIT # 8)

Filot Superone Mathematics 375 Class 9 th $S(ii) y = 2.5x$ Solution: Table value for $x = 0 2 -2$ $y = 0 5 -5$
Graph y = 2.5x Q.6 Solve the following equations
(i) $x-y+1$, $x+y=\frac{1}{2}$ (ii) $x=3y$, $2x-3y=-6$ (iii) $\frac{1}{3}(x+y)=+\frac{1}{3}(x-y)=-1$ 6(i) $x+y=\frac{1}{2}$, $x+y=1$
Solution: $y = \frac{1}{2}$ $y = \frac{1}{2} - x$ Table value for x, y
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1





Point of intersection (-6, -2) - 3 -4

Common Sol. Set = $\{(-6, 2)\}$

6(iii)
$$\frac{1}{2}(x-y)=-1$$
, $\frac{1}{3}(x+y)=2$

Solution:

$$\frac{1}{2}(x-y) = -1$$

$$x = y = -2$$

$$y = -2 - x$$

$$y = x + 2$$

$$\frac{1}{3}(x+y) = 2$$

$$x+y=6$$

$$y=6-x$$

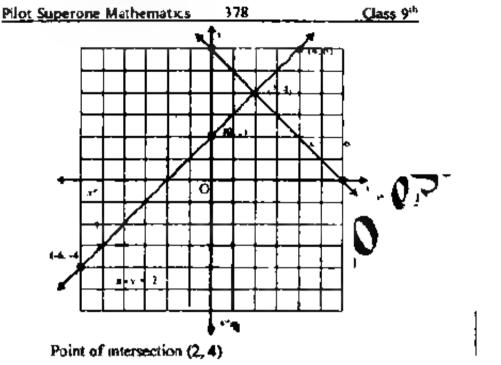
Table values for x, y

		-,,,			
€ #=	4	6	0		
γ=	6	4	2		

Table value for x, y

x =	4	2	0
y =	2	8	6





Common Sol. Set = {(2, 4)}

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Pilot Superone Mathematics 379

Class 9th



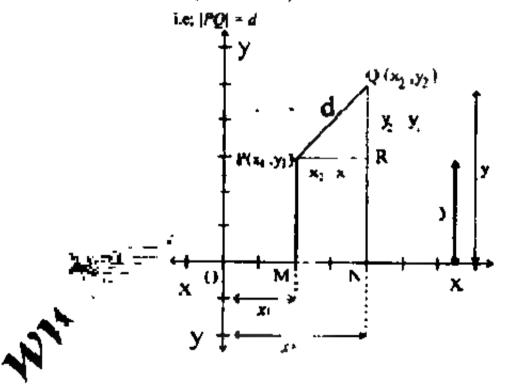
INTRODUCTION TO CO-ORDINATE GEOMETRY

- (i) The distance formula.
- (ii) Collinear Points.
- (iii) Mid Point Formula.

Distance Formula

(Finding distance between two points).

Let $P(x_i, y_i)$ and $Q(x_i, y_i)$ be any two points in the coordinate plane where distance between P and Q is 'd' (a real number).



Pilot Superone Mathematics 380 Class

 $P\overline{M} \perp X'OX$, $\overline{QN} \perp X'OX$ and $\overline{PR} \perp \overline{QN}$ therefore,

 \overline{PM} , \overline{QN} are parallel to Y'OY and PR is parallel to X'OX.

Thus \triangle PRQ is a right angled triangle and in \angle PRQ = 90°

Now $m \overline{PR} = |x_2 - x_1|$ and $m \overline{RQ} = |y_2 - y_1|$

Using Pythagoras Theorem

(m PQ Jone 4m PR)2

 $(m \overline{RQ})^{*}$

or

or

$$-\sqrt{|x_2-x_1|^2+|y_2-y_1|^2}$$

Corollary

Distance of any point (x_1, y_1) from the origin $(0, 0) = \sqrt{x_2^2 + y_1^2}$

D.G.

Prior Supergne Mathematics 311 Class 9" EXERCISE 9.1 Find the distance between the following pairs of L points. **(a)** A(9, 2), B(7, 2) (b) A(2, -6), B(3, -6)(c) A(-8, 1), B(6, 1) (d) $A(-4\sqrt{2}), B(-4, -1)$ 31 (e) A(3, 11), B(3, 4) (f) A(0, 0) B(0, -5) Solution:-I(a) A(9, 2), B(7, 2) 1(b) A(2, -6), B(3, -6) $|AB| = \sqrt{(3-2)^2 + ((-6) - (-6))^2}$ $= \sqrt{(1)^2 + (-6+6)^2}$ $\sqrt{|x_2 - x_1|^2 + |y_2 - y_1|^2}$ (Formula) $|AB| = \sqrt{(6-(-8))^2+(1-1)^2}$ $-\sqrt{(6+8)^2+0}$ - V(14) = 14 $I(d) = A(-4,\sqrt{2}), B(-4,-3)$ $\sqrt{|\mathbf{x}_2 - \mathbf{x}_l|^2 + |\mathbf{y}_2 - \mathbf{y}_l|^2}$



 $=\sqrt{0+(-1)^2(1+\sqrt{2})^2}$

 $d = \sqrt{|x_1 - x_1|^2 + |y_2 - y_1|^2}$ (Formula) $|AB| = \sqrt{|(3 - 3)|^2 + [(-4) - (-1)]^2}$ $-\sqrt{(3-3)/2} - \sqrt{0+(-4+1)^2}$

(Formula) $|AB| = \sqrt{(0-0)^2 + (-5) - 0}^3$ $\sqrt{3+(-5)^2}$ $4\sqrt{(-5)^2}=5$

Let P be the point on x-axis with x-coordinate 'a' 2 and Q be the point on y-axis with y-coordinate 'b' as given below. Find the distance between P and O.



$$a = -8$$
, $b = 0$

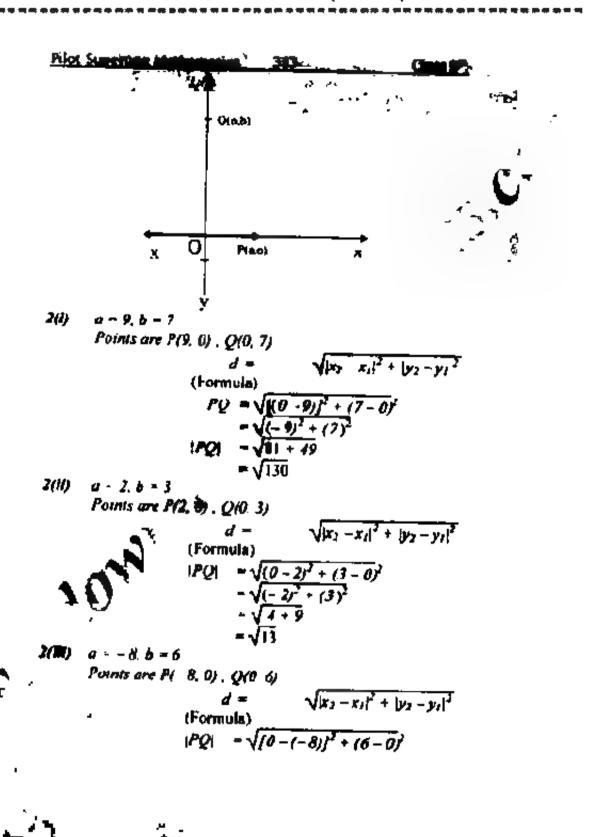
$$a = -8, b = 6$$
 (iv) $a = -2, b$

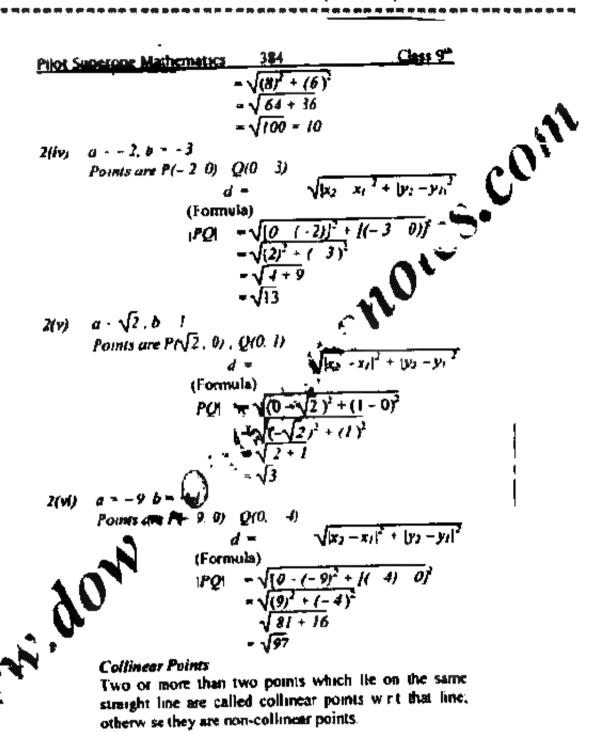
$$a = \sqrt{2} \cdot b = i$$

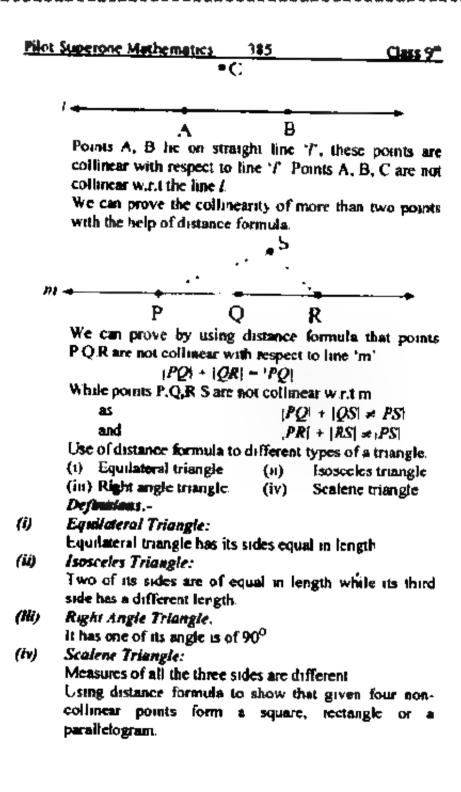
$$a = \sqrt{2}, b = I$$
 (vi) $a = 9, b$



The points which are on x-axis have y-coordinate 'o' and the points which are on y-axis have x coordinate







Written/Composed by - SHAHZAD IFTIKHAR Contact # 0313-5665666 Website www.downloadclassnotes.com, E mail ranshahzadiftikhar@gmall.com

NATHEMATICS FOR 9TH CLASS (UNIT # 9)

Class 9" Pilot Superone Mathematics 386

Square:

It is a closed plane figure formed by four non-collinear Parallelogram
It is a closed plane figure formed by four non-collingar

(i) lengths of opposite sides are equal

(ii) its opposite sides are parallel

iii) measure of none of the points such that length of all sides are equal and

(ii)

sides are equal (cach vertex is of 90°)

Jogram

a closed piane figure formed by

(i) lengths of opposite sides are equal

(ii) its opposite sides are parallel

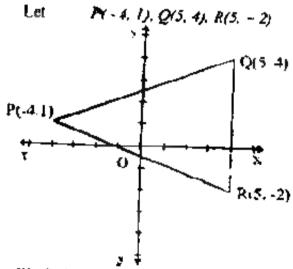
(iii) measure of none of the angle is \$00°.

Pilo, Superone Mathematics 387 Class 9th

EXERCISE 9.2

Q.1. Show whether the points with vertices (5, -2), (5, 4) and (-4, 1) are vertices of an equilateral or an isosceles triangle?

Solution:-



We find |RP|, |QR| and |PQ| $d = \sqrt{(x_2 - x_i)^2 + (y_i)^2}$ (Formula)

$$|PQ| = \sqrt{[3 - (-4)]^2 + [4 - 1]^2} = \sqrt{(5 + 4)^2 + (3)^2} = \sqrt{81 + 9} =$$

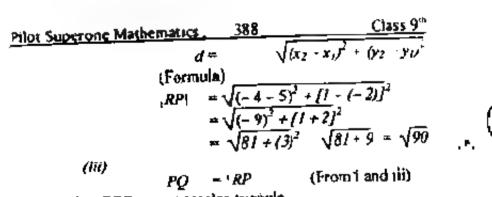
√90 (t) Q(3, 4), R(5, -2)

$$d = \sqrt{(x_2 - x_3)^2 + (y_2 - y_4)^2}$$
(Formula)
$$QR = \sqrt{(5 - 5)^2 + (-2 - 4)^2}$$

$$= \sqrt{0 + (-6)^2} = \sqrt{36^2} = 6$$

(fi) R(5, -2), P(-4, 1)

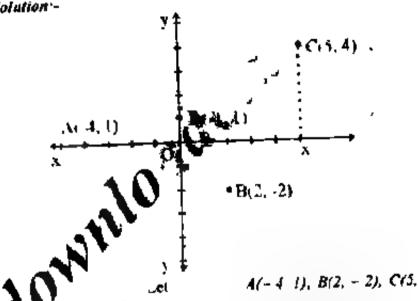




Thus PQR is an isosceles triangle Show whether or not the points with vertices (-1,

1), (5, 4), (2, -2) and (-4, 1) form a square.

Solution'-



le find $AB \cdot |BC \cdot |CD| \cdot |DA|$ $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ $|AB| = \sqrt{\frac{[2 \cdot (-4)]^2 + [(-2) \cdot (-1)^2}{2}}$ $= \sqrt{(6)^2 + (-3)^2} = \sqrt{36 + 9} =$ We find

(i)

$$|BC| = \sqrt{(5-2)^2 + (4-(-2))^2}$$

 $\sqrt{45}$

Pilot Superone Mathematics 389 Class 9th =
$$\sqrt{(3)^2 + (6)^2} = \sqrt{9 + 36} = \sqrt{45}$$

(ii)

 $|CD| = \sqrt{[(-1) - (5)]^2 + (1 - 4)^2}$
 $= \sqrt{(-1 - 5)^2 + (-3)^2} = \sqrt{36 + 9} = \sqrt{(-6)^2 + (-3)^2} = \sqrt{36 + 9} = \sqrt{(-6)^2 + (-3)^2} = \sqrt{36 + 9} = \sqrt{(-4) + (-1)} = \sqrt{(-4) + (-1)} = \sqrt{(-3)^2} = \sqrt{9} = 3$

(iv)

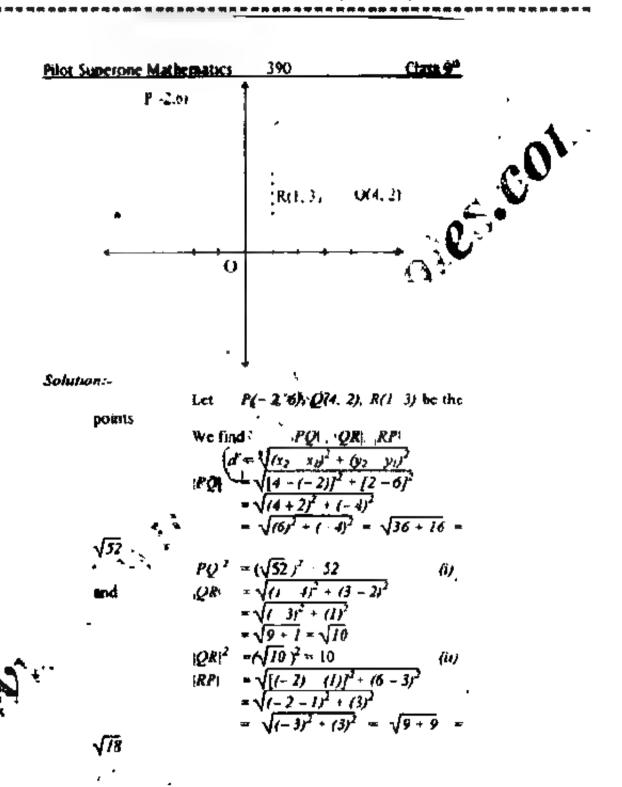
We find that

 $|AB| = |BC| = |CD| \neq |DA|$

Therefore $(-4, 1) (2, -2), (5, 4), (-1, 1)$ do not Form a square figure.

Q.3. Show whether or not the points with coordinates (1, 3), (4, 2) and (-2, 6) are vertices of a right triangle.





Pilot Superone Math	rematics	39	21	Class 9 ⁿ
and	$RP^{.2}$	- NI	$(8)^2 = 18$	(111)
	PQ_1^2		From (m), (n), (
	$ QR ^2$	- 10	, . ,	
	$ \bar{RP} ^2$	= 18		
We see that				
	52 + 10	0 × 18		
	10 + 18	8 <i>= 52</i>		
	18 + 52	2 = 10		

Therefore, points (1, 3) (4, 2), (-2, 6) do not form a right angle triangle

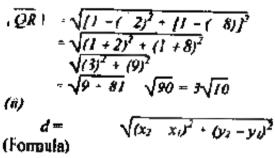
Q.4. Use the distance formula to prove whether or not the points (1, 1), (2,-8), (4,10) lie on a straight line?

Solution;-

We find

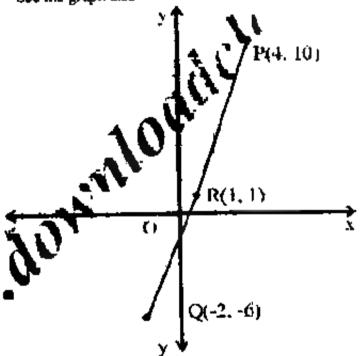
Let P(4, 10), Q(-2, -8), R(1, 1) be the points

RP(.) \overline{QR} and PQ $d' = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ (Formula) $PQ() = \sqrt{(-2 - 4)^2 + (-8 - 10)^2}$ $= \sqrt{(-6)^2 + (-18)^2}$ $= \sqrt{36 + 324} = \sqrt{360} = 6\sqrt{10}$ (i) $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ (Formula)





Pilot Superone Mathematics 392 Class 9^{th} $RP| = \sqrt{(4-I)^2 + (10-I)^2}$ $= \sqrt{3J^2 + (9)^2}$ $- \sqrt{9 + 8I} = \sqrt{90} = 3\sqrt{10}$ (ill) $|QR| = 3\sqrt{10}$ $|RP| = 3\sqrt{10}$ $|QR| + |RP| = 3\sqrt{10} + 3\sqrt{10}$ $= \sqrt{10}(3+3)$ $= 6\sqrt{10}$ $|PQ| = 6\sqrt{10}$ From (i) |QR| + |RP| = |PQ|Points are collinear.
See the graph also



Q.5. Find k, given that the points (2, k) is equidistant from (3, 7) and (9, 1)

Solution:-

13(1, 7) • C(9, 1)

Let A(2, k), B(3,7), C(9, 1) AB|, |AC| $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_2)^2}$ (Formula) $|AB| = \sqrt{(3 - 2)^2 + (7 - k)^2}$ $= \sqrt{(1)^2 + (7 - k)^2}$ $= \sqrt{1 + (7 - k)^2}$ $= \sqrt{(7)^2 + (1 - k)^2}$ $= \sqrt{49 + (1 - k)^2}$ (ii)

According to the given condition

$$|AB| = |AC|$$

$$\sqrt{1 + (7 - k)^2} = \sqrt{49 + (1 - k)^2} \quad \text{(from 1, si)}$$
Or $1 + (7 - k)^2 = 49 + (1 - k)^2$

$$1 + 49 + k^2 + 14k = 49 + 1 + k^2 + 2k$$

$$12k = 0$$

$$k = 0$$

Q.6. Use distance formula to verify that the points $A(\theta, T)$, B(3, -5), C(-2, 15) are collinear.

Solution:

$$A(0, 7), B(3, -3)$$
 $C(-2, 15)$ are

given

We find
$$|CA|, |BC|, |AB|$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

(Formula)

$$|AB| = \sqrt{(3-0)^2 + [(-5)-7]^2}$$

$$= \sqrt{(3)^2 + (-5)-7]^2}$$

$$= \sqrt{(3)^2 + (-12)^2}$$

Pilot Superone Mathematics 394 Class 99 $= \sqrt{9 + 144} = \sqrt{153}$ $= \sqrt{2 + 2 + 17} = 2\sqrt{17}$ $=\sqrt{3 \times 3 \times 17} = 3\sqrt{17}$. O $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} , \lambda$ (Formula) $BC_1 = \sqrt{(-2/3)^2 + [15 - (-5)]^2} = \sqrt{(-5)^2 + (15 - 5)^2} = \sqrt{25 + (20)^2}$ $= \sqrt{25 + 400} = \sqrt{425}$ $= \sqrt{5 \times 5 \times 17} = 2\sqrt{17}$ ſĭij $d = \sqrt{(x + \tau_1)^2 + (y_2 - y_1)^2}$ (Formula) $CA_1 = \frac{(4 - 4 - 2)f^2}{(4 - 4 - 2)f^2} \cdot (-15)^2$ $4 + 64 = \sqrt{68}$ $4 + \sqrt{2 \times 2 \times 17} = 2\sqrt{17}$ $4 + |C| = 3\sqrt{17} + 2\sqrt{17} \qquad \text{(from i + 1)}$ Gin, rji) $=\sqrt{17}(3+2)$ $3\sqrt{17}$ $|BC| = 5\sqrt{17}$ (from ii) |AB| + |CA| = |BC|

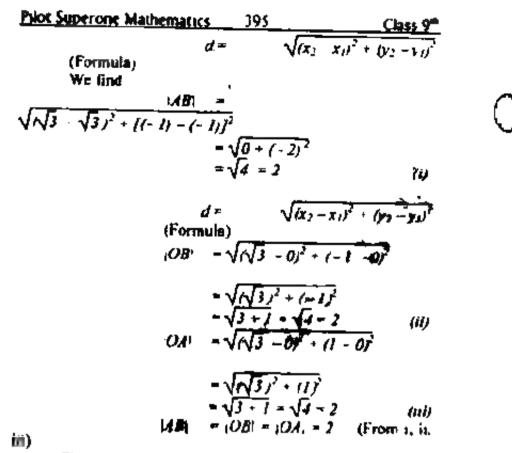
Therefore $A(\theta - 7)$, B(3 - 5) and C(-2, 15) are coffinear

Q.7. Verify whether or not the points O(0, 0), $A(\sqrt{3}, 1)$, $B(\sqrt{3}, -1)$ are the vertices of an equilateral triangle.

Solution:-

We find the lengths of the sides of the triangle O(0, 0), $A(\sqrt{3}, 1)$, $B(\sqrt{3}, -1)$





The lengths of the sides of the triangle are equatherefore, the triangle in equilateral

Q.8. Show that the points A(-6, -5), B(5, -5), C(5, -8) and D(-6, -8) are the vertices of rectangle.

Find the lengths of the diagonals. Are they equal?

Solution:

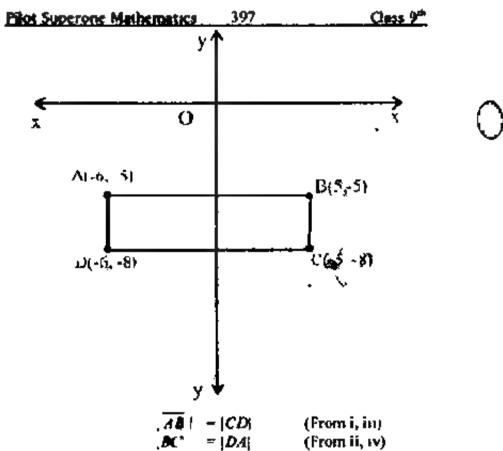
Points are
$$D(-6, -8), C(5, -8), B(5, -5), A(-6, -5)$$

We find $|DA|, |CD|, |BC|, |AB|$
 $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
(Formula)





Pilot Superone Mathematics 396 Class T $d = \sqrt{(x_2 - x_1)^2 + (y_1 - y_2)^2}$ (Formula) $(BC) = \sqrt{(5 - 5)^2 + (6 - 8) - (-5)^2} = \sqrt{(5 - 5)^2 + (6 - 8) - (-5)^2}$ Ø $= \sqrt{0 + (-8 + 5)^2}$ $= \sqrt{(-3)^2} = \sqrt{9} = 3$ (ii) $\sqrt{(x_2-x_1)^2+(y_2-y_2)^2}$ (Formula) $\#\sqrt{(-11)^2} = \sqrt{11^2} = 11$ an (Formula) .p.w.di $=\sqrt{0+(3)^2}=\sqrt{3^2}=3$



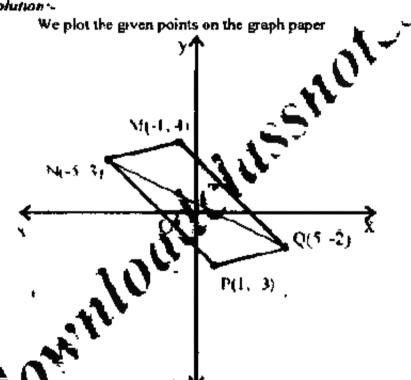
Lengths of opposite sides are equal we find the lengths of the diagonals.

Pilot Superone Mathematics Class 9th $AB^{2} + BC^{2} = 1AC^{2} = 130$

 ΔABC is a right angled thangle m $\angle B = 90^{\circ}$ Similarly all the angle of ABCD are of 90° Therefore point A, B C, D are the vertices of a rectangle

Q.9. Show that the points M(-1, 4), N(-5, 3), p(1, 4)3) and Q(5, - 2) are the vertices of a parallelogram.

Solution ~



e find the lengths of the sides with distance formula.

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
(Formula)
$$|NM| = \sqrt{(-1) + (-5)^2 + (4-3)^2}$$

$$= \sqrt{(-1+5)^2 + (1)^2}$$

$$= \sqrt{(4)^2 + 1} = \sqrt{16+1} = \sqrt{17}$$

(I)



Pilot Superone Mathematics 399 Gass 9th
$$d = \sqrt{(x_1 - x_1)^2 + (y_1 - y_1)^2}$$
 (Formula)

 $PQ! = \sqrt{(5 - 1)^2 + ((-2) - (-3))^2} = \sqrt{(4)^2 + (-2 + 3)^2} = \sqrt{16 + 1^2} = \sqrt{16 + 1} = \sqrt{17}$

(II)

 $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ (Formula)

 $|MQ| = \sqrt{[5 - (-1)^2 + (-2) - (4)]^2} = \sqrt{(5 + 1)^2 + (-2 - 4)^2} = \sqrt{(6)^2 + (-6)^2} = \sqrt{36 + 36} = \sqrt{16}$
 $|NP| = \sqrt{[1 + 3)^2 + (-3) - (3)^2} = \sqrt{(1 + 3)^2 + (-6)^2} = \sqrt{36 + 36} = \sqrt{16}$
 $|NP| = \sqrt{[1 + 3)^2 + (-6)^2} = \sqrt{36 + 36} = \sqrt{16}$
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Prior Superone Mathematics 404 Class 9° M $\left(0, \frac{-5}{2}\right)$

Q.2. The end point P of a line segment PQ is (-3, 6) and its end point is (5, 8). Find the coordinate of the end point Q.

Solution.

Let Q (x, y) be the other end point

Mid-point is R (5. 8)

One end point is P , -3, 6)

$$M(x, y) = M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right) \text{ (Mid-point Formula)}$$

$$5 = \frac{-3 + x}{2}$$

$$10 = -3 + x$$

$$x = 13$$
and
$$8 = \frac{6 + y}{2}$$

$$16 = 6 + y$$

$$y = 10$$
thus
$$Q(x, y) = Q(13 + 10)$$

Q.3. Prove that mid-point of the hypotenuse of a right triangle is equidistant from its three vertices P

(2, 5), Q (1, 3) and R (-1, 0)

Solution. Given points are

We find the lengths of the sides of the triangle.

$$\frac{1}{2} \frac{d}{dt} = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
(formula)

$$= \sqrt{[1 - (-1)]^2 + (3 - 0)^2}$$

$$= \sqrt{(1 + 1)^2 + (3)^2}$$

$$= \sqrt{(2)^2 + (3)^2}$$

$$= \sqrt{4 + 9} = \sqrt{[3]}$$
(i)
$$= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$
(Formula)
$$= \sqrt{[(-2) - (1)]^2 + [5 - 3]^2}$$

$$= \sqrt{(-2 - 1)^2 + (2)^2}$$

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Pilot Superone Mathematics 405 Class 9th $= \sqrt{(-3)^2 + (2)^2}$ $= \sqrt{9 + 4} = \sqrt{13}$ (ii) $RPI = \sqrt{[(-2) - (-1)]^3 + [5 - 0]^2}$ $RPI = \sqrt{(-2 + 1)^2 + (5)^2}$ $= \sqrt{(-1)^2 + (5)^2}$ $= \sqrt{1 + 25} = \sqrt{26}$ (iii) $|QP|^2 + |RQ|^2 = 13 + 13$ (From I, ii) = 26(iv) $|RP|^2 = 26$ (v) $|RP|^2 = |QP|^2 + |RQ|^2$ (From iv, v)

Thus hypotenuse is (RPi where R (-1, 0) and P (-2, 5) are its end point

Let M (x, y) be end point of RP

$$M(xy) = M\left(\frac{-2-1}{2}, \frac{y_1 - y_2}{2}\right)$$

$$= M\left(\frac{-2-1}{2}, \frac{y_2 - y_2}{2}\right)$$

$$= M\left(\frac{-3}{2}, \frac{y_1}{2}\right)$$

Now, we find distance of $M\left(\frac{-3}{2}, \frac{5}{2}\right)$ from the three vertices.

$$M\left(\frac{3}{2}, \frac{5}{2}\right), R (-1.0), Q (1, 3), P (-2, 5)$$

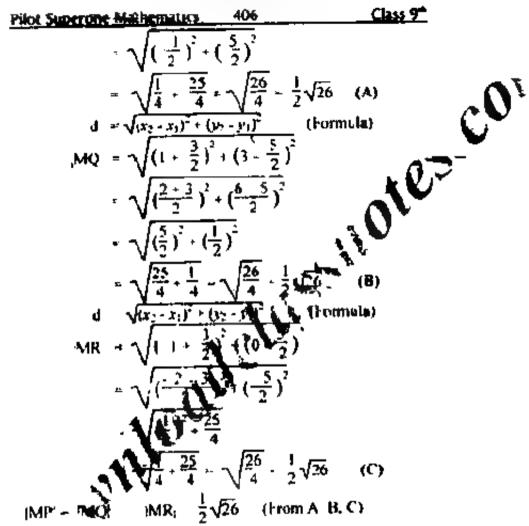
$$d = \sqrt{(x_2 + x_1)^2 + (y_2 - y_1)^2} \qquad \text{(Formula)}$$

$$|MP| = \sqrt{[(-2) - (\frac{-3}{2})]^2 + (5 - \frac{5}{2})^2}$$

$$= \sqrt{(-2 + \frac{3}{2})^2 + (\frac{0 - 5}{2})^2}$$

$$\sqrt{(\frac{4 + 3}{2})^2 + (\frac{0 - 5}{2})^2}$$





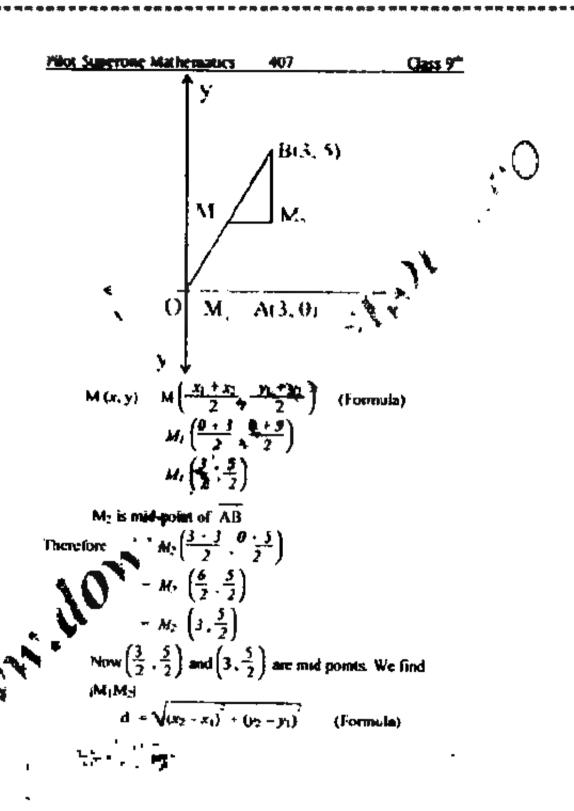
M is equidistant from P. Q. R.

Q.4. If O(0, 0), A (3, 0) and B(3, 5) are three points in the plane find M, and M; as

mid-points of the line segments AB and \overline{OB} respectively. Find M_f M_f : Solution: A (3, 0), O(0, 0) and B(3, 5) are the

sertices of aA. MI is mad-point of OB

Na.



Pilot Superone Mathematics

$$|M_1 M_2| = \sqrt{\left(3 - \frac{3}{2}\right)^2 + \left(\frac{5}{2} - \frac{5}{2}\right)^2} = \sqrt{\left(\frac{6 - 3}{2}\right)^2 + 0}$$

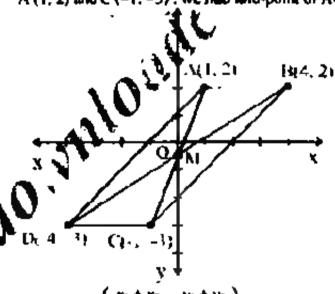
$$= \sqrt{\left(\frac{3}{2}\right)^2} = \frac{3}{2}$$

Q.5. Show that the diagonals of the parallelogram having vertices A (1, 2), B (4, 2),

> C(-1, -3) and D(-4, -3) bisect each other. Solution: ABCD is a parallelogram with vertices A(1, 2), B(4, 2), C(~1, ~ 3) and

D (-4, -3). Suppose diagonals DB and AC intersect at M.

A (1, 2) and C (-1, -3) , we find mid-point of \overline{AC}



Formula

Mid-point of AC = $\left(\frac{-1+1}{2}, \frac{-3+2}{2}\right)$

Prior Superone Mathematics 409 Class 9th $\left(0, -\frac{1}{2}\right)$ (i)

Now B (4, 2), and D (-4, 3) are end points of the second diagonal \overline{BD} .

Mad-posst of
$$\overrightarrow{BD} = \left(\frac{-4+4}{2}, \frac{-3+2}{2}\right)$$

= $\left(0, \frac{-1}{2}\right)$ (ii)

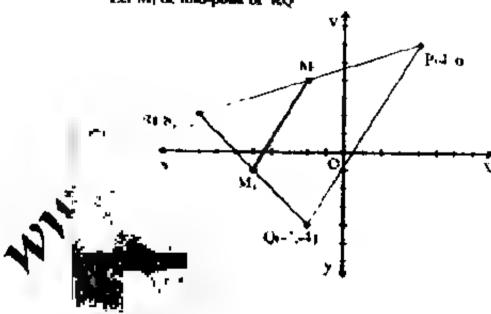
Mid-point of diagonal AC and BD is the same

Q.6. The vertices of a triangle are P (4, 6) Q (-2, -4) and R (-2, 2). Show that the length of the line segment joining the mid-points of the line

segment \overline{PR} , \overline{QR} is $\frac{1}{2}$ \overline{PQ} .

Solution: Ventuces of APQR are P(4-6), Q (-2, -4) and R (-2, 2)

Let M₁ be mid-poset of RO



Pilot Superone Mathematics 410

Then Mars

Then M₁ is
$$M = \frac{8 - 2 - 2 - 4}{2} = \frac{x_1 + x_2}{2} = \frac{y_1 + y_2}{2}$$

$$M_1 = \frac{-10 - 2}{2 - 2}$$

$$M_2 = \text{ inid-point of } RP \text{ then } M_2 \text{ is}$$

$$M = \frac{-8 + 4 - 2 + 6}{2 - 2}$$

$$= M_2 = \frac{-4 - 8}{2}$$

$$= M_2 = (-2, 4)$$
Now we use distance formula
$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} = \text{find } |PQ|$$

M₂ is mid-point of RP then M- is

$$M = \left(\frac{-8+4}{2}, \frac{2+6}{2}\right) \\ = M_2 \left(\frac{-4}{2}, \frac{8}{2}\right) \\ = M_2 \left(-2, 4\right)$$

Now we use distance formula

d
$$\sqrt{(x_1 - x_1)^2 + (y_2 - y_1)}$$
 around [PQ] P (4, 6), Q (-2, -4)

PQ =
$$\sqrt{(-2-4)^2 + (-4-6)^2}$$

= $\sqrt{(-6)^2 + (-4-6)^2}$
= $\sqrt{36 + 140} = \sqrt{136}$
= $\sqrt{2} \times 1 \times 10^{-2} = 2\sqrt{34}$ (A)

Therefore.

$$M_1M_2 = \frac{(2+5)^2 + (4+1)^2}{2}$$

$$=\sqrt{9+25}$$
 $=\sqrt{34}$ (B)

$$= \sqrt{(3)^2 + (5)^2}$$

$$= \sqrt{9 + 25} = \sqrt{34} \quad (B)$$

$$= \frac{1}{2} \text{ (PQ)} \quad \text{(From A and B)}$$

			Revier	v Exe	ercise	9			
Q.1	Chos		correct o			_	•		
(i)	Dista	ike be	tween po	: ылть (О	. 0) and ((1, 1)	is-		
	(ar	G	•	,	(b)	l			
	(c)	2			(d)	$\sqrt{2}$			- ~ \
(iı)			tween th	e point	s (l.0) a	•-	1) 15		`
•	(a)	0		_ ,	(b)	ŧ			
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,	(a)	(1.1	•	4-4	(b)			4	
	(c)	(0, 1			(d)	įΤ.			
(11)	-	-		n is (2,	2) and	•	•		
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	(c)	(0, 0))		(ď)	\mathbf{u},\mathbf{I}			
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	(v)	7	(vi)	Ŧ	(vii)	Г			

Pilot Superone Mathematics 412 Class 9th

- Find the distance between the following pairs of points. S.COM
 - (6, 3), (3, 3) (a) (7, 5), (1, -1)
 - (iii) (0,0), (4, 3)
- Let P(6, 3) Q (3, -3) 3(i)

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$|PQ| = \sqrt{(3 - 6)^2 + (-3 - 3)^2}$$

$$= \sqrt{(-3)^2 + (-6)^2}$$

$$= \sqrt{9 + 36} = \sqrt{45}$$

$$= \sqrt{3 \times 3 \times 5} = 3\sqrt{5} \quad \text{Units}$$

3(n) (7.5), (1.-1)
Let A (7; 5), B (1, 1)

$$d = \sqrt{(x_2 - x_1)^2 + (x_2 - x_1)^2}$$

$$|AB| = \sqrt{(1-7)^2 + (-1-5)^2}$$

$$= \sqrt{(-6)^2 + (-6)^2}$$

$$\sqrt{6 \times 6 \times 2} = 6\sqrt{2} \text{ Units}$$

$$d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$- |OQ| = \sqrt{(-4 - 0)^2 + (-3 - 0)^2}$$

$$= \sqrt{(-4)^2 + (-3)^2}$$

$$= \sqrt{16 + 9} = \sqrt{25} = 5 \text{ Units}$$

- Find the mid-point between following pairs of points.
 - (6, 6), (4, -2)
- (u)
- (5, 7), (7, -5)
- (13)(8,0), (0, 12)

Solutions:-

Let M be mid-point of P(6, 6), (4, -2)

Pilot Superone Mathematics 413 Class 9th

Mild point formula $\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}$ $=M\left(\frac{6+4}{2},\frac{6-2}{2}\right)$ $=M\left(\frac{10}{2},\frac{4}{2}\right)$

= M (5, 2) is the mid-point

4(6) Let M be mid-point of B(-7, 5), A(-5, -7)

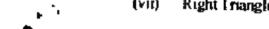
Mid point formula $\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}$ $M\left(\frac{5}{2},\frac{7}{2},\frac{5}{2}\right)$ Thus $=M\left(\frac{12}{2}, \frac{12}{2}\right)$

4(iii) Points P(8, 0) and Q(1, -12) Let M be the mid-point of P(8, 0) and Q(1, 12)

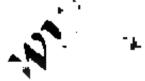
> Mid point formula $\frac{x_1 + x_2}{\sqrt{2}}, \frac{y_1 + y_2}{2}$ Thus mad-point M is $\binom{8+0}{2}, \frac{0-12}{2}$ $=\left(\frac{8}{2} - \frac{-12}{2}\right)$ = (4,-6)

5. Define the following

- (i) Co-ordinate Geometry (n) Collinear
- (hi) Non-collinear
- (v)
- (iv) Equilateral Friangle
- (vii)



Scalene Frangle (vi) Isosceles Frangle (viii) Square



Written/Composed by - <u>SHAHZAD 1FTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>ranshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 9)

Polot Superone Mathematics 414 Class 9th
Definitions:

(i) Co-ordinate Geometry

Cu-ordinate geometry is the study of geometrical shapes in the Cartesian plane co-ordinate plane)

- (ii) Collinear Points

 Two or more than two points which he the same straight line are called collinear points with that line
- (iii) Non-collinear

 Three or more than three points that do not \$6 on a straight line are called non-collinear points.
- (iv) Equitateral Triangle

 A triangle having lengths of its three states the same is called an equilateral triangle.
- (v) Scalene Triangle

 If measures of three sides of a triangle are different then
 the triangle is called a scalene triangle
- (vi) Isosceles Triangle

 If lengths of two sides of a triangle is equal and length
 of the third side is different then that triangle is called
 an isosceles triangle.
- (vii) Right Trigngle

 A triangle having one of its angle as a right angle 90°) is called a right angled triangle
- (viii) Square

 A figure formed by four non-collinear points in the plane is called a square if:
 - (i) All its sides have equal lengths
 - (ii) Measure of each angle is 90°



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Pilot Superone Mathematics

415

Class 9th



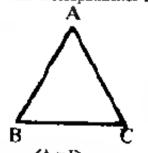
CONGRUENT TRIANGLES

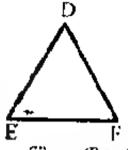
Congruent Triangles:

I'wo triangles are said to be congruent if at least one (1 .) correspondence can be established between them in which the corresponding sides and angles are congruent.

For example:

If in the correspondence \triangle ABC \leftrightarrow A DEF .





(i) Zλ ≥ D

(ii) ∠B ≅ ∠E

(iii) ∠C≘∠F

iivj BC ≅ ∠FF

(Y) CX : FD

(vi) $A\overline{B} \sim DE$

Then A ABC @ A DEF

In such a case we can also say that the correspondence ACC ← A DEF is a congruence.

Angle Side Postulate (S.A.S)

If in a given correspondence of two triangles, the two sides and the included angle of the one triangle are congruent to the corresponding two sides and the included angle of the other, the triangles are congruent in Δ LMN \leftrightarrow Δ POR

If $\overline{LM} = \overline{PQ}$, $m \ge M = m \ge Q$ $\overline{MN} = Q\overline{R}$ Then $\Delta LMN = \Delta POR$

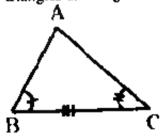
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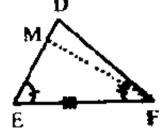
Class 9th

Theorem

In any correspondence of two triangles, if one side and any two angles of one triangle are congruent to the corresponding side and angles of the other, then the triangles are congruent (A.S.A \cong A.S.A)

416





Given

in ΔABC ↔ Δ DEF

∠B≅ZE, RC≡EF. ZC≡ZF

To Prove

 \triangle ABC \leftrightarrow \triangle DEF

Construction

Suppose AB # DE ktake a point M on DE such that

AB = MR. Join M to F

Proof:

<u> </u>	Sychocats	Reasons
In	AABC ← → AMEF AB ≥ ML(i)	Construction
So.	BC ≈ EF (ii) ∠B ≈ ∠E(iii) △ABC ≅ △ MEF ∠C ≅ ∠MFE	Given Given S.A.S postulate (Corresponding angles of congruent triangles)
But	∠C ≥ ∠DFE	Given Soth congruent to ZC

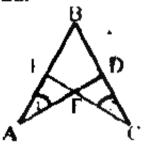
DID.

oni

Pilot Superone Mathematics 417 ZDFL ≈ ZMFL This is possible only if D and M are the same $\overline{AB} \equiv \overline{ME}$ (construction) points and AB ≥ DF and $\overline{ME} = \overline{DE}$ (proved) So. $\overrightarrow{AB} \cong \overrightarrow{DE}$. (iv) Thus from (a), (iii) and S.A.S. postulate (iv), we have AABC #ADEF

Exercise 10.1

Q.1. In the given figure AB # CD ZIM 2 prove that ∆ABD ¥ ∆CBE.



Given: in the given figure

> AB ∗ Ĉ₿ Z 1 = Z 2

To Prove: AABC ≥ ACBI

Statements Reasons Δ' ABC and CBI AB = 775 Cuven Caven ZA = ZC Common **∠B ≥ ∠B** Λ nd S.A.S postulate: ΔABC ≆ ΔCBE

2.2.	From a point on the bisector of an angle perpendiculars are drawn to the arms of the angle prove that these perpendiculars are equal
Soluti	in measure.
	Given: ZPOR is given Q1 is bisector of ZPQR (c Z1 = Z2) (i) M is a point on Q1 (ii) MN : QR MS L Q8 Let 3 . 4 (such 90°)
	Proof: Statements Reasons 10MSe+ 10MN Given Given
(ON ON Common 1 QNS 1 QNN SAS postulate MN = MS Corresponding sides of

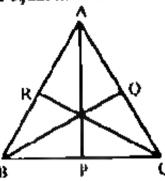
MATHEMATICS FOR 9Th CLASS (UNIT # 10)

isectors of \(\alpha \) and \(\alpha \) that I is equidistant from
isectors of ZB and ZC that I is equidistant from R R R A A That I and CS
that I is equidistant from
an of B1 and C5
and of B1 and CS
and of B1 and CS
and of B1 and CS
n of Bland (\$
vier Bi and (♂
vier Bi and (♂
A A
R ² , 3€
,
Reasons
ats en
ach 90°
Ommou
A S postulate
orresponding sides of
ongruent triangles
rom (iv) and (v)
The state of the s

j	
Class 9 Class	
Prot Superone Mainematics	
Theorem If two angles of a triangle are congruent then the sides	• •
opposite in them are also congruent	`
opposae in them are and	
A	
The state of the s	
$\lambda = \lambda + \lambda$	
<u> </u>	
$\frac{1}{10} \frac{1}{10} \frac$	
V	
Given: In AABC, ∠B • △€	
To Prove: AB & AC	
Canstruction:	
Draw AP bisector of angle A i.e. ∠1 ≥ ∠2. AP cuts	
Dear Vb preceipt of mike it me	
BC at D	
Proof: Reasons	
Statements	
In AABDer AACD	
$\angle A \cong \angle B \cong \angle C$ Given Construction	
21=2-	
AD ≥ ÂD Commor	
AARD = MACD S.A.S postulate	
AB = AC Corresponding sides of	
AB = AC congruent triangles	
• ·	

Exercise 10.2

Q.1. Prove that any two medians of an equilateral triangle are equal in measure.



Given:

In AABC

- (i) $\overline{AB} = \overline{BC} = \overline{CA}$ points P. Q. R are respectively mad points of \overline{BC} , \overline{CA} and \overline{AB} i.e; $m\overline{AR} = m\overline{BR} = \frac{1}{2}m\overline{AB}$
- (ii) $m\overline{BP} = m\overline{CD} = \frac{1}{2}m\overline{BC}$ $m\overline{CQ} = m\overline{AQ} = \frac{1}{2}m\overline{CA}$

Thus $\overline{AR} * \overline{BR} * \overline{BP} * \overline{CP} * \overline{CQ} * \overline{AQ}$ (From i. ii) Medians are $\overline{CR} \cdot \overline{BQ} \cdot \overline{AP}$

To Prove:

ĀP ∓ BQ ≥ ĈŔ

Statements

VH ≈ BC ≈ CA Oppo ∠ABC ⇒ ∠BCA ≈∠CAB sides Now ABCR ↔ ACBQ

ŘC ≥ ŘČ

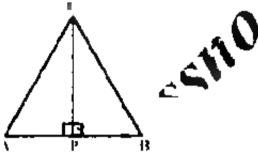
Reasons

Civen Opposite angles of equal sides

Common

manife parameters on

Pilot Superone Mathematics J	Class 9
Z ABC ZACB	Princed
I BR ≥ CQ - A BCR ≥ A CBQ	Cilven SAS≆SAS
Thus ĈŔ ⊕ BQ	Corresponding sides of congruent triangles
Similarly $BQ \triangleq \overline{AP}$ $\overline{AP} = BQ \cong CR$	·
Q.2. Prove that a point, which	egment is on the right
MSECTOR OF THE TIME SEGME	



Given

AB is a line-segment. There is a point C that $\overline{CA} \cong CB$. To Prove:

Point C has de the right bisector of AB Construction:

(i) Fuka, P as mid-point of AB i.e. AP ≇ BP

(ii) Spon point C to A, P, B

Presf.

Statements ABC		Reasons	-
CASCR ZASZB		Given Corresponding angles congruent A'	of

PIN

Pilot Superone Mathematics 4	23 Class 9 th
Now ACAP +> ACBP	
	Proved
ĀP ≘ B P	Construction
· (Thus ΔCAP ± ΔCBP	NAS≅SAS L
(0) $Z1 \cong Z2$ (0) $mZ1+mZ2-180°$	Adjumples on one side of a line
Thus m∠1 - m∠2= 90*	
Hence CP is right	
bisector of AB and point [C hes on CP	And the second
Theorem	,
In a correspondence two trait triangle are congruent to the other, their John two (S.5.5-555)	tights, if three sides of one
Green: In AABC ++ 1	M.t
AB ≥ DI	,,,
BC ± ()	
CV ₹10	
•	

Written/Composed by - <u>SHAHZAD 1FTIKHAR</u> Contact * 03 13-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>raoshahzadiftikhar@qmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 10)

Pilot Superone Mathematics 424 Class 9th

To Prove:

AABC # ADEF

Construction:

Suppose the side $B\overline{L}$ is not shorter than any of the other two sides of the triangle ABC. Construct Δ GEF

with G and D on opposite sides of EF such that

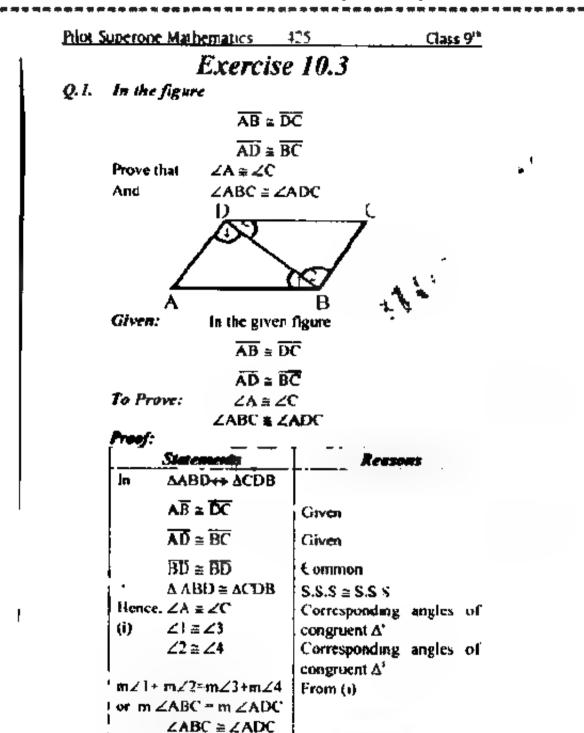
GE ≅AB and ∠CFF ≅ ∠B

Join G and D. Let the angles be named by the numbers as shown in the figure

s shown in the right	
Statements In ∆ABC → AGEF	Reasons
BC ≇ EF ∠B ≅ ∠GEF and AB ≅ GF Thus ∆ ABC ≇ AGEF Now in ∆ EGD (Construction. Construction. LASM S.A.S
DE ≥ GE. 1 v ∠2 ≥ ∠1 (ii) Thus ∠3 ≥ ∠4(ii) m∠2+ m∠3+m∠1+m∠4 or m∠C = m∠D	Each ≅ AB Opposite angles of congruent sides From(r)+(n) Addition postulate of angles
i.e. ZD = ZG Non: in A DL I ++A GEF DE = GB	From (iv) and (v) Each ≅ AB
∠D ≆ ∠G DF ⊇ GF	Proved Each & CA
ADEFEADEL But AABC * AGEF AABC * ADLE	S.A.S.# S.A.S. Transitive property of congruency

NE

7.5



Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact * 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>raoshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 10)

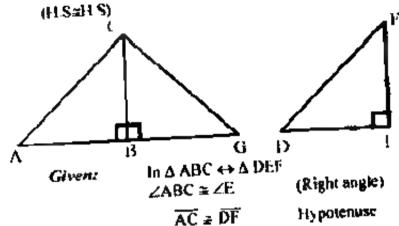
Pilot Superone Mathematics 426 (Lass 9.)
Q.2. In the figure: NP
I. $\overline{LN} \cong MN$ $MN \cong LP$ Prove that $\angle N \uparrow \angle P$ (1) and $\angle NML \cong \angle PLM$ Given: In the figure
MN ± LP
Prove that $\angle N + \angle P$ (1)
and ∠NML, ≅ ∠PLM
1N ≥ MN
MN SIP * /
To Prove
ZIRMIL = ZIPLM
Proof:
Statements Reasons
In Al Miler ALMP
III Marie Action
- TINE MP
Given
MN - IP
ÎM≅ M Given
TWIET W
∴ ΔIMN ≅ ΔLMP Common
Thus ∠N ≡ ∠P
ZNML ≅ ZPLM S.A.S ≥ S A S
Thus $\angle N \equiv \angle P$ $\angle NML \cong \angle PLM$ S.A.S $\cong S$ A S

Prot Superone Mathematics 427 Class 9 Prove that the median bisecting the base of an isosceles triangle bisects the vertex angle and it is perpendicular to the base. Given: $n\Delta ABC$ (I) AB ~ AC Point P s mid-point of BC .e. THE a C'P (ii) P is joined to A i.e AP is median (iii) To Prove. Statements MBP + MACP AB & AC Given SF 3 CP G ven AF & AP Common A ABP . SACP SAS . SAS Z1≅Z2 Corresponding angles of congruent ir angles 23 € 24 But(11)m∠3+m∠4 -180° Thus m∠3 m∠4= 90° | Corresponding angles of congruent triangles therefore From (1) and (1i)

Pilot Superone Mathematics 428

Theorem

if in the corresponding of the two right-angled triangles, the hypotenuse and one side of one triangle are congruent to the hypotenuse and the corresponding side of the other, then the triangles are congruent



BC = EF

To Prove: A ABC # A DEF

Construction.

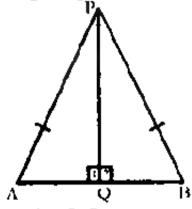
Produce AB towards B and cut off BC = DE		
Stwements	Reasons	
In AGBC m ∠CBG = 90° In AGBC ↔ ADEF	Supplementary of 90°	
GB ≥ DE ∠GBE ≅ ∠E	Construction Each 90°	
BC ≥ FF	Given	
AGBC # ADEF	S.A.S ≅ S.A.S Corresponding sides of congruent triangles	
But DF ≅ AC	Given Transitive property	

Class 9th 429 Prior Superone Mathematics Thus GC ≅ AC Corresponding angles of Now in A ACG. congruent sides ∠A ≈ ∠G Now in $\triangle ABC \leftrightarrow \triangle GBC$ Proved Proved $\overline{AC} \cong \overline{GC}$ Each 90° 5.A A 2.5 A.A ∠A ∓ ∠G Proved ZABC ≅ ZGBC Thus AABC = AGBC Transitive v fragord congruency AGBC = ADEF Hence AABC & ADFF

Exercise 10.4

Q.1. In \triangle PAB of figure, $\overline{PQ} \perp \overline{AB}$ and $\overline{PA} \cong \overline{PB}$,

prove that 4Q ≈ BQ and ∠APQ ≈ ∠BPQ



Given:

In A PAB

- (a) <u>PA</u> ≈ PB
- (ii) $\overline{PQ} \downarrow \overline{AB}$ i.e. $m \angle 1 + m \angle 2 + 90^\circ$

To Prove: $\overline{AQ} \cong BQ$ $\angle APQ \cong \angle BPQ$

	Proof:	
	Statements	Reasons
	In ΔΑΡQ ↔ ΔΒΡQ ∠1 ≅ ∠ 2	Given cach 90°
	PA ≅ PB	Given
	PQ ÷ PQ Thus ΔΑΡQ ≃ ΔΒΡQ	Common H.S. a. H.S.
	$\overline{AQ} \cong BQ$	Corresponding sides of congruent triangles.
	∠ APQ ≟ ∠BPQ	Corresponding angles of congruent trigngles.
0.2	In the figure m ZC 2 m	$\angle D = 90^{\circ}$ and $\overline{BC} \simeq 4\overline{D}$
	Prove that $4\bar{C} \cong \overline{BD}$ and	
	[)	(= 2.100.
	D D	- A
)	
)	
	, D	S B
	Given: In the given	figure B
	Given: In the given m 2'C m.	figure (1)
	Given: In the given m 2'C m. BC = A	figure ZD 90° (i)
	Given: In the given m 2'C m.	figure (1) (D) 90° (1) (D) (D)
•	Given: In the given m 2C m. BC = A To Prove AC = B	figure (1) (D) 90° (1) (D) (D)
Į,	Given: In the given m ∠C m. BC ≥ A To Prove ĀC ≥ B ∠ BAC ≥ ∠	figure (1) (D) 90° (1) (D) (D)
7	Given: 15 the given m ∠C m. BC ≥ A To Prove AC ≥ B ∠ BAC ≥ ∠ Proof: Statements In \(\alpha \text{BB} \text{\text{BAC}} \)	figure (1) (ABD)
7	Given: In the given m ∠C m. BC ≥ A To Prove AC ≥ B ∠ BAC ≥ ∠ Proof: Statements In ABD ↔ ΔBAC AD ≥ BC	figure (i) (i) (i) (i) (ii) (ii) (iii) (ii
7	Given: In the given m ∠C m. BC ≥ A To Prove AC ≥ B ∠ BAC ≥ ∠ Proof: Statements In ABD ↔ ΔBAC	figure (I)
Q.	Given: In the given m ∠C m. BC ≥ A To Prove AC ≥ B ∠ BAC ≥ ∠ Proof: Statements In ABD ↔ ΔBAC AD ≥ BC	figure (i) (i) (i) (i) (ii) (ii) (iii) (ii

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lot Superone Mathematics	131 Class 9**
$\cdot \qquad \overline{\mathbf{AC}} \succeq \overline{\mathbf{BD}}$	Corresponding sides of congruent triangles.
∠ BAC ₃ ∠ABD	Corresponding angles of congruent triangles
3. In the figure, $m \angle B =$	$m \angle D = 90^{\circ}$ and $\overline{AD} \simeq \overline{BC}$
Prove that ABCD is # 1	rectangle.
D	<u>C</u>
<u> </u>	
A Given. In the figure	Ŕ
an are right	Pr. Ja Ba
-	
(0) AD BC To Prove,	· •
ABCD is a rectangle (1.2) Constructions Join A to C Proof:	ΛĒ Īχ
Statements In 'AABC +> ACDA	Reasons
H → D	Owen (each 30°)
BC AD	Orven
# AC - AC	Common
77BC - 7CD7	HS&HS
Hence AB - DC	Corresponding sides of

Pilot Superone Mathematics 432 (lass 9)
REVIEW EXERCISE 10
1. Which of the following are true and which are
false?
(i) A ray has two end points
(ii) In a triangle, there can be only one right angle (iii) Three points are said to be collinear if they lie on same
(iv) Two paraller lines intersect at a point.
e I
(vi) A triangle of congruent sides has non-congruent angles.
Answers:
False (ii) True True
(Iv) False 1 12 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
0.2 If ∆ABC ≅ ∆LMN
, M
£
P ' ' ' '
- Jan
h ^e in him
B
Them m ∠M ()
. m∠N(n)
m ZA (nt)
Anguers:
$m = 484 \text{ 30}^{\circ}$ Gb $m \angle N = 60^{\circ}$ (10) $m \angle N = 70^{\circ}$
O 1 If MBC = ALMN, then find the unknown x.
C. M
ΔV_{*} " Σ "
607
V ₁₀ ≈₁V V

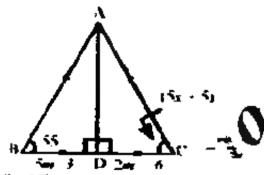
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Pilot Superprie Mathematics 433 (Less 9" Insurer:

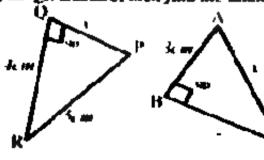
m/N 💣 60°

Q.4. Find the value of anknowns for the given congruent triangles.

Solution:-



Q.5. If APQR = AABC, then find the unknown.



Solution,-



Pilot Superone Mathematics Class 9" 6 (iii) -lem

- Remember
- in any correspondence of two triangles, if one side and any two angles of one triangle are congruent to the corresponding side and angles of the other, the two triangles are congruent (A.S.A = A.S.A)
- if two angles of a triangle are congruent, then the sides opposite to them are also congruent.
- in a correspondence of two thangles, if three sides of one triangle are congruent to the corresponding three sides of the other, then the two triangles are congruent (S.S.S = S.S.S)
- If in the correspondence of the two right-angled triangles, the hypotenuse and one side of one triangle. are congruent to the hypotenuse and the corresponding side of the other, then the triangles are congruent $(HS \ge H.S)$
- Two triangles are said to be congruent, if there exists a correspondence between them such that all the corresponding sides and angles are congruent.

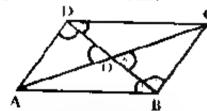
William Gowkil

Unit
PARALLELOGRAMS AND TRIANGLES

Theorem

in a parallelogram

- (i) Opposite sides are congruent
- (ii) Opposite angles are congruent
- (m)The diagonals bisect each other



Given: ABCD is a || that AD | BC and AB || DC Diagonals

 \overline{AC} and $B\overline{D}$ cut each other at O.

To prove

- (i) $\overrightarrow{AD} \cong \overrightarrow{BC} , \overrightarrow{AB} \cong \overrightarrow{DC}$
- (ii) ∠ABC ≅ ∠AIX∠BAD ≅ ∠BCD
- $\begin{array}{cc}
 OA & O\overline{C} \\
 \overline{OR} & \overline{OO}
 \end{array}$

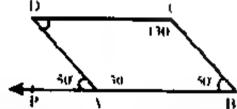
J _		≅ OD
Proof		
'	Matements_	Reasons
4	$\Delta ABD \leftrightarrow \Delta CDB$	1
1/	∠2 à ∠1	Alternatgrangles
Market Ch. S.	BD ≆ BD	Common
	∠4 <i>≟</i> ∠3	Alternate angles
	$MBD \cong MDB$	$ASA \ni ASA$
N'		Corresponding sides

Pilot S	uperone Mathematics	436	Class 9"	
		of congruent triangles		
	and $\overline{AD} \triangleq \overline{BC}$	proved		
	Now ∠2 = ∠1 (n)	proved		_ 🐧
	∠4 ≆ ∠3 (a)	from (i) + (ii)		,c01
mZ2	$+ m \angle 4 = m \angle 1 + m \angle 3$		خم	\mathbf{v}
or	$m\angle ADC = m\angle ABC$. 0.) ,
ĺ	or ZADC ≅ ZABC			
1	and ∠BAD ¥ ∠BCD		notes	ł
 	or MOC \leftrightarrow MO4	around 9	.J.	
	$\widetilde{BC} \cong \widetilde{AD}$	proved proved	.7	
	26 ≥ 25	Proven	,	- 1
	∠3 ≥ ∠4	`	;	
	ABOC > ADOA	opp Vertical angles	•	
	Thus OC = OA		,	1
	and OB.≅	Alternate angles	İ	
	٠, ٩٧	AAS > AAS		- }
i.				\$
•	λV`.			
- (<i>o</i>		,	
- AN	•			
Williams.				
1				
7				
1				

Prior Superone Mathematics 437

EXERCISE 11.1

Q.1One angle of a paradelogram is 130°, band the measure of its remaining angles.



Given ABCD is a parallelogram in which mZBAD = 130°

To prove: lotind m∠B m∠D m∠(

Construction Produce BA towards A Proof

Statements	
ABCD is a parallelogram	
in which	

 $m\angle DAB = 130^{\circ}$ Given

m∠C 130° **LOpp**osite angles of "

 $m\angle D(P = |B|)^n = |B|0^n$ Adj. supplementary angles

 $mZB = 50^{\circ}$ Corresponding angle of ZDAP

 $m\angle D = 50^\circ$ Opposite angle of $\angle B$

One exterior angle formed on producing one side of a parallelogram is 40°, band the measures of its interior angles.



Given: ABCD is a parallelogram $\overline{B4}$ is produced towards A

and angle $\angle DAP = 40^{\circ}$

Required: $m\angle BA(t) = 0$

Phot Superone Mathematics	138 Class 9*
m/B = '	
m2€ = °	
$m_s(D) = \pi^{r_t}$	
Proof:	·
Statements	Reasons
AB(: 1) is a parallelogram and	l.
m. D3P 40"	
m∠D (P + m ≥ D (B - 180°)	Adj supp angles
$40^{0} + m \angle D/(B - 140^{0})$	$m\angle DAP = 40^{6}$ given
<i>m∠D1B</i> 180° 40°	
m∠D.1B 140° (t)	- 14- 15- 15- 15- 15- 15- 15- 15- 15- 15- 15
m2C 110° (ii)	Opp. Angles of #"
m. B · m/l)AP	Corresphoding angles
m / B = 40°	
m∠D 40° m∠D m∠B	Opp. Angles of "
Thus ma D.18 140°	Prayed
m∠# = 40°	1
m∠(_ =)40°	ţ
	eorem, '
If two oppositionales of a quad	Lustern are confluent and
parallel, it is a pseudiclogium	<u>_</u>
	
- 5 * - 	\
₹ ₹\$	X
	В
Given: In a quadrilateral AB	CD, we have
(i) 1B - DC -	

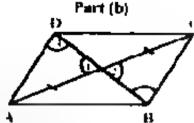
Pilot Superone Mathematics	439 Class 9°
(H) ./Bjc/Dc	1
Required: ABCD is a paralle	logram
i.e. <u>Ai) ≥</u> B(The state of the s
AD _{II} BC	
Construction Join B to 1) Proof	
, Statements.	Reasons
In MBD ↔ V(DB	
$A\overline{B} = D\overline{C}$	Given
	Afternate angles of lines
BD ≥ BD	Сестивон
AABD ≥ ∆C DB	S.A.S ≥ S.A.S
Vinc. ∠4 ± ∠3 (i)	Corresponding angles of
	congruent triangles
ADNOC (ii)	from (a)
und AD ≥ BC (iii)	Corresponding sides of
_	congruent triangles
- also AB DC	gren
ABDC matter	
	•

Exercise 11.12 Q.1. Prove that a quadrilateral is a parallelogram if its opposite angles are congruent (b) diagonals baseds each other Part (a) Given: in quadrilateral ABCD (i) 23 \(\tilde{L} \) 22 \(\tilde{L} \) 13 \(\tilde{L} \) 15
Given: In quadrilateral ABCD (i) 23 \(\alpha 2 \) (ii) \(\alpha 2 \) (iii) \(\alpha 2 \) (iii) \(\alpha 2 \) (iii) \(\alpha 2 \) (iven: ABCD is a liming i.e. \(AD \), \(\beta C \) and \(AB \) (CD (const. Produce \(AB \) towards B and \(CB \) sowards B (const. Produce \(AB \) towards B and \(CB \) sowards B (const. Produce \(AB \) towards B and \(CB \) sowards B
Given: In quadrilateral ABCD (ii) 23 = 21 (iii) 22 = 24 To prove: ABCD is a lim i.e. ADI BC and AB (CD) Const: Produce AB unwards B and CB sowards B Proof Statement Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z \frac{3}{2} \) \(Iii \) \(Iii \) \(AB \frac{1}{2} \) \(Iii \) \(Iii \) \(AB \frac{1}{2} \) \(Iii \)
Given: In quadrilateral ABCD (i) \(Z \frac{3}{2} \) \(Iii \) \(Iii \) \(AB \frac{1}{2} \) \(Iii \) \(Iii \) \(AB \frac{1}{2} \) \(Iii \)
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
Given: In quadrilateral ABCD (i) \(Z3 \Rightarrow Z4\) (ii) \(Z2 \Rightarrow Z4\) To prove: ABCD is a lim i.e. \(AD \rightarrow BC\) and \(AB \rightarrow CD\) Const: Produce \(AB \) towards B and \(CA \) sowards B Proof Statements Reasons
(ii) Z2=Z4 To prove: ABCD is a fin i.e. AD BC and AB CD Const: Produce AB towards B and CB sewards B Proof Statements Reasons
(ii) L2=L4 To prove: ABCD is a fin i.e. AD BC and AB CD Count: Produce AB towards B and CB sewards B Proof Statements Reasons
To prove: ABCD is a lim i.e. AD BC and AB CD Const: Produce AB towards B and CB sewards B Proof Statements Reasons
Count: Produce A6 towards B and Cff savards B Proof Statements Reasons
Const: Produce AS towards B and CR sowards B Proof Statements Reasons
Statements Reasons
Statements Reasons
Vens ∠3 ± ∠1 (r) GIVER
25 a 21 (iii) Vertical opposite angles
Z3 = Z5 1 From (1) and (11)
NIE COLAD
$AP C \overline{D}$
or BC AD
and ABICD
~1
ABC Disa,
-

Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>raoshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 11)

Pilot Superone Mathematics 441 (Class 9)



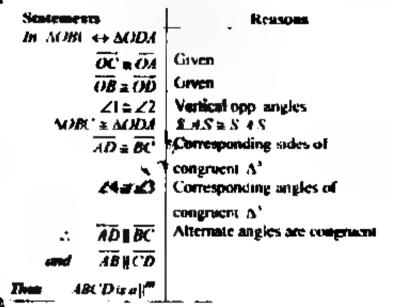
Given: ABCD is a quadrilateral in which

 $4\tilde{C}$ and $B\tilde{D}$ diagonals that bisect each at O. i.e.

0.4 ≥ OC and \(\overline{OB} \approx \overline{OD}\)

Required: Quadrifateral ABCD is parallelogram

Proof



Q.2. Prove that a quadrilateral is a parallelogram if its apposite sides are congruent.





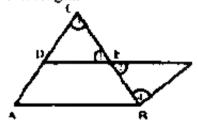
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MATHEMATICS FOR 9TH CLASS (UNIT # 11)

Prior Superone	Mathematics	442	Class 9th
Govern: In quad	nlaterar ABCD		
(i) To Pra	ĀB ÷ DC (ii)	AD ≥ BC	
ABCD Pro of.	rs a parallelugram	i.e; AD BC . AD	BC .
	Statements_	Acam	-
	AABO ↔ AC'DB		
	AD · BC	Given	\mathbf{O}^*
i	AB ≈ ĎĈ	Grven	•
	BD BO	Common	
i	AABO = KCDB	5.5.9.7.7.5	l C
l hus I	.1 .2	Conception Δ'	ngies oi
	Z4 · Z3 📉		
None	Z1° Z2	Proved	
(1)	AD BC	Alternate angles congruent	are
and	211/4" -		
, Thus (a	AB NOC	1	
	ARCD KE 🚾 🔄	<u> </u>	

Theurem

The time segment joining the mid-points of two sides of triangles, is parallel to the third side and is equal to one half of its length.



Pilot Superone Mathematics 443 Class 9"

Given:

In AABC, the line segment \overline{DE} , joins the mid-points of

AC and BC Required:

$$\overrightarrow{DE} \parallel AB$$

 $\overrightarrow{DE} = \frac{1}{2} (\overrightarrow{mAB})$

Construction.

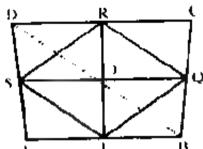
(i) (ii)	Produce DE towards Join B to F	Eand out off mLF - m DF
Proo		-
ln .	Statements	Kenton
, IN	$ADF C \leftrightarrow AFEB$	1 2
,	DF ≥ FF	Construction
	∠I ≑ ∠2	Vertical opp Angles
1	CE ≥ FB	Grven
•	ΔDIC ≅ ΔFEB > ∠3 ≅ ∠4	1 \$ A \$ a \$ A \$ 4 Corresponding angles of
	27824	Congruent triangles
	CD ≅ BF	Corresponding sides of congruent triangles
i	⊼D ≱ क्रि	As CD & AD
	AC & BF	As Alternate angles are congruent
fhus	AD # BF	As AD BE and
ſ.	ABID is ***	ĀD - BF
*	DF AB	
Le;	DF AB	



Pilot Superone Mathematics 444 Class 9th

Exercise 11.3

Q.1. Prove that the line-segment Johning the mid-points of the opposite sides of a quadrilateral bisect each other.



Given:

- (i) ABCD is a quadrilateral points P. Q. R. S are the mid-points of **AB** . **BC** . **CD** and **DA** respectively
- (ii) Pis joined to R
- (iii) S is joined to Q

PR and SQ intersect each other at O Required:

 $\overline{OS} = \overline{OQ}$

 $\overline{OR} = \overline{OP}$

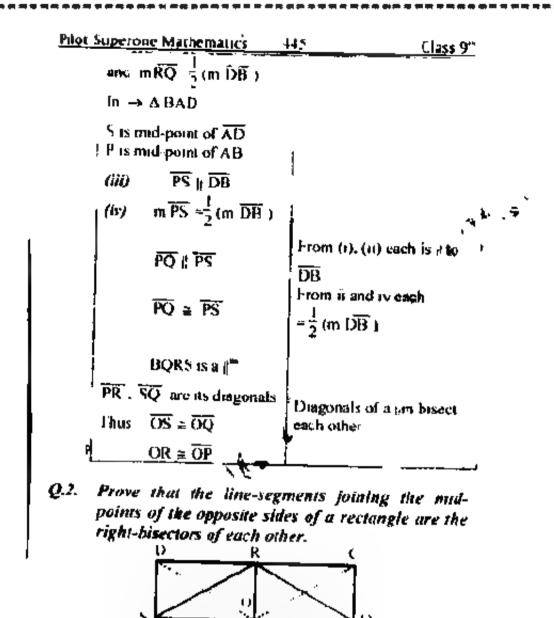
Construction:

- Join P. Q. R. S in order
- (#) Join Bito D

Proof:

Statements	R.COSOTIS
ln ABDC	•
R is mid-point of DC	Given
Q is mic-point of BC	Given
Therefore(1) RQ DB	

NE



Given:

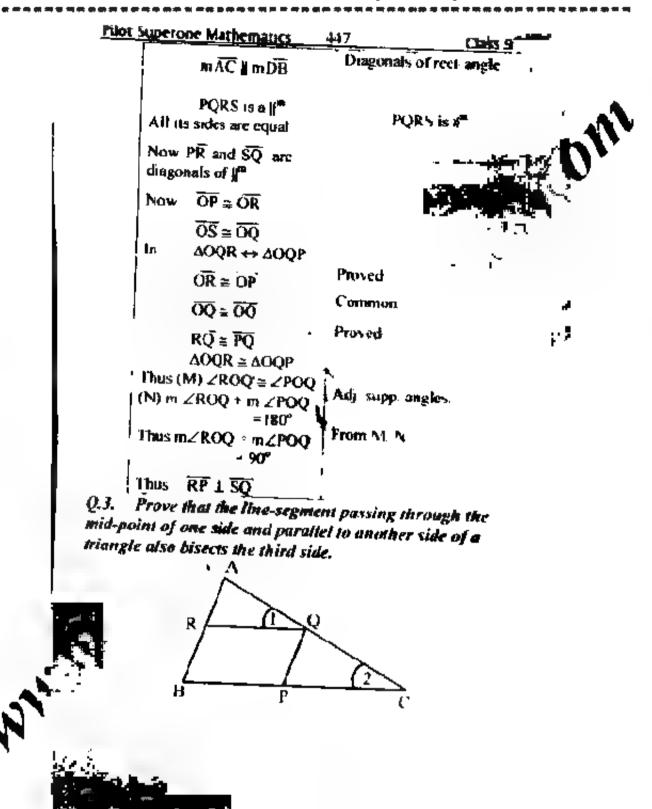
O ABCD is a rect-angle

MATHEMATICS FOR 9Th CLASS (UNIT # 11)

Pilot Superone Mathematics	4-76	Class 9th	
(ii) P. Q. R. S are	mid-points of AF	BC, CD ans	
DA respective	ely.		
(iii, RP and SQ Required.	cut other at O	_	, , ·
	$\overline{OP} \cong \overline{OR}$	C	T
	$\overline{OS} \cong OQ$	*`.•	
and	RP = SQ	•	Ì
Construction: (i) Join P. Q. R. (ii) Join A to C Proof:	S in order	Reasons	
Statements .n AABC		Vernous '	
P & mid-point of AE	Given		
, Q is mid-point of \overrightarrow{B}		,	
(i) : PQ AC			
(ii) mPQ - (m AC	' }	ŀ	
Suppler in AAD		1	
AND SR AC	•		
\sim tory mSR $\frac{1}{2}$ m	AC		
▲ ()		, (n) e≄ch _i ĀC '	
PQ SR	Lach = :	m DB	
mRQ ii m Si By joining B to D. o prove	_	ĺ	
20 4 70	P	m AĈ	
,			

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MATHEMATICS FOR 9TH CLASS (UNIT # 11)

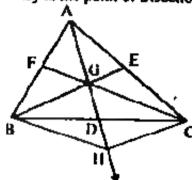


Phot Superone Mathematics 44	8 Class 9th
Given: (i) AABC point Q is mit	-point of AC
QR HBC which cuts	AB at R.
Required: (i) RA - BR Construction: (i) Take P as mid-po	ant of BČ
(ii) Join R to Q.	
Proof:	Zeasons .
Now RQ BC $mR\tilde{Q} = \frac{1}{2} (mBC)$	Given ()
mRQ mPC In AAQR ↔ AQCP	P is med point of BC
In AAQR ← AQC AQ = QC ∠I = ∠2 RQ PC AAQR = AQCP	given Corresponding angles Proved S.A.S ≅ S.A.S
$A\widetilde{R} \sim QP$ (M) $B\widetilde{P} = PC$	construction
(N) But RQ - PC	, proved
RQ - BP	From M. N
RQ BP BPQR	Given ,
(I) $RB = QP$ (I) $AR = QP$ Thus $\overline{AR} = \overline{RB}$	Proved
ur RA≈BR	from (i) and (ii)

Pilot Superone Mathematics 449 Class 9th

Theorem

The medians of a triangle are concurrent and their point of concurrency is the point of trisection of each median.



Given:

In $\triangle ABC$ \overline{BF} and \overline{CF} are medians that intersect at point G.

- (i) All the three medians of triangle ABC are congruent at point G.
- (iii) Point G is the point of trisection of each medians.

Required:

(i) Join A B G and produce shead. It cuts BC at D.

Take GH ≃ AG

Joan H to B and C

Statements	Reasons
In ΔABH (i) F is mid-point of AB	Given



Not Superone Mathematics	450	Class 9 th	
(ii) G is mid-point of A	Construction		
FG∦EH or GČ∦EH			
Similarly GB HC	İ		-6
Thus BHCG is a BC	and		
GH are its diagonals Hence		ي جريوس	•
(M) Thus BD ≅ CD			
(N) and $\overrightarrow{\text{OD}}$ ∓ $\overrightarrow{\text{HD}}$		A W	'
Point D is mic-point of	BC ↓		
We can say \overline{AD} is median. It passes through G	Construction		1 1
AD ≊ GF Are concurrent	A≱ GD ≠ DH	i	
Now m/G = mGH			
mÃŌ - 1mŌŌ	ì		
<u>神(荷</u> 2 南(荷)			
$\overline{GD} = 2$	1		,
Fight G is point of trise Similarly it can be p what G is point of trise	roved ['
of CF and BE is			İ

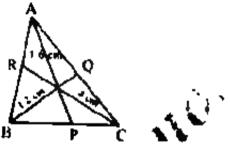
Pilot Superone Mathematics 451

Class 9th

Exercise 11.14

Q.1. The distances of the point of concurrency of the medians of a triangle from its vertices are respectively 1.2 cm, 1.4 cm and 1.6 cm. Find the lengths of the medians.

Solution:-



Let AP EQ. CR be medians of AABC

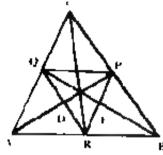
Length of
$$\overline{AP} = 1.6 + \frac{1.6}{2}$$

1.6 + 8
2.4 cm

Length of
$$\overline{BQ} = 1.2 + \frac{.2}{2}$$

1.ength & CR =
$$14 + \frac{14}{2}$$

Q.2. Prove that the point of concurrency of the medians of a trougle and the triangle which is made by joining the mid-points of the sides is the same.





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MATHEMATICS FOR 9TH CLASS (UNIT # 11)

Pilot Superone Mathematics 452 Class 9th Given:

ABC is a triangle \overline{AP} , \overline{BQ} , \overline{CR} are its medians that are concurrent at point G; $\overline{AR} \cong \overline{BR}$, $\overline{BP} \cong \overline{CP}$;

 $\overline{CQ} \cong \overline{AQ}$ points P, Q and R are joined together. PQR is a triangle formed by joining the mid-point of the sides of $\triangle ABC$

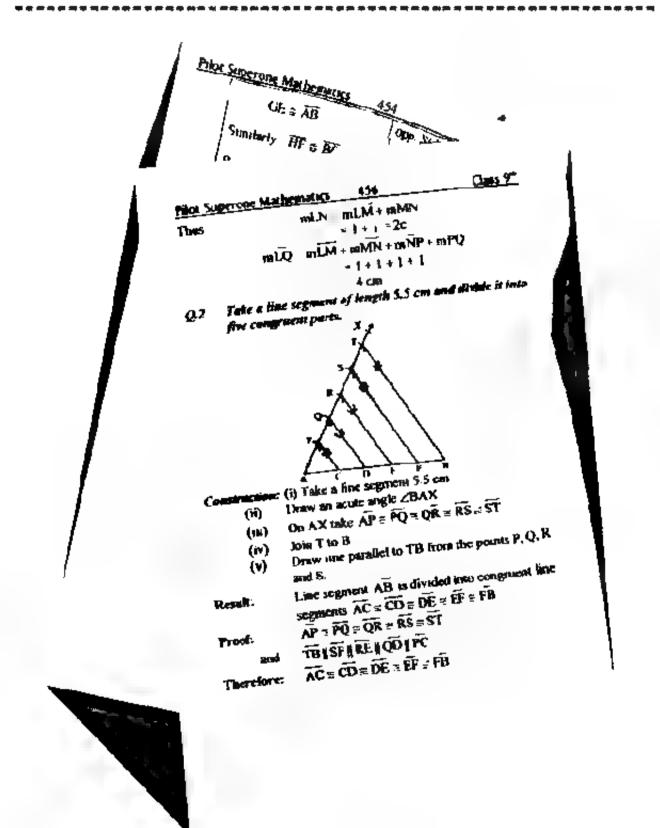
Required:

 $R\overline{F}$, \overline{PD} , \overline{QE} are the medians of triangle PQR and these pass through G also

Proof:	
Statements	,
In AABC	As # Q are mid-point of
ŎP Į ĀB	AB AC
or QF AB	App And
or QF AR	•
Thus F is mid -position Q	1
E is mid-point of PR and	D
is mid-politic of QR	
Prostore, RF, PD and Q	E
medians of triangle PC these pass through G	(* <u>)</u>
ience the result	

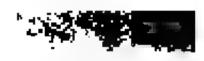
Orth dr. parallel lines make congruent PROJET SUPERIORS Mattersus transcript that the intercell Theorem If the segments on any other time that cars them. If three or many cof В n and nanaversal couls these parallel lines at A. B. (respectively that $\overline{AB} \cong \overline{BC}$ Glyen Another tracisus sail p cuts those lines of D, E, F (#) ex-pectively (vi) Gŕ Passing through F and E take line segment FH, EG DE ≈ ef Required. Consiruction: Require parallel to Solution. AB II OF IN AG IBE Statements AB AGEB 15 8 Teamsversal I L, M. ĀB Z Š LMak when as Therefore - = mP.Q - lem

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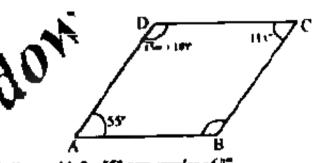
Pilot	Superoi	ie Math	iematics -	457	□ass 9°	
	R	EVI.	EW EXI	ERCI	SE 11	
1.		the bl				
	(i)	in a p	arallelogram e	эрровае	sides are	
	(ii)		araticlogram (
	(iii)					
	(iv)	Medians of a triangle are				
	(v)	Diagonal of a parallelogram divides the parallelogram into two triangles				
	Ausw					
		(i)	congruent	(ii)	congruent	
		(iti)	bisect	(iv)	concurrent	
		(v)	congruent			
Q.2.	in the	perali	clogram AB(CD C		
	(u) m			(i) (u)	7	
		1413 1423	(iii)			
	א ניינ ו	124=_	(N)	-		
	#3 63 = 1	48	hc:			





(ii) mBC = mAD(iii) mL1=mL3(iv) mL2=mL4

Pilot Superone Mathematics 458 hind the unknowns in the given figure. 0.3 Solution: mZC=mZA (i) $\mu^{*} = 75^{\circ}$ (Alternate angle) * y" = 75" (ii)Adj Sign angle y'' + y'' = 180''x' + 75' = 180'x" 180" 75" x" 105" (#) an" = X" **-" - 105**" (iv)If the gives figure ABCD is a parallelogram, then 0.4 find x, 🖛



Solution: $14\pi^2 = 55^* opp. ungles of []^2$

$$x = \frac{55}{31} = 5 \tag{6}$$

 $N_{OW} = (5m + 10) + 55 = 180$

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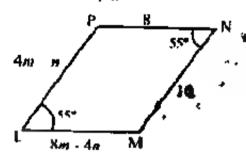
Class 9th

5m + 10 + 55 = 180

$$m = \frac{115}{5} = 23$$
 (11)

Q.5. The given figure LMNP is a parallelogram.

Find the value of m, a.



Solution: $4m + n = 10 \text{ oppsides of } ||^m (I)$

$$16m + 4n = 40$$

$$8m - 4n = 8$$
 multiplying by 4

$$24m = 48$$

(Adding)

$$m = \frac{11}{24} = 2$$

Putting

$$m = 2$$

$$4(2) + n = 10$$

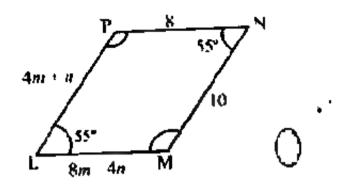
$$8 + n = 10$$

$$n = 10 - 8 = 2$$



Prior Superone Mathematics 460 Class 9"

Q.4. In the question 5, sum of the opposite angles of the parallelogram is 110°, find the remaining angles.



Solution
$$m\angle P + m\angle L = 180^\circ$$

 $m\angle P + 55 = 180^\circ$
 $m\angle P = 188 - 5$
 $m\angle P = 125^\circ$
 $m\angle M = 125^\circ$

Palot Supercine Mathematics 461

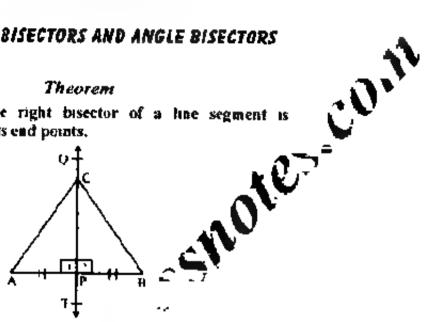
1 355.9



LINE BISECTORS AND ANGLE BISECTORS

Theorem

Any point on the right bisector of a line segment is equidistant from its end points,



AB is a line segment Given: (i)

 \overline{QT} is a right bisector of \overline{AB} i.e. $\overline{AP} \cong \overline{BP}$ (II) QI LAB

m_(1 = m_(2 = 90°

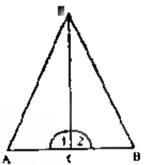
- Point Resion OT C 18 10 act to A and B (iii)
- (m)

	Required: CA MCB	
	Proof: Statements	Reasons
	In 4CAP ← → ACBP	
	m21 ≥ ∠2	Given
	CP = CP	Common
_	ĀP ≟ BP	Given
_	So ∆CAP ≅ ∆CBP	SAS≅SA.S
	$\overrightarrow{CA} \cong \overrightarrow{CB}$	Corresponding sides of congruent A ^s

Pilot Superone Mathematics 462 Class 9th

Converse of Theorem

Any point equidistant from the end points of a line segment is on the right bisector of it.



Given:

AB is a line segment

Point P is such that PA = PB

Required:

Point P is on the right bisector of AB

Construction. Take C mid point of All Le

AC ≅ BC and point P to C

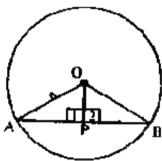
Proof	Statements	Reasons
So III	In AACP CA = BC PA = PB PC = PC ΔACP = ΔBCP (i) m∠1 = m∠2 (ii) m∠1 + m∠2 = 180° m∠1 + m∠2 = 180° m∠1 + m∠2 = 180° m∠1 - 90° PC + AB	Construction Given Common S.S.S ≈ S.S.S Corresponding angle of congruent A ^S Adj Supp. Angles m∠2 = m∠1

Thus PC . AB and point C on it.

Pilot Superone Mathematics 463 Class 9'

EXERCISE 12.1

Q.1 Prove that the centre of a circle is on the right bisector of each of its chords.



- Given: (i) O is the centre of a circle
 - (ii) AB is chord of the circle

Required: Centre O has on the right binector of AB

Construction. (1) Take mid-point of AB as P.

(II) Join P to O O to A and B.

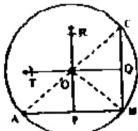
Proof:	1 1
Statements	Reasons
In $\triangle OPA \longleftrightarrow \triangle OPB$ $\frac{PA}{OP} = \frac{PB}{OP}$ $OA \neq OB$ Therefore $\triangle OPA \cong \triangle OPB$ $m \leq 1 \implies m \leq 2$ (i) $\Rightarrow PA = m \leq 2$	Construction Common Radii of a circle S.S.S = S.S.S Corresponding ar congruent \(\Delta^{3} \)
(ii) Am∠1 + m∠2 180° Flus m∠1 m∠2 90° OP is right bisector of AB and O lies on it.	Adj Supp Angles From (1) and (11)

angles

of

Pilot Superone Mathematics 464 Class 9th

Q.2 Where will be the centre of a circle passing through three non-collinear points? And why?



Given:

A, B, C are three non-collinear points and a

circle is passing through these points

Required:

To find the centre of the circle and to prove that

a is the centre.

Construction: (a) Join B to A and C.

(ii) Take PR right bisector of AB.

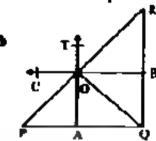
(ni) Take QT right bisector of BC

PK and QT intersect at point O

	Proof:	
ſ	Statements	Reasons
ĺ	PO is right bisector of AB	
1	ÓA ≟ÕB (i)	į
İ	QO is night biscolor BC	
١	, OB : OC (ii)	
٦	• OA = OE = OC	From (i) and (ii)
İ	Hence O is centre of the circle	

Pilot Superone Mathematics 465 Class 9th

Q.3 Three villages P, Q and R are not on the same line. The people of these villages want to make a Children Park at such place which is equidistant from these three villages. After fixing the place of Children Park, prove that the park is equalistant from the three villages.



rioles

Green.

P. Q. R times villages are non-coffinear

Required:

To locate a point for a purk equidistant from

these villages.

Construction. (i) Jon Q to P and R.

- (ii) Take AT right bisector of PQ.
- (iii) Take BL right bisector of QR
 AT and BU intersect at point O.

Bendi:

O is the required place

	Proof:	
	-	Reasons
	OQ ∓ OR (ii)	Point O is on the right bisector of AQ Point O is on the right bisector of QR
Jan.	OP = OQ ⇒ OR Hence O is equidistant from P, Q and R.	From (i) + (ii)

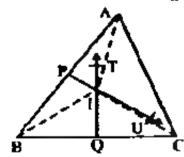
Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>ranshahzadiftikhar@qmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 12)

Pilot Superone Mathematics 466 Class 9th

Theorem

The right bisectors of the sides of a triangle are concurrent.



Given:

In AABC

PU, QT are right bisectors of AB and BC

 \overrightarrow{PU} and \overrightarrow{QT} intersect at L

Required:

Point / fies on the right bisector of AC

Le. K'≅ IA

Proof:

Sentements	Reasons
Bl≆Čl (i)	Point / is on the right bisector of BC
BI = AI (ii) CI = IA Hence Point / lies on the right beacter of AC Therefore three ngit bisectors of sides of a triangle are concurrent.	Point I is on the right bisector of AB From (i) and (ii)





Pilot Superone Mathematics 467 Theorem Any point on the bisector of an angle is equidistant from its arms. Given: (1) ∠ABC is an angle. BM is bisector of ZABC (11) (m) PQ LBC PR L BA (iv) To prove: PO ± PR Proof-Reasons BP = BF Common Gryen ∠l ⊋ ∠2 ZPRB ≅ ZPOB Each 90* $\Delta PBR = \Delta POB$

S.A.A. ≅ S.A.A.

congruent triangles.

sides

of

Corresponding

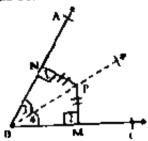
PR ≅ PO

Pilot Superone Mathematics 468

Class 9"

Converse Theorem

Any point inside an angle, equidistant from the arms, is on the bisector of it.



Given: (1) A point P lies inside of angle ∠ABC.

- (ii) PM LBC, PN LBA
- (iii) PM ≈ PN

Required: Point P is on the bisector of ∠ABC

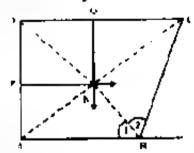
Construction: Join B to P and produce.

Proof:	
Statements	Reasons
In ∆PMB ← → APNB	•
BP≅BP	Common
∠1 # 42	hach 90° (given)
PM ≅ PN	Given
APMB = APNB	H.S. ≅ H.S
Thus ∠3 ≅ ∠4 Hence BP is bisector of	Corresponding sides of congruent triangles
ABC and point Piles on it.	

Pilot Superone Mathematics 469 Class 9th

EXERCISE 12.2

Q.I In a quadrilateral ABCD, AB a BC and the right bisector of AD, CD meet each other at point N. Prove that BN is bisector of \(\angle ABC. \)



- Given. (1) ABCD is a quadrilateral
 - (ii) AB ≈ BC
 - (III) PN is right bisector of AB
 - (iv) QN is right bisector of CD

 PN and QN intersect each other at N
 - (v) Nasjoined to N

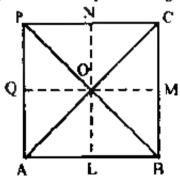
Required: BN is bisector of angle ZABC

Const- | ic ∠1 ± ∠2 | Const- | Join N to A, D, C

Proof:	
Statement	Reasons
NA'S (1)	N hes on right bisector of AD
ND ≈ NC (H)	N beson right bisector of \overline{CD} From (i) and (ii)
In ANAB ← → ANCB NA ≥ NC AB ≅ AC BN ≅ BN ANAB ≈ ANCB So ∠1 ≈ ∠2	Proved Given Common S S.S ≅ S S S
Hence BNI is besector of ∠ABC	<u> </u>

Pilot Superone Mathematics 470 Class 9*

Q.2 The bisector of $\angle A$, $\angle B$ and $\angle C$ of a quadrilateral ABCP meet each other at point O. Prove that the bisector of $\angle P$ unit also pass through the point O.



- Given: (i) ABCP is a quadrilateral
 - (ii) Bisectors of ∠A, ∠B and ∠C meet at point O

Required: Point Olies on the bisector of ZP

Construction: (I) Join O to P

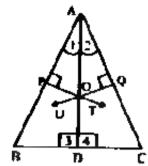
(ii) Draw $\overline{OL} \perp \overline{AB}$, $\overline{OM} \perp \overline{BC}$ and $\overline{ON} \perp \overline{PC}$ also $\overline{OQ} \perp \overline{AP}$

Proof:	4	<u> </u>
Statements	**************************************	Reasons
1 <u>0</u> ±1 00	(i)	Point O is on the bisector of ∠A
1 OL ≅OM	(ii)	Point O is on the bisector of $\angle B$
1 OM ± ON	(iú)	Point O is on the bisector of ∠C
T <u>oo</u> ≅T on		From (i), (ii) and (iii)
Thus Point O lies	on the	
besector of ∠P		
Therefore OP is bisected	or of ∠P	

Pilot Superone Mathematics 471

Class 9^a

Q.3 Prove that the right hisector of congruent sides of an isosceles triangle and its altitude are congruent.



Given:

In AABC

- (i) ĀB≅ĀC
- (ii) PT is right bisector of AB
- (mi) QU is right bisector of AC

PT and QU intersect each other at O

Required:

Point O lies on the altitude of AABC

Construction: Join A to O and produce it. It cuts BC at D.

Proof:

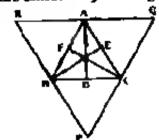
Sintracing	Reasons	
mAB =mAC	Given	
$\frac{1}{2} = \overline{AB} = \frac{1}{2} \times \overline{AC}$	Dividing by 2	;
. TAP ≡ AQ		:
In ∆APO ←→ AQO]	•
L ĀP≅AQ	proved -	
ĀŌ ≈ ĀŌ	common	:
∠APO ∈ ∠AQO	each 90"	ď
ΔΑΡΟ = ΔΑQΟ	H.S. ≆ H.S.	

Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>raoshahzadif@khar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 12)

Prior Superone Mathematics	472 <u>Cass 9</u>
Thus ∠i ≅ ∠2	
Now in ∆BAD ← → ∆CAD	
AB≅AC	Green
∠1 ≡ ∠2	Proved
ĀD̄ ₹ ĀD̄	Common
ΔBAD ≅ ΔCAD	S.A.S. ≅ S.A.S.
(i) ∠3 ∉ ∠4	Corresponding angles
	Congruent &
(ii) m∠3 +m∠4 = 180*	Adj supp. angles
Thus $m\angle 3 - m\angle 4 = 90^\circ$	1
Therefore $A\widetilde{D} \perp A\widetilde{B}$	
Point O hes on altitude AD	<u> </u>

Q.4 Prove that the altitudes of a triangle are concurrent.



Given. In AABC

 \overrightarrow{AD} , \overrightarrow{BE} , \overrightarrow{CF} are its altitudes.

is, AD L BC, BELAC, CF LAB

Required: AD, BF and CF are concurrent.

Construction: Passing through A, B, C take RQ | DC,

RP | AC and QP | AB respectively

Forming a triangle PQR

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MATHEMATICS FOR 9TH CLASS (UNIT # 12)

	Proof.		
	Statements	Жумницы	
	BC∏ <mark>P</mark> Q	Construction	1
	ABJ'QC	Construction	
	ABCQ is a !]	-	
	Hence AQ ≈ BC		
	Similarly RA : BC		. (2) 31
	Hence point A is mid-point of RQ	چ ا	
	And AD ± BC	. 1	
1	BC (RQ		
	AD 1 RQ		
	Thus AD is right bisector of RQ	10.	
	Similarly BF is righ, bisecon	fight because of a	den of A
	of RP and CF is 12	Right bisector of si are con-current	oes of A
	bisector of PQ		
	Therefore _ 'AD , BE . CF		
	are right biseggor of sides of APOR		
	AD. BF and CF are		
	A dencurrent		
	XV		
•	V		
_N	•		
arin			
27			

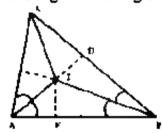
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Pilot Superone Mathematics 474

Class 9th

Theorem

The bisectors of the angle of a triangle are concurrent



Given:

I ΔABC bisectors of ∠B, ∠C meet at 1.

Required:

Bisector of ZA passes through I

Construction:

(i) Join A to I

(ii) Take If _ AB

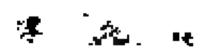
(III) ID 1 BC and .

(IV) IE ± AC

Proof:

Remons
I lies on bisector of angle
Elies on bisector of angle C.
From (i) and (ii)

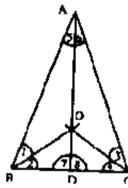


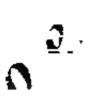


Pilot Superone Mathematics 475 Class 9

EXERCISE 12.3

Q.1 Prove that the bisectors of the angle of base of an isosceles triangle intersect each other on its altitude





Given:

in AABC

(i) AB = AC

Bisectors of ZB and ZC intersect at O

(ii) A is joined to O and produce that cuts \overrightarrow{BC} at D.

Required:

AD is altitude of AABC

ie. AD L BC

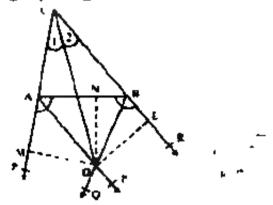
Proof:

	Reasons
ΔABC	
ĀB a ĀC	Given
∠ABC ≅ ∠ACB	Angles opposite to congruent
$m\angle ABC = \frac{1}{2} m\angle ACB$	IN FEE
∠l≘∠3	
	AB a AC ∠ABC a ∠ACB m∠ABC = 1/2 m∠ACB

Pilot Superone Mathematics 4	76 <u>Class 9</u>
Now in AOBC	Proved
∠1⊋∠3	Opp Sides of congruent angles
Now ∆AOC ←→ ∆AOB	Common Given
AO = AO AC = AB BO = CO	Proved 5.S.S. ≡ S.S. = 1
ΔAOC ≘ΔAOB 1 Thus ∠5 ≡ ∠6	Common 3
Now in AABD ← → AACD	Proved
AD = AD ∠5 = ∠6	Cuiven S.A.S. a.S.A.S.
ĀB ≅ĀC 入し	Corresponding angles of congruent triangles
ΔABD≆ΔACD (i) m∠7≆	Adj. supp. angles From (i) and (ii)
(ii) point m 27 + m 28 - 180°	
Thus re∠7 m∠\$ 90°	. 1,
And AD passes through point (

Pilot Superone Mathematics 477 Class 9th

Q.2 Prove that the bisectors of two exterior and third interior angle of triangle are concurrent.



Given:

In ΔAB€

ZABR and ZBAP are two exterior angles.

Their \widetilde{AP} and $B\overline{Q}$ bisectors intersect each other

at O. C is joined to O.

Required:

CO is bisector of angle $\angle C$ i.e. $\angle 1 = \angle 2$

Construction: Oi. LCR, ON LAB and OM LCP

Proof:

Prooj:		
	Statement	Reasons
	TOI \$1 W (I)	BO is bisector of ∠ABR
	TOM \$TON (II)	AO is bisector of ∠BAP
	±Õ Ĭ. ≆⊥ ÖN	From (i) and (ii)
Heres	CO is bisector of ∠C	•
i e	∠1 ≡ ∠2	1

Pilot Superone Mathematics 478 Class 9th

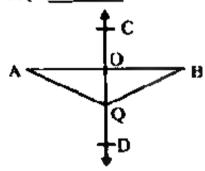
Review Exercise 12

- Q.1 Which of the following are true and which are false?
- (i) Bisection means to divide into two equal parts.
- (ii) Right bisection of line segment means to draw perpendicular which pesses through the mid-point.
- (iii) Any point on the right bisector of a line segment is not equidistant from its end points.
- (iv) Any point equidistant from the end points of a line segment is on the right bisector of it.
- (v) The right bisectors of the sides of a triangle are not
- (vi) The bisectors of the angles of a triangle are concurrent
- (vii) Any point on the bisector of an angle is not equidistant from its arms.
- (viii) Any point raside an angle, equidistant from its arms, is on the bisector

Agravet

	7774	ME/1			_				
1	0	T	(ti)	T	(HI)	F	(14)	Τ]	
	3	F	(vi)	T	(44)	F	(vili)	T	

Q.2 If CD's Held bisector of line segment AB, then



Pifor Superone Mathematics 479 Class 9th

Answers-

mOA · mOB

mAQ - mBQ

Q.3 Define the following:

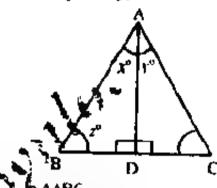
(i) Bisector of a line segment

(ii) Bisector of an angle

Answers: (i) A line is called the bisector of a line segment if it passes through its mid-point.

 f a ray divides an angle into two congruent angles then that ray is called bisector of that angle.

Q.4 The given triangle ABC is equilateral triangle and AD is bisector of angle A, then find the values of unknowns x*, y* and z*.



Given A h AABO

AB ≈ BC ≈ CA

i.e. ∠B ≘ ∠C ∉∠BAC each = 60*

 \overrightarrow{AD} is bisector of $\angle A$ i.e. $x^0 = y^0$

Required: To find x^a, y^a and z^a

z° - 60

given

AD is bisector of ∠A

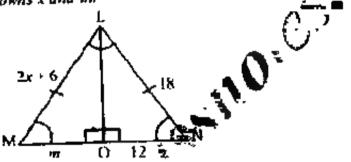
Pilot Superone Mathematics 480 Class 9th

Now

$$\frac{1}{2} \, \text{m} \angle A = x^0 = y^0 = \frac{60}{2}$$

$$x^o = y^o = 30^\circ$$

Q.5 In the given congruent triangles LMO and LNO, find the unknowns x and m.



Solution:

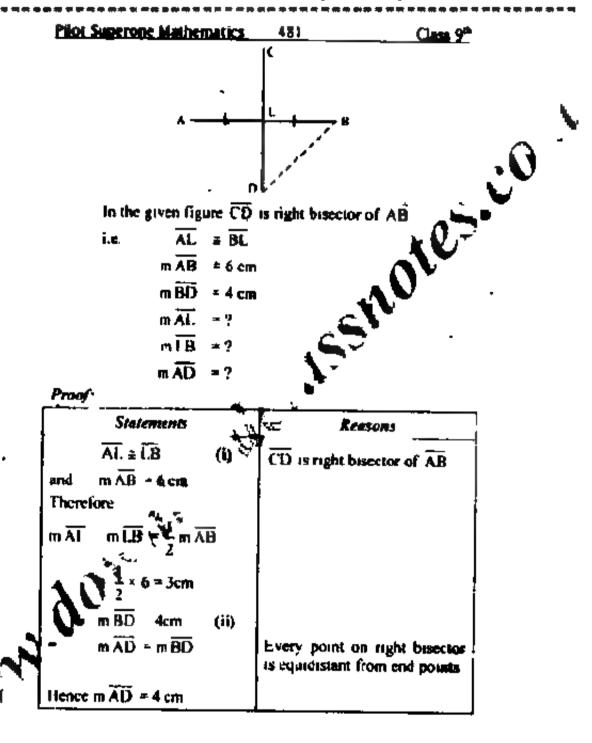
$$x = \frac{12}{2} = 6$$

Q.6 CD is right bisector of the line segment AB.

mīB.

if
$$m \overline{BD} = 4$$
 cm, then find $m \Delta D$.





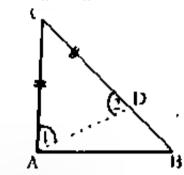
Class 9th Pilot Superone Mathematics 482



SIDES AND ANGLES OF A TRIANGUE

Theorem

If two sides of a triangle are unequal in length, the longer side has an angle of greater measure opposite to it.



· AVEN:

In AABC

 $mBC \ge mAC$

To prove:

 $m\angle A \ge m\angle B$

Construction: Form CB cut CD & CA Join D to A

*	Ŀ
	•

Proof		
	Statement	Reasons
[In AACD	
	m∠1 ~ m∠2 (i)	Angles opposite to congruent sides
	In AABD	
	m∠2 > m∠B (ii)	∠2 in exterior and ∠B is interior
	m∠1 > m∠B (iii)	By (i) and (ii)
Now	m∠A=m∠!+	Addition of angles (postulate)
m∠B.	AD	Drugith and the
ľ	m∠A>m∠. (iv)	By (iii) and (iv) Transitive property of
} .	$m\angle A \ge m\angle 1 \ge m\angle B$	nequality of numbers
or	m∠A>m∠B	residentity of itemports



Phot Superone Mathematics 483

Converse of Theorem

If two angles of a triangle are unequal in measure, the side opposite to the greater angle is longer than the side opposite to the smaller angle.



Given:

In AABC

m∠A ≯ m∠B

Required

 $m \overline{BC} > m \overline{AC}$

Statements	Leasons
If mBC > mAC Then (i) mBC = mAC	Trickotomy property of numbers.
or (ii) $m \overline{BC} \le m \overline{AC}$ For first condition if $m \overline{BC} = m AC$ Then $m \angle A = m \angle B$ Which is not possible For recondition condition	Opposite to given
if mBC < mAC Then m∠A < m∠B Thus is also not possible	Contrary to given
Now maBC ≠ m AC And mBC ≰ m AC Hance mBC > m AC	Trichotomy property of numbers.

Class 9° Pilot Superone Mathematics There say The sum of the lengths of any two sides of a triangle is greater than the length of the third side **AABC** Given: mAB+mAC > mBC **(I)** To Prove: mAB+mBC>mAC (ii) mBC + mCA > mABtiin. Construction: Take a point D on \overrightarrow{CA} such that $\overrightarrow{AD} \ni \overrightarrow{AB}$ Join B to D and name the angles. \$\angle 1\$, \$\alpha 2\$ is shown in the given figure. m &ABD AD = AB construction (i) ∠1 = *∠*2 $m\angle DBC = m\angle 1 + m\angle ABC$ mZl m∠DBC From (i) and (ii) (B) $m \angle 2$ m∠DBC Given (iri) AABD ←─→ AECD Vertical angles CIMEDWOOD BD≅CD S.A.S. Postulate Corresponding sides of $\triangleq \Delta^s$ ∠1 ≅ ∠2 AD = ED ACF is a triangle AABD - AECD Form I and II (1) $m\overline{AE} = 2m\overline{AD}$ (construction) AB ≅ EC mAC+mEC>mAE (11) +mAB>mAE

Mini

tence mAC + mAB > 2mAD

Pilot Superone Mathematics 485

Class 9°

EXERCISE 13.1

Q.1 Two sides of a triangle measure 10cm and 15cm. Which of the following measure is possible for the third side.

(a) 5 cm (b) 20 cm (c) 25 cm (d) 30cm

Solution:

Length of one side = 10 cm

Length of second side = 15 cm

Sum of length of two sides = 10 + 15 = 25 cm

- (a) 5 < 25
- (b) 20 < 25
- (c) 25 = 25
- (d) 30 > 25

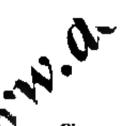
Sum of lengths of two sides is always greater than the third tide of a triangle.

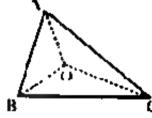
Therefore c, d are not possible.

a and b are possible.

Q.2 0 is an interior point of the AABC. Show that

$$m\overline{OA} + m\overline{OB} + m\overline{OC} > \frac{1}{2}(m\overline{AB} + m\overline{BC} + m\overline{CA})$$





Given:

Point O is an the interior of AABC

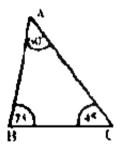
Required:

 $m\overline{OA} + m\overline{OB} + m\overline{OC} > \frac{1}{2}(m\overline{AB} + m\overline{BC} + m\overline{CA})$

Proof.	uperone Mathematics	
	Statements	Reasons
(i)	In ∆OAC mOĀ+mŌČ>mĀC	Sum of lengths of two sides is in greater than the length of the third side
(ii)	In AOAB mOA + mOB > mAB In BOCA	Sum of lengths of two sides is in greater than the length of the third side.
(ni)	,m (0B + m 0C > m BC	Sum of lengths of two sides is in greater than the length of
2m0	A + 2m OB + 2m OC >	Adding (i), (ii), (iii)
2(mi	m ĀB + m BC + mÆ ŌĀ + m ŌB + m ŌC> m ĀB + m ŌC + m C ∧	7
m O	Ā+mŌB+mŌC>	Dividing by 2
ه. در	ImAS+mBC+mCA	

Pilot Superone Mathematics 487

in the AABC m AB = 70° and m CC = 45° which of the 0.3 sides of the triangle is longest and which is the shortest?



Solution:

Given.

to AABC

AB is the shortest

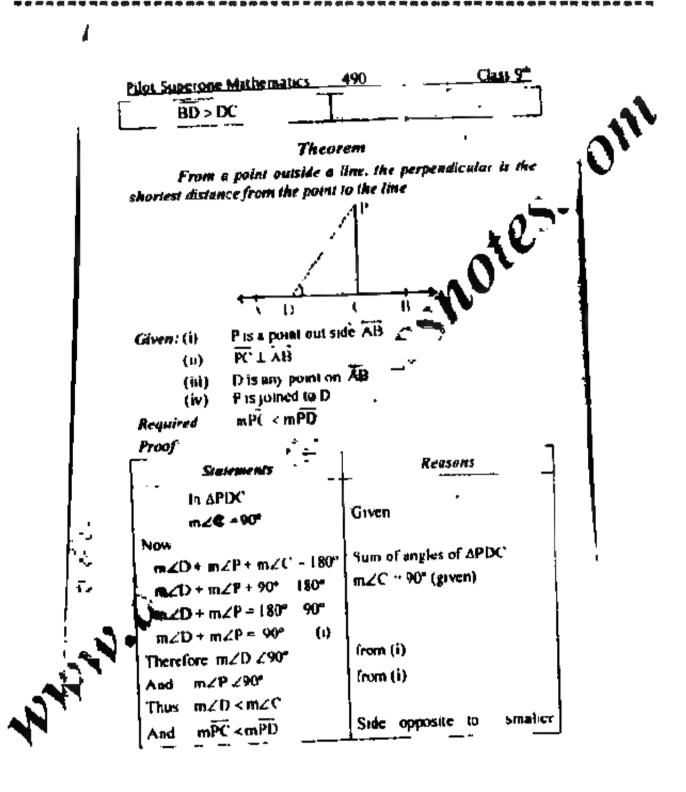
$$m\angle B = 70^{\circ}, m\angle C = 45^{\circ}$$

Required: (i) Which is longest from among AB, BC, CA

(ii) Which is shortest from among AB. BC. CA

(m) without the delocation	DON HOW GIVENE AD: DC , CA
Proof:	
Statements	Reasons
in △ABC m∠A + m∠B + m∠C = 180° m∠A + 75° + 45° = 180° m∠A + 120° = 180° m∠A = 180° 120° Helpel m∠A = 60° m∠A = 60°	Sum of angles of ∆ m∠B = 75*, m∠C = 45° given
m \angle B = 75° m \angle C > 45° \overline{AC} is the iongest \overline{AB} is the shortest	Opposite to the greatest angle Opposite to the smallest angle





Written/Composed by - <u>SHAHZAD IFTIKHAR</u> Contact # 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>ranshahzadiftikhar@qmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 12)

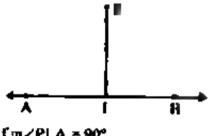
	Pilot Supergne Mathematics Hence all d stance from P to	49 l angle	<u>Class 9*</u> ;
	AB will greater than PC		
ı		<u> </u>	
		1.1	00
		-	012
- }		<u>م</u>	1 00
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Pile	ot Superone Mathematics	#92 Class 9*	
	EXERC	ISE 13.2	
Q	I In the flower P is one i	point and AB is a line. Which skortest distance between th	and the
	point P and the time AD		
			٦
	(a) mPL (b	·	
c.	(c) mPN (4	nest distance from P to AB	
	olution: mPN is the shot roof: Statements	Reasons	
In		rn∠N > 90* m∠O = 70*	
in	1 APMO mPM(>mFO (li)	smaller angle has small sw opposite to m2O > 70°, m2M = 60°	ic
lr.		m∠1 = 30° m∠O = 70°	
.4	<i>•</i>	small angle has smaller so opposite to it.	de .
Sal.	lence mPN < mPO mPM > mPO mPt, > mPO		Ì
_ '	mrs, > mro Therefore mPN is the	;	ĺ
	mailest of all PO.PM.PI		<u> </u>

Pilot Superone Mathematics 493 Class 9°

- 0.2 In the figure. P is any point lying away from the line AB. Then mPl. will be the shortest distance if
 - m CPLA
- (6) mZPL8 100°
- mZPLA (c) 90°

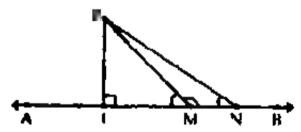


Answer

 $|fm\angle P|_A = 90^\circ$

The perpendicular distance from a point out-side Reason. the line is the shortest distance from that point to the given line.

In the figure. PL is perpendicular to the line AB and Q.3 mLN > mLM . Prove that mPN > mPM .



Given:

In the given figure

- PT 1 AB **(i)**
- $m\overline{LN} > m\overline{LM}$ (ir)

 $m\overline{PN} > mPM$



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MATHEMATICS FOR 9TH CLASS (UNIT # 12)

700	· - ;	Reasons
	Statements	Reasons .
n	ΔΡΙ.Μ	•
	m∠PI M = 90°	Given
	m∠P! M < 90° (i)	in a right angle thangle other two angles an active.
n∠Pl iı)	LM + m∠PMN =180°	Adj. Supp Angles
iii)	m∠PMN>90°]
n	API.N	Given
	m∠l = 90°	
iv)	m∠PNL ∠90°	
	mZPMN>mZPNM	
n	ΔPMN	Provided
	m∠PMN > m∠PNM	11,000
	mPN > mPM	S
•	1000	
		I
	AN T	
•	6 7.	
۸	ONINO	

Pilot Superone Mathematics 495 Class 9th

Review Exercise 13

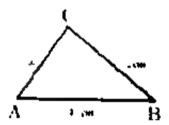
- Q.1 Which of the following are true and which are false?
- The angle opposite to the longer side is greater
- (ii) In a right-arigled triangle greater angle is of 60°
- (iii) In an isosceles right-angled triangle, angles other than right angle are each of 45°
- (IV) A triangle having two congruent sides is called equilateral triangle.
- A perpendicular from a point to line is shortest distance.
- (VI) Perpendicular to line form an angle of 90°
- (vii) A point out side the fine is collinear
- (viii) Sum of two sides of triangle is greater than the third
- (ix) The distance between a line and a point on it is zero.
- (x) Triangle can be formed of lengths 2 cm, 3 cm and 5 cm.

 Answers.

Q.2 What will be ungle for shortest distance from an outside point to the line?

Answers: 90°

Q.3 If 13 cm, 12 cm and 5 cm are the length of a triangle, then varify that difference of measures of any two sides of a triangle is less than the measure of the third

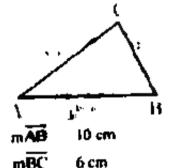


| Pilot Superone Mathematics | 496 | Class 9th | I.et | mAB | 13 cm | mBC | = 12 cm | mCA | = 5 cm |

Now
$$\overline{MAB}$$
 $\overline{MBC} = 13-12 = 1$ cm $<\overline{CA}$ (m \overline{CA} = Scm)
 $\overline{MBC} = \overline{MCA}$ 12 5 = 7cm $<\overline{AB}$ (m \overline{AB} = 13cm)
 \overline{MAB} $\overline{MCA} = 13 - 5 = 8$ cm $<\overline{BC}$ (m \overline{BC} = 12cm)

It show that difference of measure of any two sides of a triangle is less than the measure of the third side.

Q.4 If 10 cm, 6 cm and 8 cm are the lengths of a triangle, then verify that sum of measures of two sides of a triangle is greater than the third side.



Let

mCA 8 cm

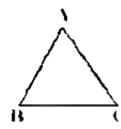
Now mAB + mBC = 10 + 6 + 16cm >mCA (mCA +8cm) mBC + mCA = 6 + 8 = 14cm AB (mAB = 10cm)

This ventiles that sum of length of any two sides of a triangle is greater than the length of the third side

rara.

Palot Superone Mathematics 497 Class 9*

Q.5 3 cm, 4 cm and 7 cm are not the lengths of the triangle. Give the reason.



Let mAB 7 cm

mBC 4 cm mCA 3 cm

Now (i) m \B + mBC 7+4 H mC\(mCA = 3cm)

titl mBC + art A = 4+3 7 m SB(m AB × 7cm)

(mi) mCA + mAB + 3 + 7 | 10 | BC (m BC | 4cm) Part (ii) as not possible

Therefore 7 cm, 4 cm, 3 cm are not the sides of a triangle

Q.6. If 3 cm and 4 cm are lengths of two sides of a right triangle then what should be the third length of the triangle.

Solution -



Let length o hypotenuse it em

v 25

x √25 (taking sq. root)

r 5 cm

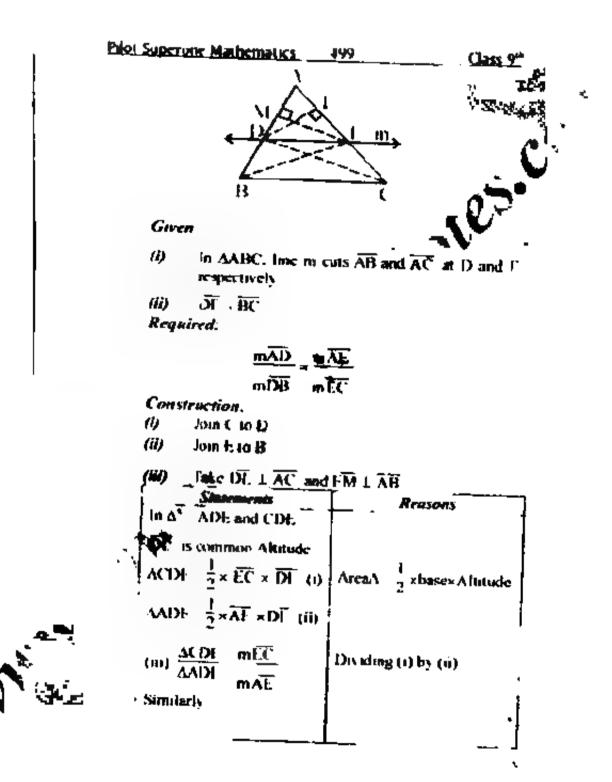
I ength of hypotenuse 5 cm

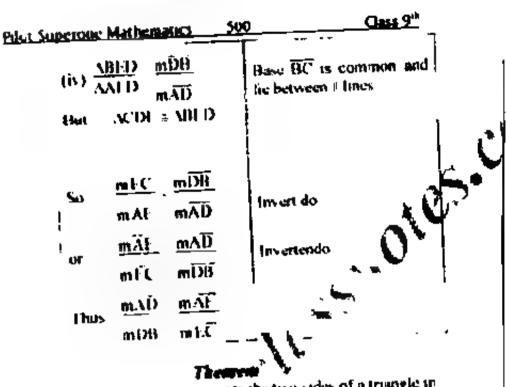
A TOTAL CHANGE

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MATHEMATICS FOR 9TH CLASS (UNIT # 14)

Class 9 Prior Superone Mat sematics: 148 Unit RATIO AND PROPORTIONAL Similar Triangles. Two triangles AABC and ADLI are similar if In MARC (4) MILL /A * /D (i) /B = /1 ZC 2 Z1 mAB (iii) and m£F. mDH Symbolically we write it as AABC - ADLE Remember: Two congreent triangles are similar Two similar triangles may not be congruent Theorem A line parallel to one side of a triangle and intersecting the other two sides divides them proportionally.





If a line segment intersects the two sides of a triangle in the same ratio then it is parallel to the third side



Given:

In VABC, a line segment cuts \overline{AB} at D and \overline{AC} at L.

that mDB mFC

Required:

Phot Superone Mathematics 501 Class 9th DF a BC Construction: Suppose $\overline{DE} + \overline{BC}$, then take $\overline{CP} \ \ \overline{DE}$ that meets AB produced at P Proof: MAPC In Construction DF CP Therefore mAD mAE mAD mAE But mAD mAD From (1) and (11) m**DB** mDP Property of real numbers m DB m DP Therefore Pilies on P. Hence our supposition is WHOME Hence DE BC

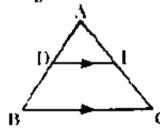
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Pilot Superone Mathematics 502

Class 9 1

Exercise 14.1

Q.1. In AABC, DE RBC



In AABC, DL BC

- (i) If AD > 1.5 cm, BD → 3 cm, AE = 1.3 cm, then find (F)
- (ii) If AD 2.4 cm, AE 3.2 cm, EC (iii) cm. find AB
- (iii) If $\frac{AD^2}{DB} = \frac{3}{5}$ cm AC 4.11, find $\frac{AE}{AE}$
- (iv) If A1) $2.4 \text{ cm.} \overline{AF} = 3.2 \text{ cm.} DE = 2 \text{ cm.} \overline{BC} = 5$
- cm, find AB, \(\bar{D}B\), \(\bar{AC}\), \(\bar{CE}\)
 (v) If AD 4x 3. Al = 8x 7. BD 3x 1 and CE 5x \$\frac{1}{2}\$, find the value of x

Solutions:

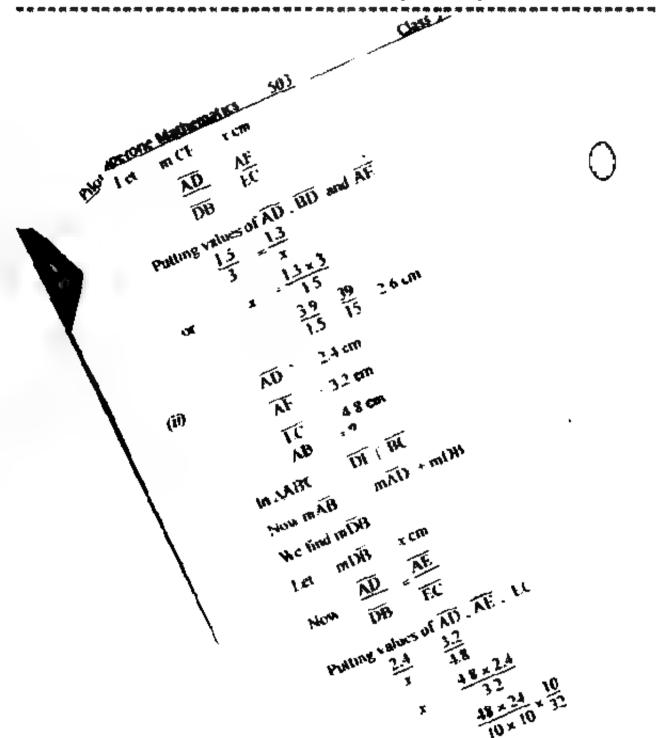
In AABC, DE | BC

IN VARC DE II BC



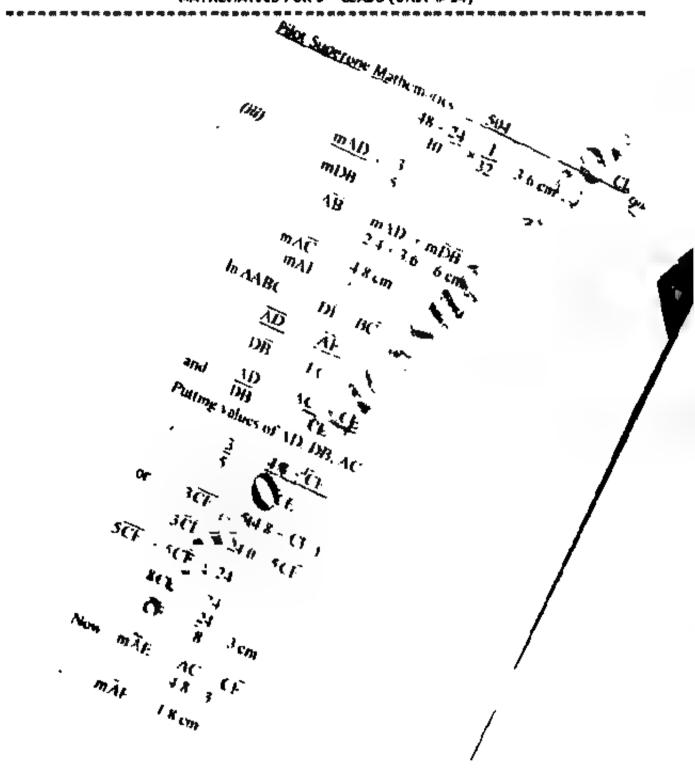
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MATHEMATICS FOR 9TH CLASS (UNIT # 14)



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MATHEMATICS FOR 9TH CLASS (UNIT # 14)



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Prior Supe	rone Math	ematics	505		Class 9 ^b
(tv)	4D	- 2.4 cm		W	
	ÄF	= 3.2 cm		(W	
	JE	= 2 cm		(iii)	
	₿Ĉ	= 5 cm			
	₹B	?, DB	2. AC	", CE	?
		B P5	<u>, </u>		

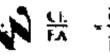
Construction:

Take Now TP ∉ AB DEPB is 7*

 $m\overline{PB} \geq m\overline{DF} \geq 2$ cm

Thus maCP = 5 2 3 cm

NOW UT AABC EP LAB



Putting values of EA, CP, PB

$$\frac{CE}{3.2} = \frac{3}{2}$$

$$\overline{CE} = \frac{3 \times 3.2}{2}$$

CF 3×16 48cm (h

NOW SE VABO DE EBO

		_				` `
Pilot	Superone Mai	hematics	506		Class 9 th	
	<u> 1915</u>	CE				
		<u>CE</u>				
	Ϋ́D					
	<u>BD</u>	4.8 3.2				
	(Putting the	values of A		ίĒ)		
	BD	2 4 × 4 3.2	<u>.\$</u>	(v)		-
	O.D			1-2	. ,	,
		- 36 cm				٠
	Now A	B ⊤AD +	ÕΒ		a	
		24+3		(I), (r)	V	
		6.0 cm				
	Hence Di	3 - 3 B cm		(7)		
	ĀČ					
	A.C.	- 3.2 + 4		n <i>(ii), (iv)</i>		
		8 D cm		• • • •		
	· Œ	- 4 B. cm	Fron	n (iv)		
1(v)	C 1.	* 4. ***	****	(*-)		
2007			\			
	7		\			
		V 19/	 ZI			
		/ /				
		[š	,			
•	0 4	= 4r 3				
`	Ai	= &r 7				
_ \	BI					
· 72 •	C	F = 5x + 3				
Visib.	1	= 7				
4	Now in AA	BC DE E	K'			
7.	<u>AI</u> BI	AE"				
•	BE	CF				

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Pilot Superone Mathematics Class 9" Putting values Now (4x/3)(5x/3) = (8x/7)(3x/1) $20x/27x + 9 = 24x^2 - 29x + 7$ $20r \quad 24r^2 \quad 27r + 29r + 9 \quad 7$ Of $4x^2 + 2x + 2 = 0$ Dividing by 2 21 1 OΓ $2x^2 2x + x + 1$ 2x(x-1)+1(x-1)=0(x-f)(2x+1)2x+1=02r (impossible)

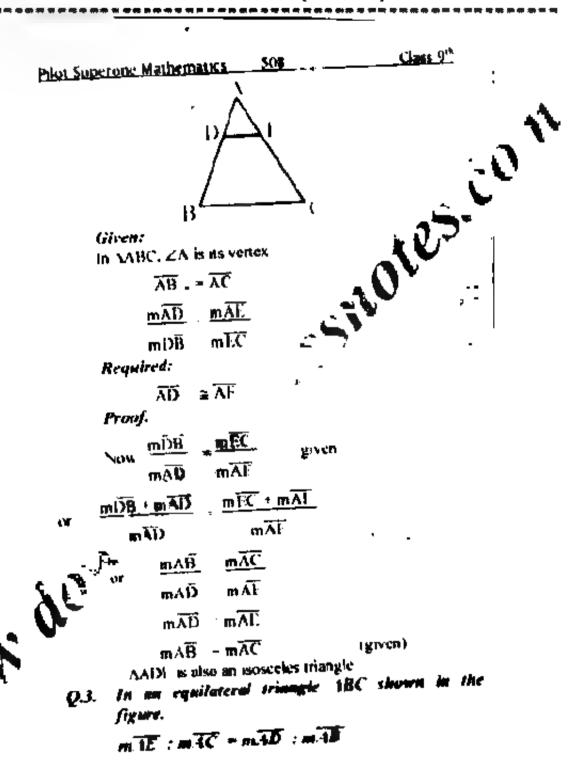
Q.2. If $\triangle ABC$ is an isosceles triangle, $\angle A$ is vertex

angle and \overline{DE} intersects the sides \overline{AB} and \overline{AC} as shown in the figure so that

mAD in \overline{DB} mAF mFC

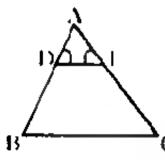
prove that \(\DADE \) is also an isosceles than gle





Pilot Superone Mathematics \$199 Qass 9

Find all the three angles of AADL and name it



Given:

ABC is an equilateral triangle i.e. AB = BC = AC also

m
$$\angle A$$
 m $\angle B$ m $\angle c$ 60° and $\frac{m\overline{AL}}{m\overline{AC}} = \frac{m\overline{AD}}{m\overline{AB}}$

Required.

to find measures of angles of AADI Solution:



DI SBC

mz Ns mZB mZC 60% (Crven

 Corresponding angles DF ŔĊ Corresponding angles 1 Corresponding angles

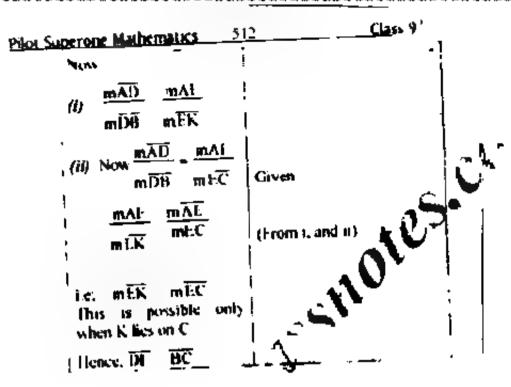
is an asosceles Given

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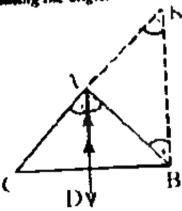
MATHEMATICS FOR 9Th CLASS (UNIT # 14)

<u>Pilor S</u>	uperone Machematics	510	Class 9th
Q.4.	Prove that the line side mid-point of one side another side bisects the	of a triangle an	
	Given: In AABC	,,\	,
	mAĎ mĎB DE vB Required. mAE Proof:	*	
	Statements in AABC	Rec	g50H5 .
,	E DE BC	Given	,
90	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Theorem	!
. 3.	Now mAD -mDB	Given	!
William.	mDB mFC	Putting in Al	D mDŘ m (i)

Pilos Saperone Mathematics or $m\overline{A}\overline{\Gamma} = m\overline{E}\overline{C}$ Hence, DF bisects AC Prove that the line segment joining the mid-points of any two sides of a triangle is parallel to the third side. Given: In AABC mAD - mDA mAE = mEC mAD mAb mĎĐi mĒČ Required. Dt BC Reasons If Def 米 BC then take produced AC at k



The internal bisector of an angle of a triangle divides the side apposite to it in the ratio of the length of the sides containing the angle.



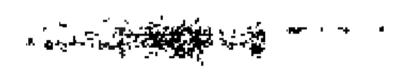
Given:

III AABC internal bisector of ZA meets CB at D

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MATHEMATICS FOR 9TH CLASS (UNIT # 14)

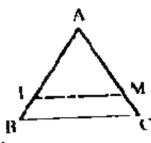
Mot Superone Mathematics 51	Gass 9
To prove-	
mAC mCD mAB mBD Construction:	
Draw BK // DA which meets	CA produced at K
Shrencuty	Regrees
AD \\BK and CK cas them m21 = m22	
$\overrightarrow{AD} \parallel \overrightarrow{KB} \text{ and } \overrightarrow{AB} \text{ cuts them}$ $m \ge 3$ $m \ge 4$	
But mZ! mZ3	Alternate angles
m∠2 ≈m∠4	Given
•	4 Th
and $AB \cong \overline{AK} \text{ or } AK \cong \overline{AB}$!
Now AD I KI	Construction
m DC mKĀ m DC mĀC	Theorem
meD mAC	
or mAB mBD	Proved



_Class 9** Pilot Superone Mathematics 514

Theorem

If two triangles are similar, then the measures of their corresponding sides are proportional.



Given:

ADEF AABC

notes i.e. $\angle A \equiv \angle D$, $\angle B \cong \angle F$ and $\angle C \equiv \angle F$ To Prove.

Construction:

- Suppose that $m A \overline{B} > m \overline{DE}$ u
- mAB smDE a

On \overline{AB} take a point L such that $\overline{mAL} = \overline{mDE}$

On \overline{AC} take a point M such that $\overline{mAM} = m\overline{DF}$ Join L. and M by the line segment LM.

arara	'n.
W.	

Remons
Given
Construction
Construction
S.A.S. postulate Corresponding angles

Pilot Superone Mathematics 515	. <u>Class 9*</u>
$\angle M \cong \angle F$ and $\angle I \cong \angle F$, $\angle M \cong \angle F$ Now $\angle E \in \angle B$ and $\angle F \cong \angle C$ $\angle L \cong \angle B$, $\angle M \cong \angle C$	of congruent A' (Corresponding angles) of congruent triangles) (Given Transtituty of congruence
Hence, mAL mDF mAB mAC or mDE mAC mAB mAC	Corresponding angles are equal by Theorem 14.1.1
	mAM mDF (Construction)
Thus mDE mDE mFF mAB mAC mBC mAB mAC mBC	by (r) and (n)
mDF mDF mFF (II) If mAB < mDL, it can similarly be proved by taking intercepts on the sides of ADFF If mAB mDE, then	by taking reciprocals

- 14.5

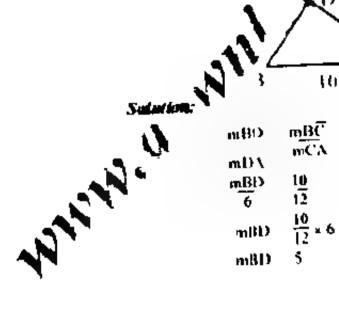
Pilot Superone Mathematics 516		Class 9"	
in ₹/BC ← → \DEF 2 \ \ \ D \ B = F	(iven Given		-
and AB * DE Su VABC \DEF (hus	` A S.A ≅ A	\S.A	<u> </u>
mAB mAt mBC mDF mDF mDF mEF Hence the result is true for all the cases	•	, BC ≡EF	6*

Exercise 14.2

Q.1. In ALBC as shown in the figure, CD bisects 2C

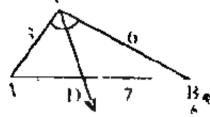
and meets
$$\overline{AB}$$
 at D : $m\overline{BD}$ is equal to

(a) 5 ,b) 16 ,c1 (0) (d) 18



Ottin	mBC
mDA	mCA
mBD	10
6	12
mBD	$\frac{10}{12} \times 6$
mBD	5

Pilot Superone Mathematics 517 Class 9 Q.2. AABC shown in the figure. CD bivects 20. If $m\overline{AC} = 3$, $m\overline{CB} = 6$ and $m\overline{AB} = 7$, then find $m\overline{AD}$ and $m\overline{DB}$



Solution:

Jet mAD a

mBD 7 x

mAD mAC mCB

Potting values

$$\frac{x}{2}$$
 6

or $\frac{1}{2}$
 $2(x) = 1(7 - x)$
 $2x + x + 7$
 $3x = 7$

or mAD 3

and mDB 7 x

 -7

ા <u>ત્રી</u> ન્યું ડ્	uperone Mathematics 5 18 m DB 3 3	Class 9"	A
		s de la la companya de la companya d	1,
Q.3.	Show that in any correspond if two angles of one triang corresponding angles of triangles are similar.	de are congruent to me	
	i)	.1	
	\	\ 	J*
		\ A U	1
		, <u>, , , , , , , , , , , , , , , , , , </u>	
	<u> </u>		ı
	- T	A Party W	
	Given. AABC and ADEF		
	m/B m/t	/A-	
	mZC mzt	J [™]	
	Required:		
	AABC ADEE		
	Proof		
	Statisticals	Reasons_	
	m/HentaCint/A 180"	Angles of AABC	
	m∠F · m∠L · m∠D 180"	Angles of Alzer	
		As m/1 m/B, m/F	
	∕ TN	mZC	
0	mzx mzD 0	Subtracting (ii) from (i)	
_ \	or m/A m/D		
₩	Now HI & ARC, DEL		
N.	mz A mz D mz B mz't		
. 1	յ տությունը ա.ե.ա.ե		
	MILL DIE		

Hence AABC - ADI F

Given: AB and CD intersect at X that mXB mXD AAXC and ABXD are similar. AB and CD intersect at X that mXB mXD Required: AAXC - ABXD Proof: In BXD and AXC A Lib 22 mAX mXB mXB AC (1 BD) AC (1 BD) AC (1 BD) AC (2 ZS) Thus MAX mCX mAX mCX Then show that mCX mXB mXD Proof: Research Research Corresponding angles	Pri <u>ut</u>	Superone Mathematics	519	Class 9°
Given: AB and CD intersect at X shall mAX mCX mXB mXD Required: AAXC - ABXD Proof: In BXD and AXC A Lib 22 mAX mCX mXB mXD AC N BD L4= 23 L6= 25 Then show that mXD Required: COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles COTTESPORTING angles MAX mCX mAC m XB mXD MAX mCX mXD MAX mXD MAX mCX mXD MA			and CD are inte	
Given: AB and CD intersect at X that reAX mCX mXB mXD Required: AAXC - ABXD Proof: B XD and AXC A A L L L 2 mAX mCX mXB mXD AC II BD AC		point X and $\frac{m\overline{AX}}{m\overline{XB}}$	$m\overline{CX}_{\perp}$. Then	show that
AB and CD intersect at X that mXB mXD Required: AAXC - ABXD Proof: In BXD and AXC A. 21th 22 Vertical opp. Angles Given AC (\(\text{BD} \) 24\(\text{2} \) 26\(\text{2} \) Thus mXB mXD MAX mCX mAC mXB mXB mIB thence sA x C - AB x D		C WEY		7,
Required: AAXC - ABXD Proof: M RAX mCX MXB mXD Vertical opp. Angles Given AC BD AC BD AC BD Corresponding angles (orresponding angles Thus MAX mCX mAC m XB mXD MAX mCX mAC m XB mXD MAX mCX mAC Thus MAX mCX mCX mAC Thus MAX mCX mCX mCX mAC Thus MAX mCX mCX mCX mAC Thus MAX mCX mCX mCX mCX mCX mCX mCX mCX mCX mC		Given:	B - 3,	•
In BXD and AXC A 21a 22 WAX mCX WXB mXD AC WBD 24a 23 24a 25 Thus MAX mCX mAC mAX mCX mAC mAX mCX mAC m XB mXS mIXB tence AA x C - AB x D		Required: AAXC - ABXD	Y 2021	
Vertical opp. Angles Given AC \(\text{\max}\) BD AC \(\text{\max}\) BD ∠4≈ ∠3 ∠6≈ ∠5 Bhus mAX mCX mAC m \(\text{\max}\) m \(\text{\max}\) MAX mCX mAC m \(\text{\max}\) m \(\text{\max}\) m \(\text{\max}\) Vertical opp. Angles Given Corresponding angles Corresponding angles Corresponding angles		Synonych	Reese	RE _
AC BD Corresponding angles $\angle 4 \ge \angle 3$ Corresponding angles		±16 ∠2 mAX mCx	Vertical opp. At Given	ngkes
mAX mCX mAC m VB mXB mIXB thence VA x C - AB x D	1	AC II BD ∠4≥ ∠3 ∠6≥ ∠5	Corresponding a	engles
The state of the s	Nich	mAX mCX mAC		* :
₹ ;		,	- <u></u> -	

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MATHEMATICS FOR 9Th CLASS (UNIT # 14)

hlot S	operone Mathematics 520 Class 9
	Review Exercise 14
Q .L.	Which of the following are true and which are
	false?
(i)	Congruen triangles are of same size and shape
(ii)	Similar triangles are of same shape but different sizes
(iH)	Symbol used for congruent is " ~
(iv)	Symbol used for similarity is ' 2'
(v)	Congruent triangles are sumilar
(M)	Similar trungles are congruent
(vii)	A line segment has only one mid point
(vih)	One and only one line can be draw through regoposits
(ix)	Proportion is non-equality of two ratios.
(x)	Ratio has no unit
ARN	
Q.2.	Delute the loston in #.
_	(i) Ratio (ii) Proportion
	(III) Congruent Troungles (iv) Similar Triangles
/\$#51	un.
(i)	Ratios
	We define ratio a $b = \frac{a}{b}$ as the companion of two aids:
:.)(quantities 'a' and 'b' called the elements of a ratio a is the first element and b is called the second element of
•	the ratio.
(ii)	Proportion:
1	The relation of equality of two ratios is called proportion. If $\mathbf{a} \cdot \mathbf{b} = \mathbf{c} \cdot \mathbf{d}$, then $\mathbf{a} \cdot \mathbf{b} \cdot \mathbf{c}$ and \mathbf{d} are said to
	be in proportion.
(ili)	Congruent Triangles:

Pilot Superone Mathematics 521 Class 95

If three sides of a triangle are equal in length to the corresponding three sides of another triangles then the triangles are called congruent triangles.

(iv) Similar Triangles

If three angles of a triangle are congruent to three corresponding angles of another triangle and their corresponding sides are proportional then these triangles are called similar triangles.

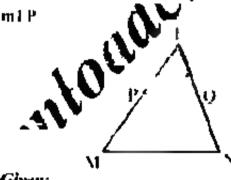
Remember:

Congruent triangles are also similar triangles but all similar triangles may or may not be congruent triangles.

Q.3 In Al MN shown in the figure, MN PQ

(i) If ml M Sem, ml P 2 Sem, ml D 23 cm, then find ml N

(iii) If ml \(\) 6cm ml \(\mathbb{Q} \) 2 \(\frac{1}{2} \mathbb{m} \), m() \(\times \) cm, there find



3(i) Given:

In ALMN

MN PQ

ml M Sem, m l P = 25 cm

and mIQ 2.3 cm Required:

ml N 2

W. Carrier

Pilot Superone Mathematics 522 Class 9 spotes.co.ii Calculations. Now men men as PO (MN) mLQ mlP $\frac{\text{mLb}}{23} = \frac{5}{25}$ putting the values 5 x 23 4.6 cm 3(ii) Given: In ALMN MN :: PO mON 5cm, and mIQ . 25 cm, mLM 6cm Required: Calculations: milP mil as PQ (M) <u>m1.Q</u> <u>m1.Q</u> m1.Q · mQN Pytting values $\frac{m\tilde{1}P}{6} = \frac{25}{25 + 5}$ mĹP <u>2.5</u> ×6 $\frac{1}{3} \times 6$

ĨP 2 cm

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MATHEMATICS FOR 9TH CLASS (UNIT # 14)

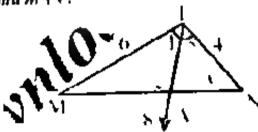
Phot Superone Mathematics 523 Cass 9th Q.4 In the shown figure, let mP1 = 8x = 7, mPB4x + 3, $m\overline{AO} = 5x - 3$, $m\overline{BR} = 3x - 1$ Find the value of x if $\overline{AB} \mid \overline{QR}$ Given. In APQR. AB # QR m PA Lns nt PR mAQ mBR ÄB # ÖR Required: Calculations: Statements Reasons **VPOR** mPÁ mΛO Putting values

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(8x 7)(3x 1) (4x 3)(5x 3) 24rt 29r+7 20r -27r+9

Pilot Superone Mathematics $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{16}$ SV $\frac{9}{2}$ $\frac{1}{2}$ s not possible.

Q.5. In ALMN shown in the figure, $T_m \hat{T}$ bivects $\angle L$. If $m \hat{T} \hat{N} = 4$ $m \hat{T} \hat{M} = 6$, $m \hat{M} \hat{N} = 8$, then find $m \hat{M} \hat{T}$ and $m \hat{T} \hat{N}$.



Given.

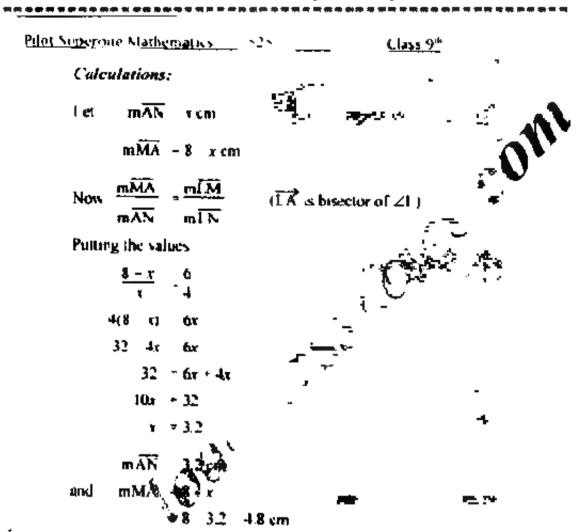
In ALMS 1 \(\) bisector of \(\alpha \) bom, mt \(\) 4cm, mMS \(8cm \) Required:

mMA ? and

was.

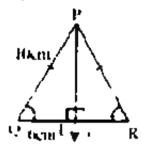
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MATHEMATICS FOR 9TH CLASS (UNIT # 14)



Q.6. In isosceles ΔPQR shown in the figure find the value of x and y.





Prior Superone Mathematics 576Class 9th
Given:
PQ́ ¶ PŘ
In ΔPQR
PL ±Q₹
Required:
x 25 2
Penaf:
Proof: Sustainents Reasons
In APRI and APQI -
m PQ ≠ m PR (i)
∠PLQ = ∠PLR Each 90°
m Pl. m Pl. Common
APQL = APRL HS = HS
mÖl miR
Corresponding sides of congruent triangles.
y 6 cm
10
Chile

ann, ton

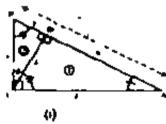
Pilot Superpre Mathematics

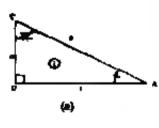
Class 9"

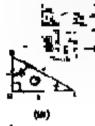


PYTHAGORAS THEOREM

in a right angled triangle, the square of the length of hypotenuse is equal to the sum of the squares of the lengths of the other two sides.







Given

ACB is right angled triangle to which $m\angle C = 90^{\circ}$ and mBC, a, mAC b and $mBB = 50^{\circ}$. To prove

$$c^2 = a^2 + b^2$$

Construction

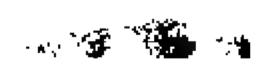
Draw \overline{CD} perpendicular from C on \overline{AB} .

Let m(D = h, mAD) = x and mBD = y. Line segment CD splits ΔABC into two As ADC and BDC which are separately shown in the figures (ii) -a and (ii) -b respectively. Proof (Using similar As)

ln.	Statements AADL - + AACB ∠A = ∠A ∠ADC = ∠ACB
	∠(' = ∠B
	AADC ~ AACB

Reasons
Refer to figure (a) a and (a)
common self congruent
Construction given, each
angle = 90°

ZC and ZB, complements of
ZA
Congruency of three angles



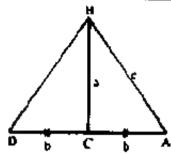
Pilot Superone Mathematics	528	Class 9
$\frac{r}{b} = \frac{b}{c}$		Fcorresponding i far triangles are)
or $x = \frac{b^2}{c}$ (1) Again in ABD(\leftarrow > ABCA $\angle B = \angle B$ $\angle BDC \cong \angle BCA$	Common-se	re (ri)- b and (i) elf c ingruent given, each
$\angle C \cong \angle A$ $\triangle BDC = \triangle BCA$ $\underbrace{P}_{a} = \underbrace{a}_{b}$	∠C and ∠A ∠B Congruency (Correspond	of three angles. Ing sides of a milar proportional)
or $y = \frac{a^2}{c}$ (11) But $y + x = c$ $\frac{a^2}{c} + \frac{b^2}{c} = c$ or $a^2 + b^2 = c^2$	Supposition the (I) and (ll) both sides by c.
1.e., $c^2 = a^2 + b^2$	<u> </u>	-

Converse of Pythagoras' Theorem

If the square of length one side of a triangle is equal to the sum of the squares' of the lengths of the other two sides then the triangle is a right angled triangle.

Wast.

Pilot Superone Mathematics



Given: In a $\triangle ABC$, m $\overline{AB} = c$, m $\overline{BC} = a$ and m $\overline{AC} = b$ such that

To prove: AABC is a right angled triangle.

Construction: (i) Draw \overline{CD} perpendicular to \overline{BC} such that

CD & CA

,ii) Join B to D.

. Statements	Rescone
ADCB is a right angled triangle.	Construction
$(m \overline{BD})^2 = a^2 + b^2 (i)$	Pythagoras theorem
But $a^2 + b^2 = c^2$ (11)	Given
$(m \overline{BD})^2 = c^2$	From i. p
or $(m\overline{BD}) = \zeta$	}
Nowin∆DCB ↔ ΔACB	
CD ≅ C A	Construction
BC ≈ BC	Common
DB x AB	each # c
. ΔDCB = ΛΛCB	333 ¥ 333
ZDCB ≆ ZACB	Corresponding angle of congruent triangles.
But <i>m2DCB</i> = 90°	Construction
$m\angle A(B = 90^{\circ}$,
Hence AACB is a right angled triangle	

Class 9th Pilot Si perone Mathematics 530

EXERCISE 15

- Q.1. Verify that the As having the following measures of sides are right angled. (i) a = 5cm, b = 12cm, c i3cm (ii) a = . 5cm, b = 2cm, c = 2 5cm (iii) a = 9cm, b = 12cm, c = 15cm (iv) a = 16cm, b = 30cm, c = 34cm

Solutions: 1(i)

$$\begin{vmatrix}
a = 5cm \\
b = 12cm \\
c = 13cm
\end{vmatrix}$$

$$\begin{vmatrix}
a^{2} = (5)^{2} = 25 \\
b^{2} = (12)^{2} = 144 \\
c^{2} = (13)^{2} = 169 \\
\begin{vmatrix}
a^{2} = (13)^{2} = 169
\end{vmatrix}$$

Now we see
$$c^2 = a^2 + b^2$$

 $169 \div 25 + 144 = 169$

The given lengths are the sides of a right angled triangle 1 (0)

$$a = 1.5cm$$

$$b = 2cm$$

$$c = 2.5cm$$

$$a^{2} = (1.5)^{2} = 2.25$$

$$and a = (2)^{2} = 4$$

$$c^{2} = (2.5)^{2} = 6.25$$

Now

$$a^2 = a^2 + b^2$$

6.25 = 2.25 + 4 = 6.25

The given lengths are the lengths of the sides of a right angled triangle

1 (道)



$$a = 9cm$$

$$b = 12cm$$

$$c = 15cm$$

$$a^{2} = (9)^{2} = 81$$

$$and b^{2} = (12)^{2} = 144$$

$$c^{2} = (15)^{2} = 225$$

Now we see
$$c^2 = a^2 + b^2$$
.
 $225 = 81 + 144 = 225$



Pilot Superone Mathematics 531 Class 97

The given lengths are the lengths of the sides of a right angled triangle

1(n)

$$\begin{vmatrix} a = 16cm \\ b = 30cm \\ c = 34cm \end{vmatrix} = \begin{vmatrix} a^2 = (16)^2 + 256 \\ and \quad b^2 = (30)^2 = 900 \\ c^2 = (34)^2 = 1156 \end{vmatrix}$$

$$c^2 = a^2 + h^2$$

Now we see 1156-256+900-1156

The given lengths are the lengths of the sides of a right angled triangle

Q.2. Verify that $a^2 + b^2$, $a^2 + b^2$ and 2ab are the measures of the sides of a right angled triangle where a and b are any two real numbers (a > 54.

Solution:

$$\begin{vmatrix} a^2 + b^2 \\ a^2 - b^2 \\ 2ab \end{vmatrix} \begin{cases} (a^2 + b^2)^2 = a^4 + b^4 + 2a^2b^2 \quad (i) \\ (a^2 + b^2)^2 = a^4 + b^4 - 2a^2b^2 \quad (ii) \\ (2ab)^2 = 4a^2b^2 \quad (iii) \end{cases}$$

Now we see if

$$(a^2 + b^2)^2 = (a^2 - b^2)^2 + (2ab)^2$$

From L M. H

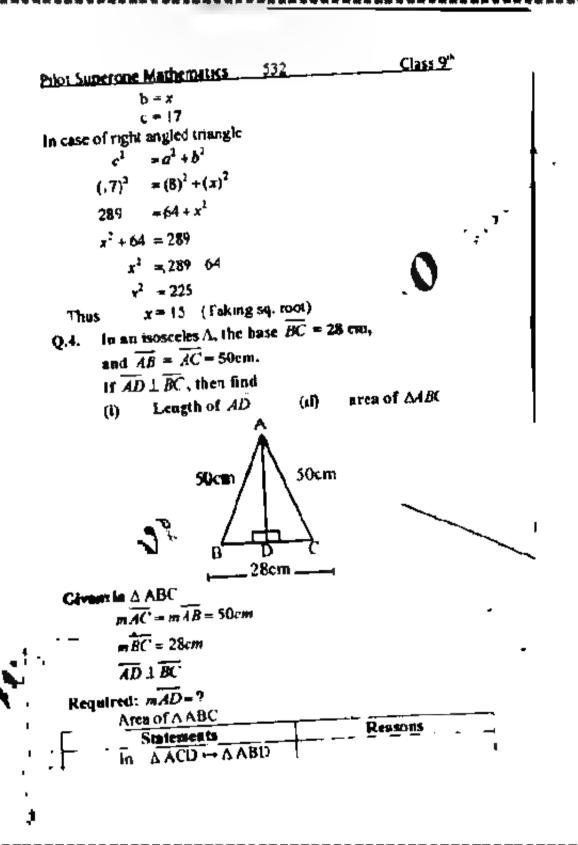
$$a^{4} + b^{4} + 2a^{2}b^{2} = (a^{4} + b^{4} - 2a^{2}b^{2}) + 4a^{2}b^{2}$$
$$= a^{4} + b^{4} - 2a^{2}b^{2} + 4a^{2}b^{2}$$

$$a^4 + b^4 + 2a^2b^2 = a^4 + b^4 + 2a^2b^2$$

The given lengths are the lengths of the side of a right angled triangle

The three sides of a triangle are of measure 8, x and 17 respectively. For what value of x will it become base of a right nagled triangle?

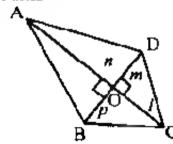
Solution. Lengths of the sides of a mangle



Prior Superone Mathematics	533 Class 9 th
$m\angle ADC = m\angle ADB$	each 90°
mAC ≈ mAB	g ven (Hyp)
mAD mĀD	common
$\Delta ABD = \Delta ACD$	Hyp side ∓Hyp side
$m\overrightarrow{BD} = m\overrightarrow{CD} = \frac{28}{2}$	
= 14 cm	'
Now in right angled \(\DC' \)	
$m\overline{CD} = 14cm$	
$\overline{AC} = 50$	given (Hyp)
$Now(mAD)^2 = (mAC)^2 - (mCD)^2$:
(50) ² -(14) ²	
= 2500 - 196	
- 2304	
Hence mAD = 18	l'aking sq root
Part (1	\
Area DABC = Base× Alt	
28×48	
2	
$=14\times48=672.Sq.cm$	

Q.5. In a quadrilateral ABCD, the diagonals \overrightarrow{AC} and \overrightarrow{BD} are perpendicular to each other.

Prove that $m\overline{AB}^2 + m\overline{CD}^2 = m\overline{AD}^2 + m\overline{BC}^2$



Pilot Superone Mathematics 534 Class 9th

Given ABCD is a quadrilateral in which its diagonals

 \overline{AC} and \overline{BD} are perpendicular to each other

Required: $(mAB)^2 + (mCD)^2 = (mAD)^2 + (mBC)^2$

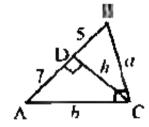
Proof

Statements	
Let $m\overline{OC}$ -1	,
ndOD = m	;
mOrl = r	!
mOB̃ = p	1
In right angled AOCD	
$(mCD)^2 = l^2 + m^2 (P)$	
in right angled AABO $(mAB)^2 = n^2 + p^2$	
Now $(mAB)^2 + (mED)^4 = I^2 + m^2 + n^2 + p^2$	from (i) + (ii) (L)
In right angled A AOD	
$(mAD)^2 = n^2 + m^2 \qquad (vi)$	
in right angled A BOC	
$(mBC)^2 = p^2 + l^2 \qquad (tr)$	•
Now $(mAD)^2 + (mBC)^2 = A^2 + m^2 + p^2$	From ii. + iv M
Thus $(mAB)^2 + (mCD)^2 = (mAD)^2 + (mBC)^2$	from I and M

Q.6. (i) In the & ABC as shown in the figure.

mZACB = 90° and CD \(\frac{1}{2}\) AB Find the lengths a, h and

b if mBD - Spaits and mAD 7 units

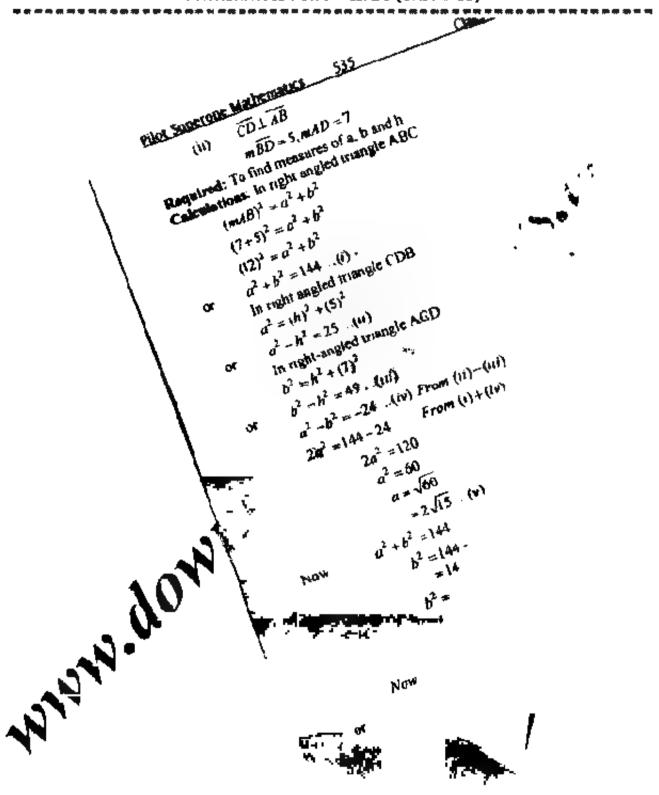


Given: In AABC

(i) $m = 1CB = 90^{\circ}$

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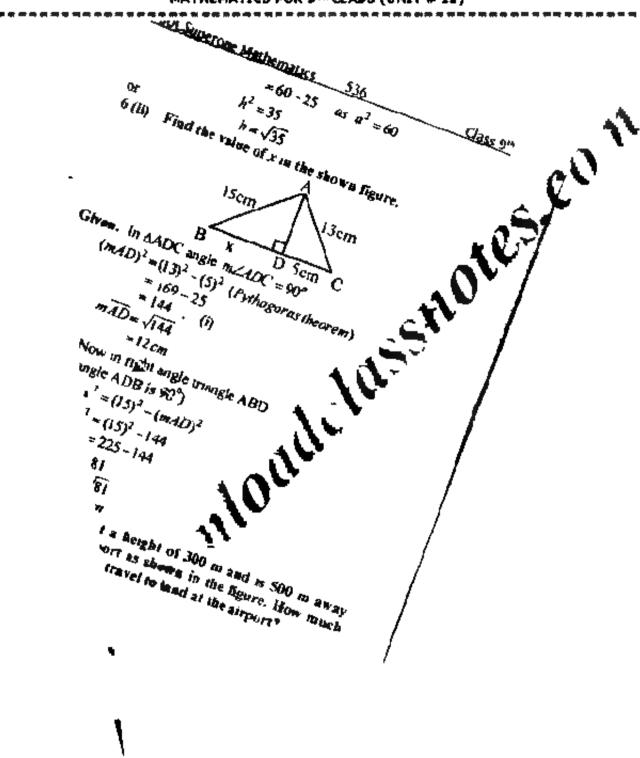
MATHEMATICS FOR 9TH CLASS (UNIT # 15)



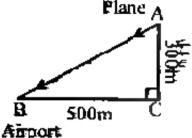
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MATHEMATICS FOR 9TH CLASS (UNIT # 15)



Pilot Superone Mathematics 537 Class 9th Plane A

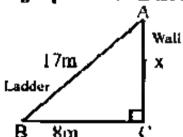


Solution: ABC is a right-angled triangle at C...

$$(mAB)^2 = (mAC_L^2 + (mBC)^2 (PythagoromTheorem)$$

 $(300)^2 + (500)^2$
 $= 90000 + 250000$
 $(mAB)^2 = 340000$
 $mAB = \sqrt{340000}$
 $= \sqrt{34 \times 100 \times 100}$

8. A fadder 17m long rests against a vertical wall. The foot of the ladder is 8 m away from the base of the wall. How high up the wall will the ladder reach?



Solution. Let \overline{AB} be the ladder

 $mA\bar{I}\bar{I}$ = 100 $\sqrt{34}$ m

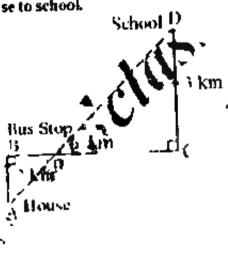
Now ABC is a right-angled triangle at C

Marie Commence

Pilot Superone Mathematics 538 Class 9 $(mAC)^2 = (mAB)^2 \quad (mBC)^2 \quad (Pythagaras Theorem)$ $Now(mAC)^2 = (17)^2 \quad (8)^2$ $= 289 \quad 64$ = 225 $mAC' = \sqrt{225} \quad Taking sq root$ mAC' = 15m

The ladder reaches upto 15m high.

 A student travels to his school by the route as shown in the figure. Find m 4D, the direct distance from his house to school.



Solutions

$$m\overline{PC} = (6-x)km$$

$$\frac{x}{6-x} = \frac{2}{3}$$

$$3x = 12-2x$$

$$5x = 12$$

$$x = \frac{12}{5} = mBP$$

PI

Pilot Superone Mathematics 539 Class 9' $mPC = 6 - \frac{12}{5} = \frac{18}{5}$ $ln PCD \triangle mP^2D = mP^2D + mc^2D ln$ $= \left(\frac{18}{5}\right)^2 + (3)^2$ $= \frac{324}{25} + 9 = \frac{324 + 225}{25}$ $= \frac{549}{25}$ $= \sqrt{\frac{549}{25}} = \sqrt{\frac{3 \times 3 \times 61}{5 \times 5}}$ $= \frac{3}{5}\sqrt{61} \, km$

REVIEW EXERCISE 15

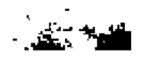
Which of the following are true and which are false?

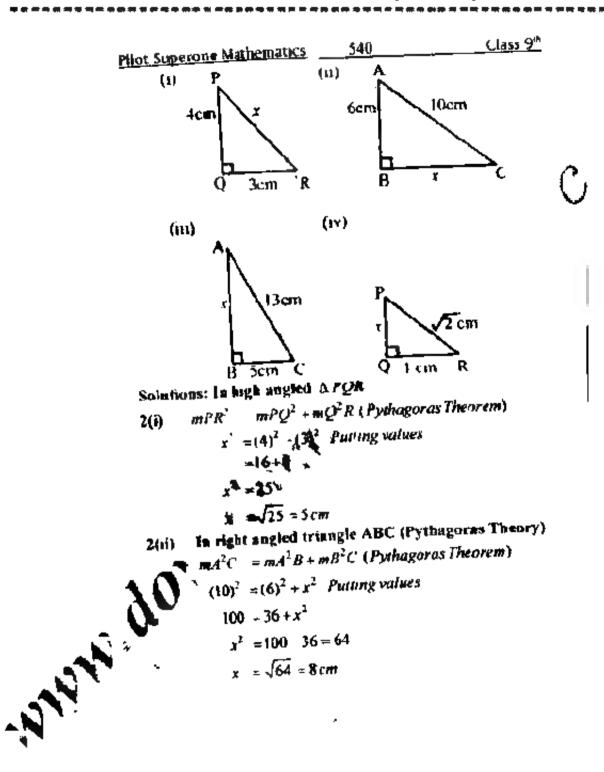
- (i) In a right angled triangle greater angle is of 90°
- (ii) In a right angled triangle right angle is of 60°
- (III) In a right triangle hypoteraise is a side opposite to right angle.
- (iv) If a, b, c are sides of right angled triangle with c as longer side then $c^2 = a^2 + b^2$
- (v) If 3 cm and 4 cm are two sides of a right angled triangle, then hypotenuse is 5 cm.
- (vi) If hypotenuse of an isosceles right triangle is $\sqrt{2}$ cm then each of the other side is of length 2 cm

Arswers:

- (i) | (ii) | F (iii) | 1 (iv) | F (v) | T (vi) | F
- Find the unknown value in each of the following figures.







Pilot Superone Mathematics 541 Class 9th

2(iii) In right angled 4 ABC

$$(mAC)^2 = (mAB)^2 + (mI + 3C)^2$$
 (Pythagoras Theorem)

$$(13)^2 = x^2 + (5)^2$$
 Put ting values

$$169 = x^2 + 25$$

$$x^2 = 169 - 25 = 1.44$$

$$x = \sqrt{144 \cdot 12c} \ m \ (Laking sq. root)$$

2(w) In right angled △ PC →R

$$(mPR)^2 = (mPQ)^2 + (mQR)^2$$
 (Pythagorus Theorem)

$$(\sqrt{2})^2 = x^2 + (1)$$
 Patting values

$$2 = x^2 + 1$$

$$r^2 = 2 - 1 = 1$$

$$x = \sqrt{cm}$$
 (Taking sy root)



Poot Superone Ma hematics 542 Class 9th Unit THEOREMS RELATED WITH AREA Area of a Figure The region enclosed by the bounding lines of a closed figure is called the Area of the figure. Triangular Region The interior of a triangle is the part of the plane enclosed by the triangle A triangular region is timon of a triangle and its interior Area of a triangle means the area its triangular region. Rectangular Region The interior of a rectangular is the part of the plane enclosed by the rectangle A rectangular region is the union of a rectangle and its

Area of a rectangular region is the product of the length and width of the region.

Pilot Superone Mathematics 543 Class 9"

Altitude of a parallelogram

If one side of a para letogram is taken as its base, the perpendicular distance between that side and the side parallel to it is called the Aktitude or Height of the parallelogram.

Altitude of a Triangle

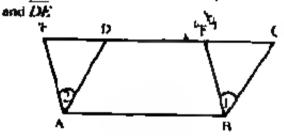
If one side of a triangle is taken as the base, the perpendicular to that side from the opposite vertex is called the Attitude or Height of the triangle.

Theorem

Parallelograms on the same base and between the same parallel fines (or of the same altitude) are equal in area.

Ghen

I wo parallelograms ABCD and ABcd baving the same base AB and between the same parallel lines \overline{AB}

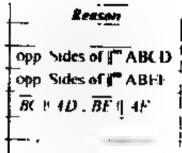


To prove

area of parallelogram ABCD = area of parallelogram ABEF

Presi

	. Semement
	In AEBC ↔ FAD
	CB ≥ DM
	BE = 4F
. 1	∠1 ≟ ∠2
	$\triangle EBC \cong \Delta FAD$
	. Area of A EBC = Area of A FAD





Paior Superone Mathematics 544	Class 9°
Also are of quad ABED = Area of quad	(same quad) (it)
Adding (1) and (ii)	
AEBC + area quad ABED - AFAD	
area quad ABED Hence ABCD (area) ABEF	
QED . Theorem	
poitelegrams on cough bases	and having the same
(or equal) shirtede are equal to	H
	<i>></i> 7

Parallelograms ABCD, EFGH are on the equal bases

BC, FG, having equal disjudes.

To Prove

area of (parallelogram ABCD) = area of (perallelogram [FGb)

Construction

Place the parallelograms ABCD and EFGH so that their equal bases \overline{BC} , \overline{FG} are in the straight line BCFG. Join

BC and TCH

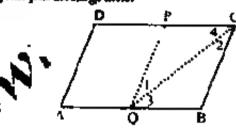
Proof	
Sestements	Reasons
The given is ABCD and EFGH are between the same	Them altitudes are equal (given)
Parallels Hence ADEH is a straight line	
to <u>BC</u>	
mBC = mFU	Given
	F.FGH is a parallelogram
= mEH	<u> </u>



Pilot Superone Mathematics	545 Class 9*
Now $mBC = mEH$ and they are [
BF and CH are both equal and	
Hence EBCH is a parallelogram	A quadrilateral with two opposite sides congruent and parallel is a parallelogram
Now i ^{EM} ABCD = j ^{EM} FBCH	Being on the same base BC and between the same parallels
But EBCH = EFGH . (ii)	Being on the same base EH and between the same parallels
Hence area (ABCD) = area(E FGH)	From (i) and (ii)

EXERCISE 16.1

Q.1 Show that the line segment joining the mid-points of opposite sides of a parallelogram, Divides it into two equal parallelograms.





- () ABCD is a []**
- (ii) P is mid point of DC 1.e. DP = PC
- (iii) Q is mid point of AB i.a. AQ = OB
- (iv) P is joined to Q.

 Required:

 | P AQPD ≅ | P OBCP



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MATHEMATICS FOR 9TH CLASS (UNIT # 16)

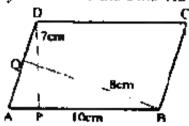
Pilot Superone Mathematics 546 C.ass 9th Construction: Join Q to C.

	Preof:	
	Statements	I
 	$\frac{m\overline{AB} = m\overline{DC}}{\frac{1}{2}m\overline{AB}} = \frac{1}{2}m\overline{DC}$	Opp. sides of ABCD Dividing by 2
or Now	mQB = mPC in ΔPQC ΔQBC QC ≈ QC QB ≈ PC ∠3 ≈ ∠4 ΔQBC ≈ ΔPQC (i) PQ ≈ CB	Common Proved Alternate angles AB DC S.A.S = S.A.S. Corresponding sides of cong. triangles Opp. side of ^m
	(ii) $\overrightarrow{AD} = \overrightarrow{CB}$ $\overrightarrow{PQ} = \overrightarrow{AD} = \overrightarrow{BC}$ $\angle 1 = \angle 2$	Corresponding angles of cong. Triangles
m∠4 or and or	L+m∠3=m∠2+ ∠PQB ≈ m∠PCB ∠A ≈ m∠PCB ∠A ≈ m∠PQB in QBCP = AQPD ^m AQ ≈ QB AD ≈ PQ	Given Proved Proved
(Therei	∠A ≆ ∠PQB fore	



Pilot Superone Mathematics 547

Q.2 In a parallelogram ABCD, mAB = 10cm. The allitudes corresponding to sides AB and AD are respectively 7 cm and 8 cm. Find \overline{AD}



Given:

ABCD is a []th in which.

- mAB **(i)** 10 cm
- (ii) Alt DP

Required:

To find m AD

Solution:

Area of
$$\int_0^\infty ABCD = 10 \times 7$$

- 70 sq cm (1)

In second case:

Base =
$$\overline{AD}$$

Area of $||^m ABCD = (2) \times (m AD)$

$$70 = 8 \times (m \overline{AD})$$
 from (i)

$$m\overline{AD} = \frac{70}{8} \cdot \frac{35}{4} \text{ cm}$$







Pilot Superone Mathematics 548

Q.3 If two parallelograms of equal areas have the same or equal bases, their alutudes are equal.

D

C

S

R

Given:

In || ABCD and PQRS

Area || ABCD = Area || PQRS

And Base AB = Base PQ

Alt of ABCD is DM

Alt of PQRS is SN

Required:

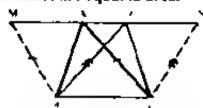
Statements	Reasons
Area ABCD = Area PQRS *	
Now (mAB)(mDMQ ⇒ (mPQ)(mSN)	Area of * Base × Alt.
(mAB)(mDM) = (mAB)(m5N)	$m\overrightarrow{AB} = m\overrightarrow{PQ}$ (given)
m DAN ≒.mSN	

Proof:

Pilot Superone Mathematics 549 Class 9 *

Theorem

Trungles on the same base and of the same (i.e. equal) sittledes are equal in area.



Given.

As ABC, DBC on the same base BC, and

having equal altitudes.

To Prove:

area of (ΔABC) = area of (ΔDBC)

Construction: Draw BM || to CA, CN || to BD AD meeting.

produced in M, N.

Proofs

2.000	<u> </u>
Statements	Reasons
ΔABC and ΔBCD are hittween the same ¹	Their altitudes are equal
Hence MADN is parallel to BC Area (PBCAM) = Area (PBCAM) (1)	These ^{am} are on the same base ^{BC} and between the same ^a
But $\triangle ABC = \frac{1}{2} (i)^{-1} BCAM (ii)$	Each diagonal of a igm bisects in the into two congruent triangles
And $\Delta DBC = \frac{1}{2} (P BCND)$ (iii)	
Hence Area (∆ABC) ≠	From (i), (ii) and (iii)

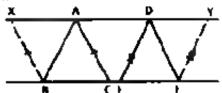


Area (ADBC)

Pilot Superone Mathematics 550 Cass 9th

Theorem

Triangle on equal bases and of equal aktitudes are equal in area.



Given:

Δs ABC, DFF on the same base BC, BF and

having altitudes equal.

To Prove:

Area of (\triangle ABC) = Area of (\triangle DEF)

Construction:

Place the DFABC and DEF so that their equal bases BC and EF are in the same straight line BCEF and their vertices on the same side of it. Draw BX It to CA and FY || to ED meeting AD produced in X, Y respectively



Proof:	
Statement	Reasons
Δ ABC and Δ DEF are between the same parallels XADY is to BCEF Area (BCAX) = Area (EFYD) (But ΔABC = 1/2 (BCAX) ((given) These ^{gen} are on equal bases and between the same parallels Disconsi of a life bases it
And $\triangle DEF = \frac{1}{2} (f ^{-1} EFYD)$ (iii))
Hence Area (ΔABC) = Area (ΔDE)	From (i), (ii) and (iii)

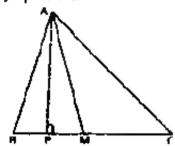


Priot Superone Mathematics 551

Class 9th

EXERCISE 16.2

Q.1 Show that a median of a triangle divides it into two triangles of equal area.



Given:

In AABC: AM is a median i.e mBM = mMC

Required:

Area A AMC = Area A ABM

Proof:

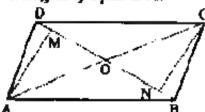
Area of $\triangle ABM = \frac{mAP \times mBM}{}$ (i)	
2 '	
Area of $\triangle AMC = \frac{mAP \times mMC}{2}$	
$= \frac{m\overline{AP} \times m\overline{BM}}{2} (ii)$	$mBM = m\overline{MC}$ (given)
Area of AABM=Area of AAMC	
Similarly it can be proved that every median of a triangle divides it into two triangles equal in area.	





Pilot Superone Mathematics 552 Class 9th

Q.2 Prove that a parallelogram is divided by its diagonals into four triangles of equal area.



- Given: (1) ABCD is a ||^m
 - (ii) AC and BD are its diagonals that intersect each other at O.

Required: $\triangle OBC = \triangle OCD = \triangle OAD = \triangle OAB$ Construction:

- (i) Drop perpendicular from C to \overline{DB} i.e. \overline{CN}
- (ii) Drop perpendicular from A to DB i.e AM

Proof:

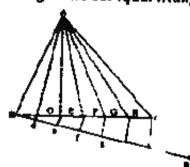
Statements 3 %	Reasons		
m OB = m OD	Diagonals of a m bisect each		
mOA = mOC	other		
$\Delta OBC = \frac{m\overline{OR} \times m\overline{CN}}{2} (i)$			
And $\Delta U \Delta D = \frac{mOD \times mCN^2}{2}$			
$= \frac{m\overline{OB} \times mCN}{2} (0)$			
ΔOBC = ΔOAD			
Similarly \(\Delta OAD = \Delta OAD \)			
$\triangle OBC = \triangle OCD = \triangle OAD = \triangle OAB$	From (i) and (ii)		

Written/Composed by - <u>SHAHZAD 1FTIKHAR</u> Contact * 0313-5665666 Website <u>www.downloadclassnotes.com</u>, E mail <u>ranshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 16)

Pitot Superone Mathematics 553 Class 9th

Q.3 Divide a triangle into six equal triangular parts.



Given:

ABC is a triangle

Recuired

To divide AABC

qual triangular parts

(triangles)

Construction:

(i) Fake BP any rav

i acute angle with

 \overline{BC}

(ii) Draw six arcs of the i.e. mBd = mde = mef

uson BP meh mhe

(ui) Joan o To C and parallel line oC || hH || aG || fF | cE || do

पादमांड वड

(IV) Join A to O, E, F, Q, R

Proof:

Base BC of AABC has been divided to equal parts six in number

We get six triangles having equal base and same

Their area is equal

Hence $\triangle BOA$ $\triangle AOEA = \triangle EFA = \triangle FGA = \triangle GHA = \triangle HCA$





Pilot Superone Mathematics 554 Class 9" Review Exercise 16 Which of the following are true and which are false? Q.IArea of a figure means region enclosed by bounding (i) lines of closed figure. Similar figures have same area. (ii) Congruent figures have same area. (in) A diagonal of a parallelogram divides it into two non-(lv)congruent triangles. Altitude of a triangle means perpendicular from vertex (v) to the opposite side (base). Area of a parallelogram is equal to the product of base (vi) and height. Answers: (v) (lii) T Ai) (i) Ŧ (vi) Find the area of the **following figures.** 0.2 (i) (ii) 3 cm 4 cm (iv) 8cm 4 cm ന് അ Length of the rectangle = 6 cm

Width of the rectangle = 3 cm

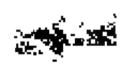
6×3

Area of the rectangle

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MATHEMATICS FOR 9TH CLASS (UNIT # 16)

Pilo	t Superone Mathematics 555 Class 9th					
2(ii)	Area = (side) ²					
2(iii)	$= (4)^{2}$ $= 16 \text{ sq. cm}$ Length of side of a $\ ^{m} = 8 \text{ cm}$ Act of the $\ ^{n} = 4$ Area = 8×4					
2(iv)	= 32 sq. cm Base of the triangle = 16 cm Alt = 10 cm					
	Area of the $\Delta = \frac{16 \times 10}{2}$ = 80 sq. cm					
Q .3	Define the following (i) Area of a figure (ii) Triangular Region (iii) Rectangular Region (iv) Altitude or Height of a triangle					
Soluti	ton:					
3(1)	Area of a figure					
	Area of a figure means region enclosed by the boundary lines of a closed figure.					
3(11)	Triangular Region					
	A triangular region means the union of triangle and its					
3(111)	Rectangular Region					
	A rectangular region is the union of a rectangle and its interior					
3(14)	Aithude or Height of a triangle					
	Altitude or height of a triangle means perpendicular distance to base to base from its opposite vertex.					



Pilot Superone Mathematics



PRACTICAL GEOMETRY

EXERCISE 17.1

Construct a AABC in which Q.1

(i)
$$mAB = 3.2 \text{ cm}, mBC = 4.2 \text{ cm}, mCA = 5.2 \text{ cm}$$

(ii)
$$m\overline{AB} = 4.2 \text{ cm}$$
, $m\overline{BC} = 3.9 \text{ cm}$, $mCA = 3.6 \text{ cm}$

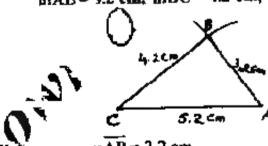
(iii)
$$mAB = 4.8 \text{ cm}, mBC = 3.7 \text{ cm}, m\angle B = 60^{\circ}$$

(v)
$$mB\bar{C} = 4.2$$
 cm, $mC\bar{A} = 3.5$ cm, $m\angle C = 75$ °

(vi)
$$mAB = 2.5$$
 cm, $m\angle A = 30^{\circ}$, $m\angle B = 105^{\circ}$

Construct a AABC in which 1(i)

 $m\overline{AB} = 3.2$ cm, $m\overline{BC} = 4.2$ cm, $m\overline{CA} = 5.2$ cm



 $m\overline{AB} = 3.2 \text{ cm}$

 $m\overline{BC} = 42 cm$

mCA 5.2 cm

Required: Construct a AABC

Step of Construction:

Take a line segment CA = 5.2 cm (i)

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

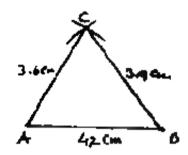


Pilot Superone Mathematics 557 Class 9rd

- (ii) Taking C as centre and draw an arc of radius 4.2 cm.
- (in) Taking A as centre and draw another arc of radius 3.2 cm. It intersect the first arc at B
- (iv) Join C to A and B.

Result. ABC is the required triangle

I(ii) Construct a $\triangle ABC$ in which $mA\overline{B} = 4.2$ cm, $m\overline{BC} = 3.9$ cm, $m\overline{CA} = 3.6$ cm



Given.

 $m\overline{AB} = 4.2 \text{ cm}$ $m\overline{BC} = 3.9 \text{ cm}$ $m\overline{CA} = 3.6 \text{ cm}$

Required: Construct a AABC

Steps of Construction:

- (i) Take a line segment AB of length 4 2 cm.
- (ii) Take A as centre and drawn arc of 3.6 cm radius.
- (iii) Take B as centre and draw an are of 3 9 cm radius.
 This cuts the first are at C.
- (iv) Join C to A , B

Result: ABC is the required triangle.



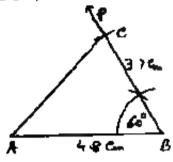
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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 558 Class 9"

1(iii) Construct a AABC in which

 $\overline{MAB} = 4.8 \text{ cm}, \ \overline{MBC} = 3.7 \text{ cm}, \ \overline{MZB} = 60^{\circ}$



Given:

mAB = 4.8 cm

 $m\overline{BC} = 3.7 \text{ cm}$

m∠B 60°

Required: Construct triangle ABC

Steps of Construction:

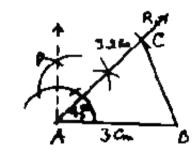
- (i) Take a line segment AB : 4.8 cm.
- (ii) Make an angle of 60° at B
- (iii) Cut off $\overline{BC} = 3.7$ cm from \overline{BP}
- (iv) Join C to A.

Result. ABC is the required triangle.

ob. ware.

Pilot Superone Mathematics 55II

I(iv) Construct a triangle ABC in which
mAB = 3 cm, mAC = 3.2 cm, m∠A = 45°



Given:

$$\mathbf{m}\overline{\mathbf{AC}} \approx 3.2 \, \mathrm{cm}$$

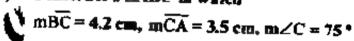
Required: Construct a triangle ABC

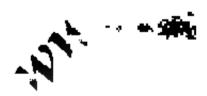
Steps of Construction.

- (i) Take a line segment AB = 3 cm.
- (ii) Make an angle of 45° at A.
- (iii) Take A as centre and cut off $\overrightarrow{AC} = 3.2 \text{ cm on } \overrightarrow{AR}$
- (iv) Jom C to B.

Result: ABC is the required triangle.

I(v) Construct a AABC in which





Prior Superone Mathematics 560 Class 9"



Given:

$$mB\hat{C} = 4.2 cm$$

$$m \angle C = 75^{\circ}$$

Required: Construct a AABC

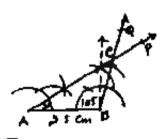
Steps of Construction.

- (i) Take a line segment CA = 3.5 cm.
- (ii) Make an angle of 75° at C.
- (iii) Cut off CB = 42 cm from CP
- (iv) Join B to A

Result: ABC is the required triangle.

J(vi) Construct a AABC in which

mAB=2.5 cm, m∠A = 30°, m∠B = 105 °



Given:

 $m\overline{AB} = 2.5 \text{ cm}$

Pilot Superone Mathematics 561 Class 91

$$m\angle A = 30^{\circ}$$

Required: Construct a triangle ABC

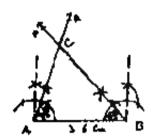
Steps of Construction:

- (i) Take a line segment $\overrightarrow{AB} = 2.5 \text{ cm}$
- (ii) Make an angle of 45° at A.
- (iii) Make an angle of 105° at B
- (iv) AP. BQ intersect at C

Result. ABC is the required triangle

I(vii) Construct a AABC in which

 $mAB = 3.6 \text{ cm}, m\angle A = 75^{\circ}, m\angle B = 45^{\circ}$



Cham

Required: Construct a triangle ABC

Steps of Construction:

- (i) Take a line segment AB = 36 cm
- (it) Make an angle of 75° at A.
- (iii) Make an angle of 45° at B
- (iv) AR and BP intersect at C



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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

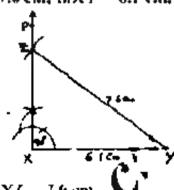
P.lot Superone Mathematics 562 (Lasy 9)

Result. ABC is the required triangle

O.2 Construct a AXV Z in which.

- (i) $mY/ = 7.6 \text{ cm}, mXY = 6.1 \text{ cm}, m\angle X = 90^{\circ}$
- (ii) mZX = 6.4 cm, mYZ = 2.4 cm, mZY = 90°
- (iii) $mXY = 5.5 \text{ cm}, m/X = 4.5 \text{ cm}, m/Z = 90^\circ$
- 2(i) Construct a ΔΧΥΖ in which.

mY/ 7.6 cm, mXY 6.1 cm, mZX 90°



Given:

mY7 7.6 cm

mXY 6 Feat

m∠X 💖 -

Required:

Construct a triangle XYZ

Steps of Construction.

- (i) Take a line segment XY 6.1 cm
- (n) Make an angle of XYP of 90° at X
- (iii) Take Y as centre and draw an are of radius of 7.6 cm. This are intersect XP at /
- (iv) Join / to Y

Result. XYZ is the required triangle.

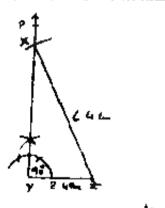


Pilot Superone Mathematics 563

(1458.9)

2(ii) Construct a AXY Z in which,

m/X = 6.4 cm, mY/ = 2.4 cm, $m\angle Y = 96^{\circ}$



Given

m/X 644m

24 .m

m∠ Y 90°

Required: To construct \$ AXY

Steps of Construction:

(i) Take a line segment \$\forall 2.4 cm

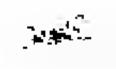
(ii) Make an angle of 90° at Y.

(iii) Take z as conffe and draw an arc of radius 6.4 cm. which cuts \(\bar{V}\)P at X.

(iv) Jam X to /

Result: XY/ is the required triangle







Pilot Supergne Mathematics 564 Class 9

2(iii) Construct a AXYZ in which

 $mXY = 5.5 \text{ cm}, \ mZ\overline{X} = 4.5 \text{ cm}, \ m\angle Z = 90^{\circ}$



Given.

$$m\overline{LX} = 4.5 \text{ cm}$$

Required:

Construct a AXYZ

Steps of Construction:

- (i) fake a line segment $\overline{ZX} = 4.5$ cm
- (ii) Draw an angle ∠XZP of Z of 90°
- (iii) Take X as centre and draw an arc of 5 5 cm radius.

 which cuts ZP at Y
- (iv) Join Y to X.

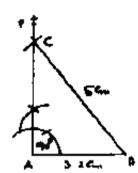
Result: XY/ is the required triangle

T 7

PIP

Pilot Superone Mathematics 565. Class 9th

Q.3 Construct a right angled triangle measure of whose hypotenuse is 5 cm and one side is 3.2 cm.



Given: I ength of hypotenuse = 5 cm

One side

= 3 2 cm

Required: To construct a right angled triangle.

Steps of Construction:

- (i) Take a line segment of 3.2 cm.
- (n) Make an angle ZBAP = 90° at A.
- (ii) Take B as centre and draw an arc of radius 5 cm which cuts AP cuts at C
- (iii) Join C to A.

Result: ABC is the required triangle

- Q4 Construct a right angled isosceles triangle whose hypotenuse is
 - (i) 5.2 cm
- (ii) 4.8 cm
- (in) 6.2 cm
- 6.2 cm (iv) 5.4 cm long.



Palot Superore Mathematics 40j 5.3 cm Given: Tength if hypotentise 5.2 cm o construct a right angled two wells Required. triancle Steps of Construction. ake a me segment AB 52 6 6.3 ake O as mid-point by drawing PQ as 4113 perpendicular b sector of Alb ake O as centre and draw a semi-circle of radius OA 1663 Jour C to Sand B ₩\\$C*is the required isosceles right impled R side Bearing to at C 4.8 cm

Pilot Superone Mathematics 567 Class 9*

Given: I ength of hypotenuse 48 cm

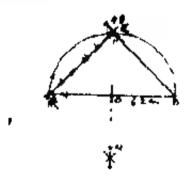
Required: To construct a right angled isosceles triangle

Steps of Construction:

- (i) Take a line segment A.3 = 4.8 cm
- (ii) Draw PQ right bisector of AB which cuts AB #0
- (iii) Take O as centre and draw a semi-circle of radios OA or OB which cuts PQ at C
- (IV) Join C to A and B

Result: ABC is the required triangle which is right angled at C and mAC mBC.

4(ui) 6.2 cm



Ghen I ength of hypotenuse 6.2 cm

Required To construct a right angled isosceles (it agle with hypotenuse = 6.2 cm.)

Steps of Construction:

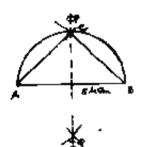
- () Take a line segment AB = 6.2 cm
- (ii) Draw Pr) right bisector of AB which cuts AB at (

Pilot Superone Mathematics 568 Class 9"

- (1ti) Take O as centre and draw a semi-circle of radius \overrightarrow{OA} or OB which cuts \overrightarrow{PQ} at C
- (iv) Join C to A and B

Result: ABC is the required triangle which right-angled at C and $\overrightarrow{mAC} = \overrightarrow{mBC}$

4(iv) 5.4 cm



Given: Length of hypotenuse = 5.4 cm

Required: To construct a right angled isosceles triangle

Steps of Construction:

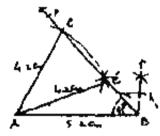
- (i) Take a line segment $\overrightarrow{AB} = 5.4$ cm.
- (ii) Draw PQ right bisector of AB which cuts it at point
- (iii) Take O as centre and draw a semi-circle of radius OA or OB which cuts PQ at C
- (iv) Join C to A and B

Result: ABC is the required triangle which is rightangled at C and mAC - mBC

- Q.5 (Ambiguous Case) Construct a AABC in which
- (i) $m\overline{AC} = 4.2 \text{ cm}, m\overline{AB} = 5.2 \text{ cm}, m\angle B = 45^{\circ}$
- (ii) $m\overline{BC} = 2.5 \text{ cm}, m\overline{AB} = 5.0 \text{ cm}, m\angle A = 30^{\circ}$

Pilot Superone Mathematics 569 Class 9th

(21) mBC = 5 cm, mAC = 3.5 cm, m
$$\angle$$
B = 60°



Given: $\overrightarrow{mAC} = 4.2 \text{ cm}$ $\overrightarrow{mAB} = 5.2 \text{ cm}$ $\overrightarrow{m} \angle B = 45^{\circ}$

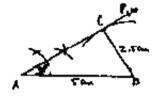
Required: To construct triangle ABC.

Steps of Construction:

- (i) Take a line segment AB 5.2 cm
- (ii) Make an angle $\angle ABP = 45^{\circ}$ at point B
- (in) Take point A as centre and draw an arc of 4.2 cm radius. It cuts \overrightarrow{BP} at two points C, C'
- (iv) Join C, C to A

Result: Two \D' ABC, ABC' fulfill the requirements

5(ii) $mB\overline{C} \approx 2.5$ cm, $m\overline{AB} = 5.0$ cm, $m\angle A = 30^{\circ}$





Given: mBC 25 cm mAB = 50 cm

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 570 Class 9°

m. 4 30°

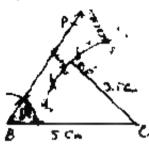
Required: Construct a VABC

Steps of Construction:

- (i) Take a line segment AB 5 cm.
- (ii) Make an angle z BAP 30° a. A
- (iii) Take B as centre and draw an arc of 2.5 cm radius. This arc touches $\Delta \hat{P}$ at C.
- (re) Join C to A.

Result: ABC is the required triangle

5(rin) Construct a triangle ABC in which is mBC = 5 cm, mAC = 3.5 cm, maZB = 60°



Given mile com

Required Construct a triangle ABC

Sueps of Construction:

- Take a line segment BC 5 cm
- (ii) Make an angle ∠ CBR of 60° at B
- (iii) Take C as centre and draw an arc of \$5 cm richus. This are coes buch and out BR at any point.



Prior Supero to Mathematics 571 Class 9

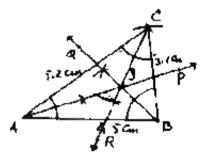
Result: I mangle ABC cannot be constructed with the given sides and angle.

Remember

- (i) The internal bisectors of the angles of a triangle meet at a point on led the incentre of the triangle
- (ii) The point of concarrency of the three perpendicular bisectors of the sides of a A is called the circumcentre of the A.
- (iii) The point of concurrency of the three altitudes of a Vis called its orth scenter.
- (iv) The point where the three medians of a A meet is called the centroid of the triangle.

EXERCISE 17.2

- Q1 Construct the following & ABC. Draw bisectors of their angles and verify their concurrency
- (i) mAB = 4.5 cm, mBC = 3.1 cm and mCA = 5.1 cm
- (ii) $mAB = 4.2 \text{ cm} \cdot mB(-6 \text{ cm and } m(A = 5.2 \text{ cm})$
- (iii) at AB = 3.6 cm, and C = 4.2 cm and at $ZB = 75^{\circ}$
- 10) mABF = 4.5 cm, mBC 3.1cm and mCA 5.2cm



Given: mAB 45 cm

Class 9" Pilot Superone Mathematics 572

 $mB\hat{C} = 3.1cm$

mCA 5.2cm

Required: Construct AABC and see the concurrency of the bisectors of its angles

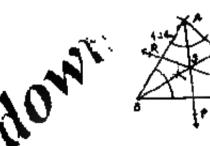
Steps of Construct:

- Take a line segment \overline{AB} = 4.5 cm (i)
- Take A and B as centers and draw arcs of 5.2. tii) 3.1cm radii respectively. These are intersect each other at point C
- Join C to A and B ABC is the required triangle. (iii)
- (iv) Take AP, BQ, CR bisectors of angles A, B, C respectively.

Result:

We see that bisectors \overrightarrow{AP} , \overrightarrow{BQ} , \overrightarrow{CR} are concurrent at point ...

1(ii) $m\overline{AB} = 4.2$ cm, $m\overline{BC} = 6$ cm and $m\overline{CA} = 5.2$ cm



$$m\overline{AB} = 4.2 \text{ cm}$$

$$m\overline{RC} = 6 \text{ cm}$$

$$\overrightarrow{mCA} = 5.2 \text{ cm}$$

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 573 Class 9th

Required: Construct AABC and verify the concurrency of the bisectors of its angles.

Steps of Construction:

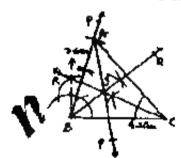
- (i) Take a line segment $\overrightarrow{BC} = 6$ cm
- (ii) Take B as center and draw an ares of 4.2 cm radius
- (iii) Take C as centre and draw an arc of 5.2 cm radius that cuts the first arc at point A.
- (iv) Join A to B and C.

 AABC is the required triangle
- (v) Take AP, BQ and CR bisectors of angle A. B and C respectively

Result

 \overrightarrow{AP} , \overrightarrow{BQ} , \overrightarrow{CR} are concurrent at point I

1(iii) $\overline{MAB} = 3.6$ cm, $\overline{MBC} = 4.2$ cm and $\overline{MZB} = 75^{\circ}$



Given:

mAB - 36 cm

 $m\overline{BC} = 4.2 \text{ cm}$

 $m\angle B = 75^{\circ}$

Densuead

Construct AABC and see that bisectors of angles are concurrent.



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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

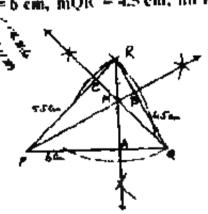
Filot Superone Mathematics 574 Class 9"
Steps of Construct.

- (i) ake a me segment BC 4.2 cm
- (n) Make an ingle 2 CBP 75°
- (iii) Take B us centre and draw an arc of radius 3 6 cm which cuts BP at 5
- (iv) Join A to C ABC is the required mangle
- (x) Take \overline{AP} \overline{BQ} and \overline{CR} bisectors of angles.

Result.

AP BQ and CR are concurrent at point is

- Q.2 Construct the following Δ' PQR, draw their attitudes and show that they are concurrent.
- (i) mPQ = 6 cm, mQR = 4.5 cm, mPR = 5.5 cm
- (ii) mPQ 4.5 cm. mQR = 3.9 cm, m∠R = 45°
- (ni) mRP = 3.6 cm, m∠Q = 30°, m∠P = 105°
- 2(t) = mPQ = 6 cm, mQR = 4.5 cm, mPR = 5.5 cm



Given:

nPO 6 cm

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 575 (Jass 9)

mQR 4.5 cm

mPR = 5.5 cm

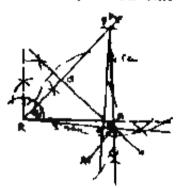
Required. Construct APQR and take their altitudes. Steps of Construction:

- (i) Take a line segment PQ 6 cm
- (ii) Take P as centre and draw an arc of 5.5 radius
- (ii) Take Q as centre and draw an arc of 4.5 radius.
- (iv) Join R to P and Q.
 PQR is the required triangle
- (v) Drop RA . PB and QC perpendiculars to PQ .
 QR . RP respectively

Result.

RA PB and QC are concurrent at M

2(ii) mPQ = 4.5 cm, mQR = 3.9 cm, m \angle R 45°



Given: mPQ 45 cm

mQR 39 cm

m∠R - 45°

Required: Construct APQR and draw its a titude



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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 576 Class 9th Steps of Construction:

- (i) Take $R\bar{Q} = 39$ cm.
- (11) Make an angle ∠QRA ~ 45°
- (m) Take Q as centre and draw an arc of 4.5 cm radius, which cuts RA at P
- (ix) Join P to Q.
 PQR is the required triangle
- (v) Drop QM. RN and PW perpendiculars on RP.

 PQ and RQ respectively

Result:

QM. RN and PW are concurrent at b.

2(iii) mRP = 3.6 cm, $m\angle R = 30^{\circ}$, $m\angle P = 105^{\circ}$





$$m\angle R = 30^{\circ}$$

$$m \angle P = 105^{\circ}$$

Required: Construct APQR and verify that its altitudes are concurrent

Steps of Construction:



Pulot Superone Mathematics 577 CI

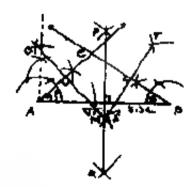
- (1) Take a line segment RP = 3 6 cm
- (ii) Draw an angle ∠PRQ 30°
- (iii) Draw an angle ∠RPQ = 105°

 RM and PW intersect at point Q
 PQR in the required triangle
- (A) Drop RB, PA and QC perpendicular on QP, PA, RP respectively

Result:

RB. PA. QC are concurrent at O.

- Q.3 Construct the following triangles ABC. Draw the perpendicular bisector of their sides and verify their concurrency. Do they meet inside the triangle.
- (i) $mAB = 5.3 \text{ cm}, m\angle A = 45^{\circ}, m\angle B = 30^{\circ}$
- (ii) $m\overline{BC} = 2.9$ cm, $m\angle A = 34^{\circ}$, $m\angle B = 60^{\circ}$
- (iii) mAB ≈ 2.4 cm, mAC ≈ 3.2 cm, m∠A = 120°
- 3(i) mAB = 5.3 cm, m∠A = 45°, m∠B = 30°



Given:

 $m\overline{AB} = 5.3$ cm

m∠A 45°

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 578 Class (**

m∠B = 30°

Required: Construct AABC Draw perpendicular bisectors of its sides and verify their concurrency

Steps of Construction:

- (i) Take a line segment AB = 5 3 cm
- (ii) Make an angle ∠BAW = 45°.
- (iii) Make an angle ∠ABJ = 30°
 AW, BJ intersect at point C
 ABC is the required triangle.
- (iv) Take PQ, TS, UV right bisectors of AB, BC. (A respectively

Results

 \overline{PQ} , \overline{TS} , \overline{UV} are concurrent at point M.

3(ii)
$$m\overline{BC} = 2.9 \text{ cm}, m\angle A = 30^{\circ}, m\angle B = 60^{\circ}$$



Given:

$$m\angle A = 30^{\circ}$$

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 579

Required: Construct triangle ABC Draw perpendicular bisector of its sides and verify their com. concurrency

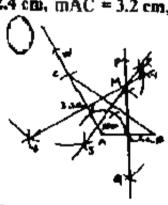
Steps of Construction:

- Take a line segment $\overline{BC} = 29 \text{ cm}$ (i)
- Draw an angle ∠CBW = 60°, (11) Place of A is not known, we find m/C $m\angle C = 180 \quad m\angle B - m\angle A$ m∠C = 180 60 30 = 90°
- (iii) Draw an angle \(\text{BCN} = 90\) PW . CN intersect at point A ABC is the required triangle.
- Take PQ, RS, UV the right bisectors of BC, CA, (iv) AB sides

Result.

PQ, RS, UV are concerrent at point M.

3(iii) $m\overline{AB} = 2.4 \text{ cm}$, $m\overline{AC} = 3.2 \text{ cm}$, $m\angle A = 120^{\circ}$



mAB = 2.4 cm

 $mA\overline{C} = 3.2 \text{ cm}$

m∠A = 120°

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superone Mathematics 580 Class 9th

Required: Construct a AABC and draw perpendiculars of its sides and verify their concurrency

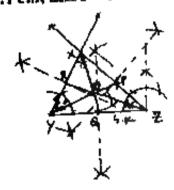
Steps of Construction:

- (i) Take a line segment AB = 24 cm.
- (ii) Make an angle ∠BAW 120° at A.
- (iii) Cut off mAB 32 cm from AW
- (iv) Join C to B
 ABC is the required triangle
- (v) Take PQ, RS, UV right bisectors of AB, BC, CA sides

Result

 \overline{PQ} RS. \overline{UV} are concurrent at point M. (out side the Δ)

- Q.4 Construct the following Δs XYZ. Draw their three medians and show that they are concurrent.
- (i) $m Y \hat{Z} = 4.1 \text{ cm}, m \angle Y = 60^{\circ} \text{ and } m \angle X = 75^{\circ}$
- (a) $m\overline{XY} = 4.5 \text{ cm}, \ m\overline{YZ} = 3.4 \text{ cm}, \ mZ\overline{X} = 5.6 \text{ cm}$
- (iii) $m7\overline{X} = 4.3 \text{ cm}, m\angle X = 75^{\circ}, m\angle Y = 45^{\circ}$
- 4(i) $mYZ = 4.1 \text{ cm}, m\angle Y = 60^{\circ} \text{ and } m\angle X = 75^{\circ}$



Pilot Superone Mathematics 581 Class 9th

Given:

mYZ = 41 cm

m∠Y ~ 60°

 $m \angle X = 75^{\circ}$

Required: Construct AXYZ. Draw medians and verify their concurrency.

Steps of Construct:

Take a line segment $\overline{YZ} = 4.1 \text{ cm}$ (i)

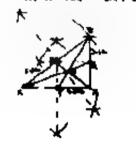
Make an angle ∠ZYW = 60° (i.)

(iii) Make an angle ∠YZS = 45* YW and ZS intersect at X. XYZ is the required triangle.

(iv) Find mid point of YZ, ZX, XY as O.P.R.

Join X to Q, Y to P, Z to R. (v) XQ, YP and ZR are medians hese are concurrent at

mXY = 4.5 cm, mYZ = 3.4 cm, m/X = 5.6 cm4(ii)



Given:

 $m\overline{XY} = 4.5 \text{ cm}$

 $m\overline{Y}\overline{Z} = 3.4 \text{ cm}$

mZX = 56 cm

Required: Construct triangle XYZ. Draw medians and

verify their concurrency



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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

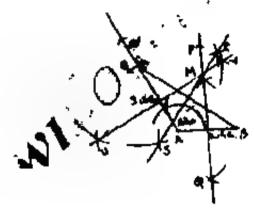
Class 9th Pilot Superone Mathematics 582 Steps of Construction:

- Take a line segment $\overline{XY} = 4.5$ cm. (f)
- Take X as centre and draw an arc of radius 5.6 cm (ü)
- Take Y as centre and draw an ares of radius 3.4 cm (iii) These ares intersect at point /
- (iv) Join 2 to X and Y XYZ is the required triangle
- Find mid points P, Q, R of \overline{XY} , \overline{YZ} , \overline{ZX} (v)
- Draw PZ. QX, RY medians. (vi)

Result:

PZ, QX RY are concurrent at O.

4(iii) $mZX = 4.3 \text{ cm}, m\angle X = 7.5 \text{ m}\angle Y = 45^{\circ}$



m/X = 4.3 cm

m∠X 75°

mZY = 45°

Required: Construct AXYZ and draw its medians and

verify their concurrency

Photosuperone Mathematics 583 Class 9th Steps of Construction.

- Lake a line segment ZX = 4.3 cm.
- (ii) Make an angle \(\angle ZXM = 75^\circ\)
 Place of Y is not known, we find angle at Z.

 iii\(\all Z = 180^\circ \cdot m \angle Y m \angle X\)

 iii\(\all Z = 180^\circ \cdot 45^\circ 75^\circ = 60^\circ\)
- (iii) Draw an angle ∠XZW = 60° at Z.
 ∠W, XM intersect at Y,
 XYZ is the required triangle.
- (iv) Find P. Q. R and points of \overline{ZX} , \overline{XY} , \overline{ZY} as the mid points.

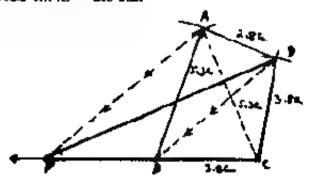
 Join Y to P, Z to Q, X to R

Result:

, Medians YP XR , ZQ are concurrent at point O. EXERCISE 17.3

- Q.1(i) Construct a quadrilateral ABCD, having mAB = mAC = 5.3 cm. mBC = mCD = 3.3 cm. And mAD = 2.8 cm.
- (ii) On the side BC construct a Δ equal in area to the quadrilateral ABCD
- 1(i) Construct a quadrilateral ABCD, having mAB = mAC = 5.3 cm. mBC = mCD = 3.8 cm.

 And mAD = 2.8 cm.



Class 9" Pilot Superone Mathematics 584

Given:

mAB = mAC = 5.3 cm

 $m\overline{BC} = m\overline{CD} = 3.8 \text{ cm}$

 $m\overline{AD} = 2.8 \text{ cm}$

Construct a quadrilateral ABCD Required.

Construct a D equal in area to quad. ABCD.

Steps of Construction:

- Take a line segment BC = 3.8 cm (i)
- Iake B, C as centre and draw two arcs of 53 cm (ii) radius. These intersect each other at A. Join A to B and C.
- Take A as centre and draw an arc of radius 2.8 cm. (111)
- Take C as centre and draw an are of radius 3 8 cm (iv) This cuts the first are at D.
- Join D to A and C. (v) ABCD is the required quadrilateral.

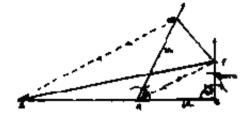
Part II

- Join B to D (vi)
- Take AP BD which meets extended CB at P (vii)
- (viii) Join P to D. PCD is the required triangle which is equal in area to quadrilateral ABCD
- Construct a A equal in area to the quadrilateral. Q.2 PQRS, having $m\overline{QR} = 7cm$. $m\overline{RS} = 6cm$, $m\overline{SP} =$ 2.75, m \(QRS = 60° and m \(RSP = 90° \)



Pilot Superone Mathematics 5

Class 9th



Given:

mQR = 7cm mRS = 6cm, mSP = 275,

 $m\angle QRS = 60^{\circ}$ and $m\angle RSP = 90^{\circ}$

Required:

Construct a triangle equal in area to quadrilateral. PQRS of which measurements

are given.

Steps of Construction:

- (i) Take a line segment RS →6cm
- (ii) Make an angle of 60° at R.
- (iii) Make an angle of 90° at S.
- (iv) Cut off $\overline{SP} = 2.75$ cm.
- (v) Cut off RQ = 7 cm

PQRS is the required quadrilateral

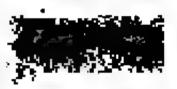
Part II

- (vi) Join P to R. PR is diagonal of the quadrilateral
- (vii) Take QA||RP which meets extended SR at A.

(viii) Join A to P

Recult.

ASP is the required Δ of which area is equal to quadrilateral PQRS

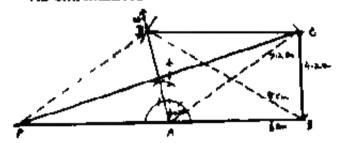


Pilot Superone Mathematics 586 Class 9"

Q.3 Construct a ∆ equal in area to the quadrilateral.

ABCD having mAB = 6 cm, mBC = 4 cm, mAC

- 7.2 cm, m∠BAD > 105° and BD = 8 cm.



Given: $\overline{MAB} = 6 \text{ cm}$, $\overline{MBC} = 4 \text{ cm}$, $\overline{MAC} = 7.2 \text{ cm}$, $\overline{MAC} = 105^{\circ} \text{ and } BD = 8 \text{ cm}$

Required: Construct a quadrilateral, ABCD and a Δ equal in area of ABCD.

Steps of Construction.

- (i) Take a line segment AB = 6 cm
- (it) Make an angle ∠BAW = 105° at A.
- (iii) Take B as centre and draw an arc of radius 8 cm which cuts AW at D.
- (iv) Take A and B as centre and draw arcs of radius 7.2 and 4.5 cm respectively. These intersect at C.
- (v) Join C to B and D.
- ABCD is the required quadrilateral

Part II

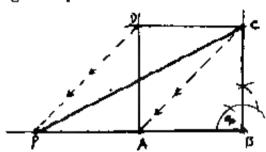
- (vi) Join C to A.
- (vii) Take $\overline{CP} \parallel \overline{CA}$ which meets BA extended at P

Result:

Pilot Superone Mathematics 587 Class 9th

CPB is the required Δ which is equal in area to quadrilateral ABCD

Q.4 Construct a right angled triangle equal in area to a given square.



Given: ABCD is a given square

Required: Construct a right angled triangle equal in area to square. ABCD,

Steps of Construction:

- (i) Take CA the diagonal of the square ABCD
- (ii) Fxtend BA towards A
- (iii) Take DP || CA which meets extended BA at P

Result:

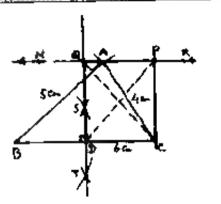
PBC is the required Δ equal in area to square. ABCD

EXERCISE 17.4

Q.1 Construct a Δ with sides 4 cnt, 5 cm and 6 cm and construct a rectangle baving its area equal to that of the Δ. Measure its diagonals. Are they equal?



Prior Superone Mathematics 588 Class 9th



Given: mBC 6cm $\overline{\text{mAB}} = 5$ cm $\overline{\text{mAC}} = 4$ cm

Required: To construct the triangle and a rectangle equal in area to the Δ_k

Steps of Construction:

- (1) Lake line segment BC = 6 cm.
- (ii) Take B and C as centre and draw are of radii 4, 5 cm respectively. These ares intersect at A.
- (m) loin A to B, C

 Also s the required triangle
- (it) Draw NAP | to BC passing through A.

 Lake right bisector WS which cuts BC at D and NP at O.
 - (vi) Take Q as centre and draw an arc of radius DC
 - (vii) Take C as centre and draw an arc of radius \overline{DQ} , which cuts the first arc at P
 - (vih) Join P to Q and C.

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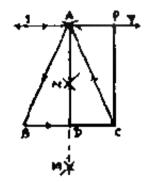
MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Priot Superone Mathematics 589 Class 9th

Result

DCPQ is the required rectangle which is equal in area to \triangle ABC in DP = mQC = 4.5 cm

Q.2 Transform an isosceles Δ into a react angle.



Given: ABC is an isoscoles \triangle an which $\overline{AB} \ge AC$

Required: To construct a rectangle equal in area to the Δ .

Steps of Construction:

- (1) Take SAT | BC passing through A.
- (ii) Take right bisector of BC which cuts BC at D and passes through A
- (in) Take A as centre and draw an arc of radius DC which cuts ST at P.
- (iv) Joan P to C

Result:

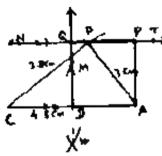
ADCP is the required rectangle which is equal in area to \triangle ABC.

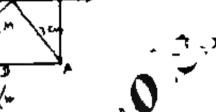
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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilos Superone Mathematics 590 Class 9th

Q.3 Construct a \triangle ABC such that mAB = 3 cm, mBC = 3.8 cm, mAC = 4.8 cm. Construct a rectangle equal in area to the \triangle ABC, and measure its sides





Given: ABC is a triangle that

$$mA\hat{B} = 3 cm$$

$$mB\overline{C} = 38 cm$$

Required: Construct the ΔABC and a rectangle equal in area to ΔABC

Steps of Construction:

- (i) Take a line segment $\overline{CA} = 4.8$ cm.
- (ii) Take C and A as centre and draw arcs of 3.8 cm, 3 cm radii respectively. These cut each other at B.
- (iii) Join B to C and A

 ABC is the required Δ.
- (N) Take NBT || CA which passes through B
- (v) Take right bisector of CA which cuts CA at D and NT at Q.
- (vi) Cut off OP = mOD and P to A



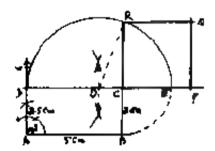
Priot Superone Mathematics 591 Class 9th Result:

QDAP is the required rectangle equal in are to ABC

$$m\overline{DA} = 2.4 \text{ cm}, m\overline{DO} = 2.4 \text{ cm}$$

EXERCISE 17.5

Q.1 Construct a rectangle whose adjacent sides are 2.5 cm and 5 cm respectively Construct a square having area equal to the given rectangle.



Given: Sides of a rectangle are 2.5 cm, 5 cm

Required: (i) Construct rectangle

(ii) Construct a square equal in area to the rectangle

Steps of Construction:

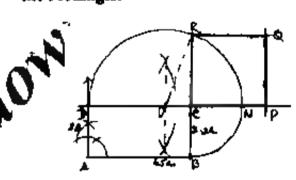
- (i) Take a line segment $\overline{AB} = 5$ cm
- (ii) Make an angle of 90° at A.
- (iii) Cut off 2.5 cm AD and AW
- (iv) Draw arcs with centre at D, B respectively of radius 5 cm and 2.5 cm. These cut each other at C.
- (v) Join C to D, B.ABCD is the required rectangle.



Pilot Superone Mathematics 592 Class 9th

Part II

- (vi) Extend DC towards C
- (vii) Cut off CE = BC i.e 2.5 cm on DN
- (viii) Find midpoint O of DE
- (ix) Take O as centre and a semicircle on \overline{DE}
- (x) Extend side BC towards C which meets the semicircle at R.
- (xi) mRC is the ength of the required square
- (xii) Cut off $\overline{CP} = CR$ on \overline{DF}
- (KIII) Take R and P as centre and draw two ares that cut each other at O.
- (xiv) Jom Q to R and P.
 CPQR is the required square whose area is equal to the area of rectangle ABCD
- Q.2 Construct a square equal in area to a rectangle whose adjacent sides are 4.5 cm and 2.2 cm respectively. Measure the sides of the square and find its area and compare with the area of the rectangle.



Given: Sides of a rectangle are 2.5 cm, 5 cm.

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot Superione Mathematics 593 Cla

Required: Construct the rectangle and construct a square equal in area to the rectangle

Steps of Construction:

- (i) Take a line segment AB= 4.5 cm
- (ii) Make an angle ∠BAW = 90° at A.
- (iii) Cut off 2.2 cm from AW as AD.
- (iv) Fake D and B as centre and draw of radius 4.5 and 2.2 cm respectively. There are scut each other at C.
- (v) Join C to D and B.ABCD is the required rectangle.

Pari II

- (yi) Extend DC towards C.
- (vii) Cut of $\overline{CE} = \overline{CB} = 2.2$ cm on \overline{DN}
- (viii) Find midpoint O of DE.
- (ix) Take O as centre and draw a semi-circle on DE taking OD as radius
- (x) Extend BC towards C which meets the semicircle at R. anRC is the length of side of the required
- (xi) Cut off CP = mRC on DN.
- (xii) Take R and P as centre and draw two arcs of radius CR. These cut each other at Q.
- (Kirii) Jour Q to R and P

Result:

CPQR is the required square whose area is equal to area of rectangle ABCD.



Pilot Superone Mathematics	594 Class 9*
Part II	
Area of the rectangle	4.5 × 2.2
	- 9.9 sq. cm
Side of the square	= 3.1 cm
Area of the square	= 3.1 × 3 L
•	· 9.6 sq. cm
Area of the square 15	approximately equal to the

Q.3 In Q.2 above verify by measurement that the perimeter of the square is less than that of the

rectangle.

Solution:

Perimeter of the rectangle = 2(4.5 + 2.2)= 2(6.7)

- 13 4 cm

Side of the square

3.1 cm

Perimeter of the square

= **4**(3.1)

= 12.4 cm

Marie

12.4 < 13.4

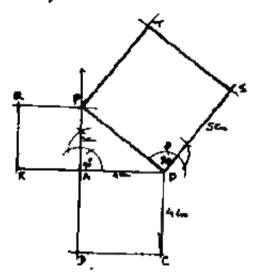
Charagore.

Perimeter of the square is less than the perimeter of the rectangle.



Pilot Superone Mathematics 595 Class 9"

Q.4 Construct a square equal to area to the sum of two squares having sides 3 cm and 4 cm respectively.



Given: Two square having 3 cm and 4 cm sides are given.

Required: To construction a square equal in area to the sum of the area of two squares.

Steps of construction.

- (i) Take a line segment mAB = 4 cm
- (ii) . Complete square ADCB on AB
- (hii) Extend DA towards A and cut off AP = 3 cm.

 OR Make an angle of 90° at A and cut off AP = 3 cm.
- (iv) Construct a square ARQP on AP
- (v) Join B to P
 ABP is a right angled triangle of which one side is 4 cm and the other side is 3 cm.

Pilot Supergne Mathematics 596 Class 9th

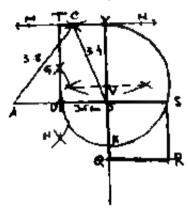
(vi) Construct a square on hypotenuse BP

Result:

$$(mPB)^2 = (mAB)^2 + m(AP)^2$$

(P) thagorean theorem)

Q.5 Construct a Δ having base 3.5 cm and other two sides equal to 3.4 cm and 3.8 cm respectively. Fransform it into an equal square.



Given: ABC is a triangle by which (suppose)

mAB • 3.5 cm

mAC = 3.8 cm

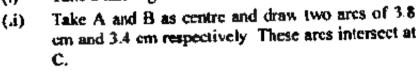
m8C = 3.4 cm

Required: Fo construct a square equal in area to the triangle ABC

Steps of Construction:

Part I

(1) Take a line segment AB = 3.5 cm





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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

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(iii) Join C to A and B.

ABC is the required A.

Part II

- (i) Take MN (AB passing through C
- (ii) Take right bisector GH of AB which bisects AB at O, and MN at I
- (iii) Sides line segments OT and OB are the sides of a rectangle
- (iv) Complete rectangle OBYT its area is equal to the area of AABC

Part II

- (i) I xtend YB towards B.
- (ii) Cut off BK = mBC on \overline{YW}
- (iii) Find midpoint V of BK
- (iv) I ake V as centre and draw a semicircle on YK
- (v) Extend OB towards B which meets the semicircle at S.
- (vi) Complete square on BS square BQRS is equal in area of rectangle OBYT

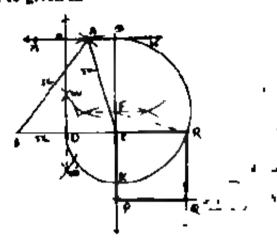
From Part I, II, III

Square BQRS is equal in area to triangle ABC.



Pilot Superone Mathematics SAB Loass 9

Q.6 Construct a A having base 5 cm and other sides equal to 5 cm and 6 cm. Construct square equal in area to given A.



Given: Let $\triangle BC$ be the D in which $\triangle BC = 5$ cm

mAB 6cm

mĀČ ≈5 cm.

Required. Construct a square equal in area to \triangle ABC.

Steps of construction:

Part I

- (i) Take a line segment $\overline{AB} = 5$ cm
- (ii) Take B and C as centre and draw two arcs of radius 6 cm, 5 cm, respectively. These cut each other at A.
- (iii) Josn A to B and C ABC is the required Δ.

Part 11

(i) Take MN | BC pessing through A.

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MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Filot Superone Mathematics 599 Class 9th

- (ii) Take WW right bisector of BC at O and cuts MN
 at E.
- (iii) Complete the rectangle EOCD which is equal in area to AABC

Fore III

- (i) Extend DC side of rectangle towards C and take mCK = mCO
- (ii) Find F the midpoint of DK
- (m) Take F as centre and complete a semicircle on \widetilde{DK}
- (iv) Extend OC towards C, this cut the semicircle on R.
- (v) Complete square CRQP and its area is equal to the area of rectangle EOCD

Result!

Area of square CRQP is equal to the area of rectangle EOCD which is equal to the area of the triangle ABC.



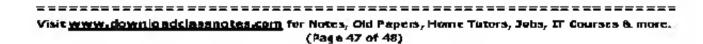
E L

P214 2		view Exerci		
		lowing blanks to ma		
(i)	90° is	side of a right angi		
(ii)		ine segment joining mid-point of its o	_	_
(iii)	A lin	e drawn from a ver	ntex of a	triangle which
	17.10	to its o	pposite s	ide is called an
(6.3		de of the triangle.		
(iv)	are_	bisectors of the thr	ce angre	of a franche
(v)	The p	mint of concurrence	y of the	right bisectors.
	of the	three sides of the .	riangle is	1
	from	its vertices.		
(vi)		its vertices. or more triangles a	ure said t	o be simular if
(vi)	Two			
(vi)	Two	or more triangles a		
(vi) (vii)	Two they corre	or more triangles a are equiangular a	and meas	sures of their
	Two they corres The a	or more triangles a are equiangular a sponding sides are	ind meas	sures of their
(vii) Answ	Two they corres The a the rers:	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the	iangle an	sures of their e concurrent at the.
(vii) Answ	Two they correct The a	or more triangles a are equiangular a sponding sides are kitudes of a right tr	iangle an	sures of their
(vii) Answ	Two they correst The athe (ers: (iii)	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the bypotenuse perpendicular	iangle an right ang (ii) (iv)	e concurrent at the concurrent at the concurrent at the concurrent
(vii) Answ	Two they correct The a the _ (ers: (ii) (iii) (v)	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the bypotenuse perpendicular equidistant	iangle an right ang (ii) (iv)	sures of their concurrent at the the
(vii) Answ	Two they correct The a the _ (ers: (ii) (iii) (v) (viii)	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the hypotenuse perpendicular equidistant vertex	iangle and right ang (ii) (iv) (vi)	e concurrent at the concurrent at concurrent proportional
(vii) Answ	Two they correct The a the _ (ers: (ii) (iii) (v) (viii) iple Ch	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the bypotenuse perpendicular equidistant	iangle and right ang (ii) (iv) (vi)	e concurrent at the concurrent at concurrent proportional
(vii) Answ	Two they correct The a the _ (ers: (ii) (iii) (v) (viii) iple Ch er.	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the hypotenuse perpendicular equidistant vertex olde Questions. Ch	iangle and right ang (ii) (iv) (vi)	e concurrent at the concurrent at concurrent proportional correct
(vii) Amsw Amsw A triz	Two they correct The a the _ (ers: (iii) (viii) (pie Ch er. ungle ha	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the bypotenuse perpendicular equidistant vertex olde Questions. Ch	iangle and right ang (ii) (iv) (vi) cose the gruent is o	e concurrent at the concurrent at concurrent proportional correct
(vii) Answ Answ A triz (a) se	Two they correct The a the _ (ers: (ii) (iii) (v) (viii) iple Ch er.	or more triangles a are equiangular a sponding sides are kitudes of a right tr of the hypotenuse perpendicular equidistant vertex olde Questions. Ch wing two sides cong (b) right a	iangle and right ang (ii) (iv) (vi) cose the greent is congled	e concurrent at the concurrent at concurrent proportional correct

Written/Composed by: - <u>SHAHZAD 1FTIKHAR</u> Contact # 03 13-5665666 Website: <u>www.downloadclassnotes.com</u>, E-mail: <u>raoshahzadiftikhar@qmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot	Superone Mathemati	cs 60 Class 9	<u>*</u>			
	(*) parallelogram	(b) rectangle				
	(c) trapezium	(d) rhombus				
(iii)	The right bisectors	of the three sides of a triangle are:				
	(a) congruent	(b) collinear				
	(c) concurrent	(d) parallel				
(iv)	The altitudes of an isosceles triangle are congruent:					
	(a) two	(b) three				
	(c) four	(d) none	-			
(v)	1 /	from the end points of a line				
	(a) bisector	(b) right-bisector				
	(c) perpendicular	(d) median				
(vi)	riangles can be made by joining the des of a triangle:					
	(a) three	(b) four				
	(c) five	(d) two				
(vii)	The diagonals of other:	a parallelogram each				
	(a) bisect	(b) trisect				
	(c) bisect at right an	gle(d) none of these				
(viii)	The medians of a	triangle cut each other in the ratio:				
	(a) 4:1	(b) 3 : I				
	(c) 2:1	(d) 1:1				
(ix)	One angle on the	base of an isosceles triangle is 30°.				
•	What is the measure	e of its vertical angle:				
	(a) 30°	(b) 60°				
	(c) 90°	(d) 120°				
(1)		of a triangle are congruent, then				
	the triangle is:					
	(a) equilateral	(b) right engled				
	(c) isosceles	(d) acuse angled				



Written/Composed by: - <u>SHAHZAD 1FTIKHAR</u> Contact # 03 13-5665666 Website: <u>www.downloadclassnotes.com</u>, E-mail: <u>raoshahzadiftikhar@gmail.com</u>

MATHEMATICS FOR 9TH CLASS (UNIT # 17)

Pilot	Superone Ma	thematic	<u> </u>	02		Q	155 9°°
(xi)	It two med triangle w		riangle	are cor	gruen	then the	•
	(a) isoscel	(b) equilateral (d) acute angled					
	(c) right an						
	American:		, .				
	1 10 14	(iii)	ь	(iii)	¢	(17)	a
	(v) b	svij	ь	(vill)		cotto	C
	(m) , d	(x)		(xi)	a	I .	
QJ.	Define the	following	t				
(i)	ls-centre		(ii)	Circ	um-ce	ntre	
(iii)	Ortho-cen	tre	(iv)	Cent	roid		
(v)	Point of concurrency						
(i)	la-centre: interior un	•					លាន ប
(11)	Circum-ce right bisect centre.						
(iii)	Ortho-cer altitudes of		-		-		ree
(iv)	Centroid: of a triangl				ey of th	ree mode	ians

(v) Point of concurrency: If three or more than three straight lines, rays, line-segments, intersect each other at a single point then that point is a point of concurrency of these straight lines, rays or line-segments.